Experimental and numerical analysis for high intensity swirl based ultra-low emission flameless combustor operating with liquid fuels

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Title: EXPERIMENTAL AND NUMERICAL ANALYSIS FOR HIGH INTENSITY SWIRL BASED ULTRA-LOW EMISSION FLAMELESS COMBUSTOR OPERATING WITH LIQUID FUELS

Article Type: Research Paper

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EXPERIMENTAL AND NUMERICAL ANALYSIS FOR HIGH INTENSITY SWIRL BASED ULTRA-LOW EMISSION FLAMELESS COMBUSTOR OPERATING WITH LIQUID FUELS

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V. Mahendra Reddy\textsuperscript{1,2}, Amit Katoch\textsuperscript{1}, William L. Roberts\textsuperscript{2}, Sudarshan Kumar\textsuperscript{1}

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Abstract:

Flameless combustion offers many advantages over conventional combustion, particularly uniform temperature distribution and lower emissions. In this paper, a new strategy is proposed and adopted to scale up a burner operating in flameless combustion mode from a heat release density of 5.4 to 21 MW/m\textsuperscript{3} (thermal input 21.5 – 84.7 kW) with kerosene fuel. A swirl flow based configuration was adopted for air injection and pressure swirl type nozzle with an SMD 35-37 µm was used to inject the fuel. Initially, flameless combustion was stabilized for a thermal input of 21.5 kW (\(\dot{Q}'\))=5.37 MW/m\textsuperscript{3}). Attempts were made to scale this combustor to higher intensities \textit{i.e.} 10.2, 16.3 and 21.1 MW/m\textsuperscript{3}. However, an increase in fuel flow rate led to incomplete combustion and accumulation of unburned fuel in the combustor. Two major difficulties were identified as possible reasons for unsustainable flameless combustion at the higher intensities (i) A constant spray cone angle and SMD increases the droplet number density (ii) Reactants dilution ratio (\(R_{dil}\)) decreased with increased thermal input. To solve these issues,
a modified combustor configuration, aided by numerical computations was adopted, providing a chamfer near the outlet to increase the $R_{dit}$. Detailed experimental investigations showed that flameless combustion mode was achieved at high intensities with an evenly distributed reaction zone and temperature in the combustor at all heat intensities. The emissions of CO, NO$_x$ and HC for all heat intensities ($\Phi=1 - 0.6$) varied between 11 - 41, 6 - 19 and 0 - 9 ppm, respectively. These emissions are well within the range of emissions from other flameless combustion systems reported in the literature. The acoustic emission levels were also observed to be reduced by 8-9 dB at all conditions.

**Keywords:** Flameless combustion; Swirl flow combustion; Liquid fuel; High intensity; Burner scaling; Ultralow emissions; Residence time.

1. **Introduction:**

Flameless/Mild combustion has gained significant importance due to its ability to suppress thermal NO formation and improve thermal efficiency of combustion systems. Flameless combustion has been primarily identified with gaseous fuels and extensive work has been reported [1-10]. Scaling the flameless combustors to higher intensities has been proposed in recent studies reported in the literature [7, 8, 11]. A brief summary of various high intensity flameless combustion systems with gaseous fuels is listed in Table 1. Lückerath *et al.*, [11] have developed a Forward Flow (FF) combustor configuration with a thermal input of 475 kW and heat intensity of 240 MW/m$^3$ (at 20 bar). Kumar *et al.*, [7] have scaled up a high-intensity combustor (5-150 kW thermal input) with new scaling methodology and compared various existing scaling techniques *i.e.* Constant Velocity (CV), Constant Residence Time (CRT) and Cole’s approach with the proposed technique. The comparison of Weber [12] shows that CRT approach is relatively better for scaling swirl type combustor configurations. They have hinted at
the need of maintaining high reactant dilution rates to ensure that flameless combustion mode is achieved in scaled combustors. These types of combustor configurations with high heat intensity are expected to be useful in gas-turbine applications. Arghode and Gupta [8] have demonstrated a laboratory scale combustor achieving colorless distributed combustion with a high intensity of 453 MW/m$^3$ ($Q_{th} = 6.25$ kW) with a combustor volume of ~13 cm$^3$ and Reverse Flow (RF) configuration. Scaling of these concepts with low thermal input and high heat intensity render the systems very complex and making their implementation highly challenging. Further, very little literature is available in the field of scaling of flameless combustors with liquid fuels. Some basic studies on flameless/mild combustion with liquid fuels [3, 5, 13-15] have been reported recently. Traditional industrial burners and stationary gas-turbine combustors operate with liquid fuels at higher thermal inputs (~1 MW) and higher heat intensities (100 MW/m$^3$). Therefore, additional studies are required to investigate the issues related to the scaling of high intensity flameless combustors with liquid fuels and their relation with spray characteristics.

In this study, a swirl based combustor operating in flameless combustion mode with kerosene at 21.5 kW (base case, $Q'''' = 5.37$ MW/m$^3$) [16], is developed and scaled up to operate at 85 kW (21.1 MW/m$^3$). Attempts were made to achieve flameless combustion with higher intensity of 10.2, 16.3 and 21.1 MW/m$^3$ using the base case combustor configuration with increased thermal input of 40.8, 65.1 and 84.7 kW respectively. However, the existing combustor configuration was unable to achieve stable flameless combustion. Computational and experimental studies were carried out to identify the causes preventing successful scale-up of the combustor. The combustor configuration was modified by providing a chamfer, thus increasing the degree of recirculation in the combustor, allowing stable flameless combustion. Computational studies show that with increased chamfer radius ($R_c$), recirculation of the combustion products and fuel
residence time increased. Three different $R_c$ values were considered, for the 10.2, 16.3 and 21.1 MW/m$^3$ cases respectively, and shown to achieve combustion with low emissions. The influence of spray characteristics on scaling the combustor was studied and the results are presented in this paper.

2. Computational Studies

2.1 Geometry design methodology

The base combustor was designed to stabilize high intensity flameless combustion using conventional liquid fuels. Stabilization of flameless combustion with liquid fuels depends on three important parameters,

1. Sauter Mean Diameter (SMD) of the spray. The evaporation rate is a function of boiling point and surface area to volume ratio ($A_s/V$) of the droplet. The evaporation time increases with increasing boiling temperature and SMD.

2. A group of parameters including droplet distribution, evaporation, mixture formation and subsequent combustion with preheating and dilution of reactants.

3. In flameless combustion mode, the increased dilution of fresh reactants with hot combustion products results in reduced reaction rate. Due to this, reaction zone is uniformly distributed throughout the combustor volume with lower peak flame temperature than that of conventional mode [4]. In conventional mode, the fuel spray directly enters the combustion zone having higher peak temperature. Therefore, the droplet evaporation rate is relatively slower in flameless combustion mode [4]. To achieve complete evaporation and combustion, the droplet residence time should be higher in flameless combustion mode.
To sustain flameless combustion with liquid fuels, the above three issues can be addressed by increasing the residence times and recirculation as compared to flameless combustion with gaseous fuel. A swirl flow creates a central vortex zone and low pressure gradient, supporting a large reverse flow region in the combustor. High swirl creates higher centrifugal force that enhances the residence time of the hot gases trapped within the swirling flow [13-20]. The increased residence time enhances the flame stability limits and rate of mixing of products and reactants. The high recirculation allows for good mixing, essential for obtaining a distributed reaction zone over a large volume of the combustor [13-20]. Therefore, a tangential air injection scheme was used in this study to generate the swirl flow in the combustor.

In this study, a conical combustor with 60° diverging angle was considered with a total volume of ~0.004 m$^3$ [16, 21]. A pressure swirl fuel injector was used for injection of kerosene. The combustor configuration is shown in Fig. 1. Computational and experimental studies were carried out simultaneously. Recirculation of combustion products was identified as the key factor to sustain flameless combustion. Hence, the reactants dilution ratio ($R_{dil}$) is the governing metric. $R_{dil}$ is calculated as follows [14, 16].

\[
R_{dil} = \frac{\dot{m}_{axial} - (\dot{m}_{ox} + \dot{m}_f)}{(\dot{m}_{ox} + \dot{m}_f)}
\]

\[
\dot{m}_{axial} = \iiint \rho v_{axial} dy dz
\]

2.1.1 Challenges in scaling

Initially, the combustor was tested at 21.5 kW thermal input using the unmodified combustor configuration (without chamfer, i.e. $R_c=0$ mm) and exit diameter (D) of 25 mm. Well stabilized
flameless combustion was observed experimentally [16, 21]. Computational results showed that $R_{dit}$ varied spatially from 1.1 to 3.2. The same combustor was tested at higher thermal inputs of 40.8, 65.1 and 84.7 kW (respective heat intensities 10.2, 16.3 and 21.1 MW/m$^3$) and experimental observations revealed that, flameless combustion was not stabilized in the combustor at these higher inputs and large quantities of unburned fuel accumulated in the combustor. The fuel spray cone angle was maintained constant at 45° for all nozzles and SMD of all nozzles were in the range of 35-37 µm (details in Section 4.1). Therefore, with the increased fuel mass flow rate, droplet number density (DND) also increased. Hence, more recirculation (increased residence time) would be required to increase the entrainment and to achieve complete evaporation. The computational results also revealed that, $R_{dit}$ decreased with increasing thermal input. Computational and experimental evidence suggested that $R_{dit}$ needed to be sufficiently high for all thermal inputs to provide the required entrainment and residence time.

CRT approach appears suitable for scaling swirl combustors operating with gaseous fuels [12]. However in case of liquid fuels, the DND increases with thermal input. The residence time should be increased for complete evaporation and combustion. CV scaling approach for higher thermal inputs results in increased combustor volume and reduced heat intensity [7, 12]. Hence, for the present case, both CV and CRT approaches are not suitable. Similarity of certain dimensionless quantities in scaling is different for various combustor configurations, operating conditions and modes of combustion [22]. Therefore, a combination of experimental and numerical simulations aimed at improving the droplet residence times and recirculation rates were considered. To enhance both droplet residence time and recirculation rate, a chamfer at the top of the combustor is provided as shown in Fig 1. A computational analysis (described below)
was carried out for high thermal inputs, by varying chamfer radius \( R_c \) to determine the \( R_{dlt} \) for each case and the operating conditions that yielded an \( R_{dlt} > 2.5 \). The combustor geometry for different thermal intensities is non-dimensionalized with \( D \), as shown in Fig. 1 and listed in Table 2.

### 2.1.2 Numerical method

A general purpose CFD code Fluent-14.5 was used for computational studies in this work. A 3-D double-precision pressure-based solver was used. For all thermal inputs, tangential air inlet and combustor exit velocities were maintained constant to ensure similar level of pressure drop across the combustor. Therefore, the air inlet diameter \( (d_{in}) \) and exit diameter \( (D) \) are increased with increased thermal input. Chamfer radius is varied from 10 to 30 mm at 5 mm increments.

Three-dimensional Navier-Stokes equations were discretized and solved in a finite-volume domain. Reynolds Stress Model (RSM) was used for turbulence modeling. The energy equation was solved considering 20 intermediate species equilibrium chemistry and a non-premixed droplet combustion model for simulating the combustion of the liquid fuels. Compressible flow was considered and the viscosity was calculated using Sutherland’s law. Specific heats were defined as a function of the temperature (piecewise-polynomial). A P1 radiation model was used. Constant mass-flow inlet condition normal to the boundary surface was applied at air inlets, and a pressure outlet based boundary condition was applied at the exit. No-slip wall and constant temperature boundary conditions were applied at the walls. Non-premixed droplet evaporation and combustion, following the spherical law was considered with PDF droplet evaporation. A single component surrogate, \( \text{C}_{12}\text{H}_{23} \) was used to simulate kerosene with a density of 780 kg/m\(^3\).
Fuel injection was simulated as a solid cone type spray with a droplet diameter of 36 µm and a cone angle of 45°. The amount of heat removal from the combustor walls is 3.2, 8.3, and 12.9 kW respectively, for three higher heat intensities of 10.2, 16.3 and 21.1 MW/m³. The heat removal through wall cooling is considered by applying heat-loss through combustor walls as heat flux boundary condition for higher heat intensity cases. The solution is considered to be converged when RMS residuals of the system were less than 1×10⁻⁶. A number of computations were carried out using hexa mesh with different mesh sizes varying from 1.1-2.5 mm. The number of cells for computations was varied from 2 to 4.5 million elements. A mesh size of 1.2 mm was considered sufficient to obtain grid-independent results with approximately 3.6 million grid points. The grid convergence was calculated based on the Grid Convergence Index (GCI) criteria. If the GCI for two successive grid sizes was below 3%, it was considered that grid convergence has been achieved [15].

2.2 Reactants dilution ratio \( (R_{dl}) \)

\( R_{dl} \) was calculated at different axial planes of the combustor. For the case of \( Q_{th}=21.5 \) kW \( (R_C=0 \) mm) with exit port diameter of 25 mm, a maximum \( R_{dl} \) of 3.2 was achieved. Complete flameless combustion with low emissions was observed experimentally. \( R_{dl} \) was calculated for higher thermal inputs \( (Q_{th}=40.8, 65.1 \) and \( 84.7 \) kW) with different \( R_C \) of 10, 15, 20, 25 and 30 mm and results are shown in Fig. 2. It was observed that, for constant thermal input and increasing \( R_C \), the degree of flow reversal increased in the combustor. The resulting \( R_{dl} \) increased with \( R_C \). For instance, at \( Q_{th}=21.5 \) kW, a maximum \( R_{dl} \) of 5.22, 5.77, 6.26 and 6.75 was obtained for \( R_C = 10, 15, 20 \) and 25 mm respectively (Fig. 2a). The curved profile of the combustor dome and chamfer near the exit combined to form curved vanes promoted a large degree of flow reversal. Hence, \( R_{dl} \) increased with increased \( R_C \). For a constant \( R_C \) and
increasing thermal input, $R_{dil}$ was calculated as shown in Fig 2a-d. For example, at $R_c=25$ mm, the maximum $R_{dil}$ calculated were 6.77, 3.75, 3.51 and 2.71 respectively, for 21.5, 40.8, 65.1 and 84.7 kW. Therefore, it was observed that with increasing thermal input, the chamfer radius must be increased appropriately to maintain a constant $R_{dil}$ for all thermal inputs. The zone length of $R_{dil} > 2.71$, which is the lower limit for achieving flameless combustion is calculated for all computational conditions and shown in Fig. 2e. It was observed experimentally that an $R_c=20, 25$ and 30 mm were sufficient to achieve flameless combustion at higher heat intensities (10.2, 16.3 and 21.1 MW/m$^3$ respectively).

2.3 Residence Time Distribution

The residence time of the reactants in the combustion chamber is a significant parameter to achieve flameless combustion [23]. Three basic time parameters were considered to calculate the residence time of reactants.

1. Average residence time; $\tau_{avg} = \left(\frac{V}{\dot{v}}\right)$: $V= $ combustor volume and $\dot{v}= $ volume flow rate of reactants. However, since the present combustor operates with a swirl flow, the residence time was calculated computationally for different cases by injecting particles from air/fuel inlets in the combustor.

2. Swirl based residence time with $R_c=0$ mm; $\tau_{s(Rc=0\,mm)}$.

3. Swirl based residence time with $R_c=25$ mm; $\tau_{s(Rc=25\,mm)}$.

The calculated $\tau_{avg}$ decreased from 0.61 to 0.15 s as the thermal input increased from 5.37 to 21.1 MW/m$^3$. The calculated $\tau_{s(Rc=0\,mm)}$ with swirl flow, decreased from 0.76 to 0.29 s and $\tau_{s(Rc=25\,mm)}$ decreased from 0.98 to 0.69 s for this same range of thermal inputs. For the case of 21.1 MW/m$^3$, the percentage increase in residence time is 93 and 360 % for $\tau_{s(Rc=0\,mm)}$ and
respectively as compared with $\tau_{avg}$. It was observed from the computational study that the residence time increased with both swirl flow pattern and increased chamfer radius ($R_C$). Residence time distribution, $E(t)$ [23] was calculated for all cases by considering the combustor as a well-stirred reactor and shown in Fig. 3. The $E(t)$ of the reactor is the probability density function of a particle in the reactor. If $E(t)$ of a reactor is high, the residence time of the particle is large. It is observed from Fig. 3 that $E(t)$ increases with swirl flow, and increases further with chamfer plus swirl flow.

3 Details of experimental methodology

3.1 Experimental setup

Figure 4 shows a schematic diagram of the experimental setup. The combustor was placed vertically on a test stand. Kerosene was stored at a pressure of 9 bar ($\Delta P$) in a pressurized stainless-steel tank. The fuel injector was located at the center of the combustor. The fuel injector imparts a clockwise rotation to fuel spray; hence a counter-clockwise air injection was selected to impart more shear force to the flow resulting in enhanced mixing and evaporation of droplets. Air supply to the combustor was regulated through electric mass flow controllers (accuracy ±1.5% of full scale).

3.2 Experimental procedure and instruments

Initially, the premixed LPG-air mixture was ignited with a spark and combustor was run for 2-3 min to preheat the combustor. The kerosene fuel is injected at 5 bar pressure by opening the ball-valve in the fuel line. The LPG flow rate was then gradually reduced and the kerosene injection pressure was simultaneously raised to 9 bar. A stable flame was established in conventional combustion mode with stoichiometric kerosene-air mixture for next 4-5 min. After an initial
start-up time of 7-8 min, the combustor wall temperature reached ~ 900 K. A chamfered flange was placed at the top to effectively reduce the exhaust port diameter from 90 mm to a diameter (D) for the particular heat intensity (Table 2). The conventional flame then gradually shifted to a flameless combustion mode. This strategy was adapted to understand and evaluate the effect of exit port diameter variation on transition between conventional (90 mm) and flameless combustion mode (30 mm). The present combustor can be started with the top components in place for a real practical application.

Exhaust gas composition was measured with a gas analyzer which included O$_2$ analyzer (0-25% range, 0.1% accuracy), CO analyzer (0-10000 ppm, ±5 ppm accuracy), NO analyzer (0-5000 ppm, ±1 ppm accuracy), CxHy analyzer (0-50,000 ppm), and CO$_2$ analyzer. Temperature measurements were carried out with R-type ($d_{junction}=1$ mm) thermocouples. The sound level at the exit (100 mm away from axis) of the combustor was measured for different combustion modes with a fast response (Resolution=0.1 dB, $\tau_{response}=200$ ms) sound level instrument.

4 Results and discussion

4.1 Spray characteristics

In the present study, four nozzles N1 - N4 with mass flow rates of 1.72, 3.27, 5.21 and 6.78 kg/h respectively, were used to provide 21.5, 40.8, 65.1 and 84.7 kW thermal inputs respectively. An injection pressure of 9 bar was maintained for all experiments. Various details of the spray characteristics such as $D_{10}$, $D_{32}$ (SMD), $D_{V10}$, $D_{V50}$ and $D_{V90}$, droplet distribution, droplet number density (DND) were measured with a particle shadowgraphy technique. 7000-9000 droplets were considered in each sample size. A count of 150 pictures was selected for each sample at an axial position of 45 mm from the nozzle tip.
It was observed that for all four nozzles, SMD was in the range of 35-37 µm and variation in other diameters was relatively very small. Since the spray cone angle and droplet diameters were nearly the same for all four nozzles, the DND increased for higher mass flow nozzles, the measured DND for N1-N4 nozzles was $32 \times 10^3$, $64 \times 10^3$, $110 \times 10^3$ and $167 \times 10^3$ n/cm$^3$ respectively. Therefore, entrainment of hot gases needed to be increased significantly with the increasing DND to achieve complete evaporation of all droplets. The DND distribution for all four nozzles is shown in Fig. 5.

4.2 Temperature distribution

Temperature variation in the radial direction of the combustor at an axial location of 120 mm was measured for different heat intensities at $\Phi=0.92$ and comparison with predicted results is shown in Fig. 6. Due to larger thermocouple response time (~0.25 s) as compared to integral turbulence time-scales (~3 ms), it is difficult to measure actual temperature variation in the combustor. However, temperature variation with time is measured at a given location and the mean was calculated from recorded temperatures over a period of 10 – 20 seconds. The measured temperature was corrected by considering convection and radiation losses from the thermocouple junction. For the case of 5.37 MW/m$^3$, the wall temperature of the combustor was ~800 K. When the combustor was operated at 10.2 MW/m$^3$, the walls became red hot. Hence, cooling of outer walls of the combustor was mandatory for higher heat densities, achieved through water circulation through copper tubes brazed on the outer walls of the combustor. A constant wall temperature of ~950 K was maintained for higher heat intensities (10.2-21.1 MW/m$^3$). The heat removal through wall cooling is 3.2, 8.3, and 12.9 kW respectively for three
higher heat intensities of 10.2, 16.3 and 21.1 MW/m$^3$. Fresh air at ambient temperature entered the combustor and circulated on the inner walls; a sharp rise in temperature of the air was observed near the walls of the combustor (Fig. 6). Temperature at all radial locations increased with increasing heat intensity of the combustor. As expected, the temperature increased from the walls to the center line of the combustor. The temperature difference across the plane, from axis to near wall (0.0975 m) for 5.37 MW/m$^3$ with $R_e=0$ mm was 443 K. The temperature difference for higher heat intensities (10.2-21.1 MW/m$^3$) was 319, 293 and 245 K respectively. With increased heat intensity, the overall temperature of the combustor and the temperature of the fresh air circulating increased. Hence the temperature gradient across the radial direction decreased significantly. Maximum temperature at the center of the combustor increased from 1633 to 1741 K as heat intensity increased from 5.37 to 21.1 MW/m$^3$. The temperature fluctuations around the mean value were in the range of 1.3-1.8% for all cases (variation bands shown in Fig. 6). A low temperature gradient and smaller fluctuations are representative characteristics of flameless combustion. For all thermal input conditions, the maximum temperature is below 1800 K. Therefore, NO$_x$ emissions were expected to be relatively very low. The predicted temperatures in the central zone are slightly lower than the measured temperatures for all thermal inputs. For the outer region (next to the central zone), the predicted temperatures are slightly higher than measured temperatures. Uniformly distributed temperature with low temperature gradients is observed in computational studies.

4.3 Pollutant emissions

The CO, NO$_x$ and HC emissions were measured for the range of operating conditions and emission levels were corrected to 15% O$_2$ level and shown in Fig. 7. CO emissions increased with a decrease in $\Phi$ from 1 to 0.6 and increase in heat intensity. However, the specific
emissions index (ppm/kW) decreased with increasing heat intensity. For \( R_C = 20 \text{ mm} \) and \( \dot{Q}'' = 5.37, 21.1 \text{ MW/m}^3 \), CO emissions varied from 11 to 21 ppm and 25 to 41 ppm respectively, as \( \Phi \) varied from 1 to 0.6. The specific CO emissions for these cases varied from 0.51 to 0.977 ppm/kW and 0.3 to 0.48 ppm/kW respectively. The emission release rate decreased with increasing heat intensity, indicating a positive outcome for higher heat density combustion systems. NO\(_x\) emissions decreased with decreasing \( \Phi \), as expected. For lean mixtures, the average measured temperature in the combustor decreased with a decrease in \( \Phi \). This led to a reduction in the NO\(_x\) emissions, however, CO emissions increase slightly. For the case of \( R_C = 20 \text{ mm} \) and \( \dot{Q}'' = 5.37, 21.1 \text{ MW/m}^3 \), NO\(_x\) varied from 9 to 6 ppm and 19 to 12 ppm respectively, for \( \Phi \) varied from 1 to 0.6. The specific NO\(_x\) emissions for these cases varied from 0.42 to 0.28 ppm/kW and 0.22 to 0.14 ppm/kW respectively.

HC emissions increased with decreasing \( \Phi \) from 1 to 0.6 and the specific emissions decreased with increasing heat intensity. For the case of \( R_C = 20 \text{ mm} \) and \( \dot{Q}'' = 5.37, 21.1 \text{ MW/m}^3 \), HC emissions varied from 0 to 3 ppm and 3 to 9 ppm respectively, for \( \Phi = 1 \) to 0.6. The specific HC emissions for these cases varied from 0 to 0.14 ppm/kW and 0.03 to 0.1 ppm/kW respectively. The overall variation of CO, NO\(_x\) and HC emissions for all heat intensities (\( \Phi = 1 \) to 0.6) were measured to be 11-41, 6-19 and 0-9 ppm respectively. These emissions are well within the range of emissions from flameless combustion with gaseous fuels reported in the literature.

A combustor with a chamfer radius of \( R_C = 25 \text{ mm} \) is tested for all thermal inputs (21.5-84.7 kW) conditions. Flameless combustion mode is observed for all cases without any issues related to combustion stability. Minimum recirculation required for each case of thermal input is determined experimentally and computationally by varying from \( R_C = 10 - 30 \text{ mm} \).
4.4 Acoustic emissions

Figure 8 shows the variation of acoustic emissions of the combustor in various combustion modes. Base level acoustic emissions of 84 dB were measured initially for cold flow conditions. After ignition, initially the combustor operated in the conventional mode with exit diameter of 90 mm and the level of acoustic emissions increased to an average value of 102 dB. After 3 min of conventional combustion, the chamfered portion was mounted and the exit diameter was reduced to \( D \) mm (Table 2). Immediately after reducing the diameter, the sound level increased. After a time of 2-3 min, the swirl flow was well stabilized in the combustor and flameless combustion was observed. The sound level reduced dramatically to a level well below the conventional combustion mode. For the case of 21.1 MW/m\(^3\), 113.5 and 93.6 dB of sound level was observed in the transition and flameless modes respectively. It was observed that with increased heat intensity, the sound level increased during the operation of the combustor in transition mode. However, for all heat intensities, almost a same sound level of approximately 94 dB was observed during the flameless combustion mode. The overall net sound level reduction from conventional to flameless mode for all combustors was in the range of 8-9 dB. A similar reduction has been reported in the literature [7, 14].

5 Conclusions:

In the present work, a new combustor configuration was designed and scaled-up to achieve flameless combustion with liquid fuels at high heat intensities for various industrial and gas turbine applications. Observations are summarized below.

1. Flameless combustion was stabilized in the base combustor with 21.5 kW thermal input (5.37 MW/m\(^3\)) and maximum \( R_{dll} \) of 3.2 with very low emissions. However, flameless
combustion was not achieved and unburned fuel accumulated in the combustor for higher fuel flow rates.

2. A chamfer added near the exit in the modified combustor configuration helped increase the $R_{dil}$ and residence time, permitting flameless combustion at higher intensities. The curved profile of the combustor dome and chamfer combined to form a curved vane which helps increase the degree of flow reversal. A computational investigation with experimental evidence suggests that a chamfer radius of 20, 25 and 30 mm was sufficient to achieve flameless combustion for $\dot{Q}'' = 10.2, 16.3$ and $21.1$ MW/m$^3$, respectively.

3. The peak temperature increases in the combustor and the temperature gradients decreases with an increase in the heat intensities. The temperature fluctuations were very small (1.3-1.8% of the mean value) for all cases.

4. The overall variation of CO, NO$_x$ and HC emissions for all heat intensities ($\Phi = 1$ to 0.6) were 11-41, 6-19 and 0-9 ppm respectively. These emissions are well within the range of emissions from flameless combustion with gaseous fuels operating at high intensity in the literature. Specific emissions (ppm/kW) decrease with an increase in heat intensity.

5. The outstanding performance of the burner with very low chemical and acoustic emissions at high heat release rates indicate the potential for use in various industrial and gas turbine applications.

**Acknowledgements:** Authors acknowledge the support received from ‘Aeronautics Research and Development Board’ (ARDB), Bangalore, India through Grant-in-Aid scheme.
References


Table 1 Variation of heat intensities reported in literature (SJ: Straight Jet, Forward Flow, FF (i.e. reactants enters from one side and products leave from opposite side), Reverse Flow, RF (i.e. reactants and products from same side of the combustor), $Q_{th}$: Thermal input (kW) and $\dot{Q}'''$: Heat intensity (MW/m$^3$), S: Solid, L: Liquid, G: Gas

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Table 2 Dimensional details of the combustor

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Figure 2 Variation of $R_{dit}$ with $R_C$ (a) 5.37 MW/m$^3$ (b) 10.2 MW/m$^3$ (c) 16.3 MW/m$^3$ (d) 21.1 MW/m$^3$ (e) Minimum and maximum $R_{dit}$ for all cases and zone length of $R_{dit}>2.72$ (in parenthesis)
Figure 3 Residence time distribution (E(t)) for three cases based on \( \tau_{avg} \), \( \tau_{s(Rc=0mm)} \) and \( \tau_{s(Rc=25mm)} \).
Figure 4 Schematic diagram of experimental setup
Figure 5 Distribution of DND for nozzles of different fuel flow rates
Figure 6 Temperature distribution comparison of experimental and computational measurements

\( \begin{align*}
5.37 \text{ MW/m}^3 \text{ RC}=0 & \quad \bullet \circ \bullet \quad 5.37 \text{ MW/m}^3 \text{ RC}=20 & \quad \bullet \diamond \bullet \quad 10.2 \text{ MW/m}^3 \text{ RC}=25 & \quad \bullet \Delta \bullet \\
5.37 \text{ MW/m}^3 \text{ RC}=25 & \quad \circ \circ \circ \quad 21.1 \text{ MW/m}^3 \text{ RC}=30 & \quad \bullet \quad 5.37 \text{ MW/m}^3 \text{ RC}=20 \text{ Comp} & \quad \bullet \\
5.37 \text{ MW/m}^3 \text{ RC}=25 \text{ Comp} & \quad \circ \quad 16.3 \text{ MW/m}^3 \text{ RC}=25 \text{ Comp} & \quad \bullet \quad 21.1 \text{ MW/m}^3 \text{ RC}=30 \text{ Comp}
\end{align*} \)
Figure 7 Variation of emissions with equivalence ratio for different heat intensities
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2. Dimensional details (in mm) of the air inlet (d), exit port (D) and chamfer radius (RC)

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3. Residence time distribution (E(t)) for three cases based on \( \tau_{avg} \), \( \tau_{s(RC=0mm)} \) and \( \tau_{s(RC=25mm)} \)

4. Schematic diagram of experimental setup

5. Distribution of DND for nozzles of different fuel flow rates

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7. Variation of emissions with equivalence ratio for different heat intensities

8. Variation of acoustic emissions for all heat intensities
EXPERIMENTAL AND NUMERICAL ANALYSIS FOR HIGH INTENSITY SWIRL BASED ULTRA-LOW EMISSION FLAMELESS COMBUSTOR OPERATING WITH LIQUID FUELS

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Colloquium Topic: New Technology Concepts
Short running title: SCALING OF LIQUID FUEL BASED FLAMELESS COMBUSTOR

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2
Experimental and numerical analysis for high intensity swirl based ultra-low emission flameless combustor operating with liquid fuels

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Abstract:

Flameless combustion offers many advantages over conventional combustion, particularly uniform temperature distribution and lower emissions. In this paper, a new strategy is proposed and adopted to scale up a burner operating in flameless combustion mode from a heat release density of 5.4 to 21 MW/m\textsuperscript{3} (thermal input 21.5 – 84.7 kW) with kerosene fuel. A swirl flow based configuration was adopted for air injection and pressure swirl type nozzle with an SMD 35-37 µm was used to inject the fuel. Initially, flameless combustion was stabilized for a thermal input of 21.5 kW ($\dot{Q}_{\text{in}}$=5.37 MW/m\textsuperscript{3}). Attempts were made to scale this combustor to higher intensities \textit{i.e.} 10.2, 16.3 and 21.1 MW/m\textsuperscript{3}. However, an increase in fuel flow rate led to incomplete combustion and accumulation of unburned fuel in the combustor. Two major difficulties were identified as possible reasons for unsustainable flameless combustion at the higher intensities (i) A constant spray cone angle and SMD increases the droplet number density (ii) Reactants dilution ratio ($R_{\text{dil}}$) decreased with increased thermal input. To solve these issues,
a modified combustor configuration, aided by numerical computations was adopted, providing a chamfer near the outlet to increase the $R_{dit}$. Detailed experimental investigations showed that flameless combustion mode was achieved at high intensities with an evenly distributed reaction zone and temperature in the combustor at all heat intensities. The emissions of CO, NO$_x$ and HC for all heat intensities ($\Phi=1 - 0.6$) varied between 11 - 41, 6 - 19 and 0 - 9 ppm, respectively. These emissions are well within the range of emissions from other flameless combustion systems reported in the literature. The acoustic emission levels were also observed to be reduced by 8-9 dB at all conditions.

**Keywords:** Flameless combustion; Swirl flow combustion; Liquid fuel; High intensity; Burner scaling; Ultralow emissions; Residence time.

1. Introduction:

Flameless/Mild combustion has gained significant importance due to its ability to suppress thermal NO formation and improve thermal efficiency of combustion systems. Flameless combustion has been primarily identified with gaseous fuels and extensive work has been reported [1-10]. Scaling the flameless combustors to higher intensities has been proposed in recent studies reported in the literature [7, 8, 11]. A brief summary of various high intensity flameless combustion systems with gaseous fuels is listed in Table 1. Lückerath et al., [11] have developed a Forward Flow (FF) combustor configuration with a thermal input of 475 kW and heat intensity of 240 MW/m$^3$ (at 20 bar). Kumar *et al.*, [7] have scaled up a high-intensity combustor (5-150 kW thermal input) with new scaling methodology and compared various existing scaling techniques *i.e.* Constant Velocity (CV), Constant Residence Time (CRT) and Cole’s approach with the proposed technique. The comparison of Weber [12] shows that CRT approach is relatively better for scaling swirl type combustor configurations. They have hinted at
the need of maintaining high reactant dilution rates to ensure that flameless combustion mode is achieved in scaled combustors. These types of combustor configurations with high heat intensity are expected to be useful in gas-turbine applications. Arghode and Gupta [8] have demonstrated a laboratory scale combustor achieving colorless distributed combustion with a high intensity of 453 MW/m³ ($Q_{th} = 6.25$ kW) with a combustor volume of ~13 cm³ and Reverse Flow (RF) configuration. Scaling of these concepts with low thermal input and high heat intensity render the systems very complex and making their implementation highly challenging. Further, very little literature is available in the field of scaling of flameless combustors with liquid fuels. Some basic studies on flameless/mild combustion with liquid fuels [3, 5, 13-15] have been reported recently. Traditional industrial burners and stationary gas-turbine combustors operate with liquid fuels at higher thermal inputs (~1 MW) and higher heat intensities (100 MW/m³). Therefore, additional studies are required to investigate the issues related to the scaling of high intensity flameless combustors with liquid fuels and their relation with spray characteristics.

In this study, a swirl based combustor operating in flameless combustion mode with kerosene at 21.5 kW (base case, $Q'' = 5.37$ MW/m³) [16], is developed and scaled up to operate at 85 kW (21.1 MW/m³). Attempts were made to achieve flameless combustion with higher intensity of 10.2, 16.3 and 21.1 MW/m³ using the base case combustor configuration with increased thermal input of 40.8, 65.1 and 84.7 kW respectively. However, the existing combustor configuration was unable to achieve stable flameless combustion. Computational and experimental studies were carried out to identify the causes preventing successful scale-up of the combustor. The combustor configuration was modified by providing a chamfer, thus increasing the degree of recirculation in the combustor, allowing stable flameless combustion. Computational studies show that with increased chamfer radius ($R_c$), recirculation of the combustion products and fuel
residence time increased. Three different $R_c$ values were considered, for the 10.2, 16.3 and 21.1 MW/m$^3$ cases respectively, and shown to achieve combustion with low emissions. The influence of spray characteristics on scaling the combustor was studied and the results are presented in this paper.

2. Computational Studies

2.1 Geometry design methodology

The base combustor was designed to stabilize high intensity flameless combustion using conventional liquid fuels. Stabilization of flameless combustion with liquid fuels depends on three important parameters,

1. Sauter Mean Diameter (SMD) of the spray. The evaporation rate is a function of boiling point and surface area to volume ratio ($A_S/V$) of the droplet. The evaporation time increases with increasing boiling temperature and SMD.

2. A group of parameters including droplet distribution, evaporation, mixture formation and subsequent combustion with preheating and dilution of reactants

3. In flameless combustion mode, the increased dilution of fresh reactants with hot combustion products results in reduced reaction rate. Due to this, reaction zone is uniformly distributed throughout the combustor volume with lower peak flame temperature than that of conventional mode [4]. In conventional mode, the fuel spray directly enters the combustion zone having higher peak temperature. Therefore, the droplet evaporation rate is relatively slower in flameless combustion mode [4]. To achieve complete evaporation and combustion, the droplet residence time should be higher in flameless combustion mode.
To sustain flameless combustion with liquid fuels, the above three issues can be addressed by increasing the residence times and recirculation as compared to flameless combustion with gaseous fuel. A swirl flow creates a central vortex zone and low pressure gradient, supporting a large reverse flow region in the combustor. High swirl creates higher centrifugal force that enhances the residence time of the hot gases trapped within the swirling flow [13-20]. The increased residence time enhances the flame stability limits and rate of mixing of products and reactants. The high recirculation allows for good mixing, essential for obtaining a distributed reaction zone over a large volume of the combustor [13-20]. Therefore, a tangential air injection scheme was used in this study to generate the swirl flow in the combustor.

In this study, a conical combustor with 60° diverging angle was considered with a total volume of ~0.004 m³ [16, 21]. A pressure swirl fuel injector was used for injection of kerosene. The combustor configuration is shown in Fig. 1. Computational and experimental studies were carried out simultaneously. Recirculation of combustion products was identified as the key factor to sustain flameless combustion. Hence, the reactants dilution ratio (\(R_{dil}\)) is the governing metric. \(R_{dil}\) is calculated as follows [14, 16].

\[
R_{dil} = \frac{\dot{m}_{axial} - (\dot{m}_{ox} + \dot{m}_{f})}{(\dot{m}_{ox} + \dot{m}_{f})}
\]

\[
\dot{m}_{axial} = \iiint \rho v_{axial} dydz
\]

### 2.1.1 Challenges in scaling

Initially, the combustor was tested at 21.5 kW thermal input using the unmodified combustor configuration (without chamfer, i.e. \(R_c\)=0 mm) and exit diameter (D) of 25 mm. Well stabilized
flameless combustion was observed experimentally [16, 21]. Computational results showed that $R_{dlit}$ varied spatially from 1.1 to 3.2. The same combustor was tested at higher thermal inputs of 40.8, 65.1 and 84.7 kW (respective heat intensities 10.2, 16.3 and 21.1 MW/m$^3$) and experimental observations revealed that, flameless combustion was not stabilized in the combustor at these higher inputs and large quantities of unburned fuel accumulated in the combustor. The fuel spray cone angle was maintained constant at 45° for all nozzles and SMD of all nozzles were in the range of 35-37 µm (details in Section 4.1). Therefore, with the increased fuel mass flow rate, droplet number density (DND) also increased. Hence, more recirculation (increased residence time) would be required to increase the entrainment and to achieve complete evaporation. The computational results also revealed that, $R_{dlit}$ decreased with increasing thermal input. Computational and experimental evidence suggested that $R_{dlit}$ needed to be sufficiently high for all thermal inputs to provide the required entrainment and residence time.

CRT approach appears suitable for scaling swirl combustors operating with gaseous fuels [12]. However in case of liquid fuels, the DND increases with thermal input. The residence time should be increased for complete evaporation and combustion. CV scaling approach for higher thermal inputs results in increased combustor volume and reduced heat intensity [7, 12]. Hence, for the present case, both CV and CRT approaches are not suitable. Similarity of certain dimensionless quantities in scaling is different for various combustor configurations, operating conditions and modes of combustion [22]. Therefore, a combination of experimental and numerical simulations aimed at improving the droplet residence times and recirculation rates were considered. To enhance both droplet residence time and recirculation rate, a chamfer at the top of the combustor is provided as shown in Fig 1. A computational analysis (described below)
was carried out for high thermal inputs, by varying chamfer radius \( R_C \) to determine the \( R_{dit} \) for each case and the operating conditions that yielded an \( R_{dit} > 2.5 \). The combustor geometry for different thermal intensities is non-dimensionalized with \( D \), as shown in Fig. 1 and listed in Table 2.

### 2.1.2 Numerical method

A general purpose CFD code Fluent-14.5 was used for computational studies in this work. A 3-D double-precision pressure-based solver was used. For all thermal inputs, tangential air inlet and combustor exit velocities were maintained constant to ensure similar level of pressure drop across the combustor. Therefore, the air inlet diameter \( (d_{in}) \) and exit diameter \( (D) \) are increased with increased thermal input. Chamfer radius is varied from 10 to 30 mm at 5 mm increments.

Three-dimensional Navier-Stokes equations were discretized and solved in a finite-volume domain. Reynolds Stress Model (RSM) was used for turbulence modeling. The energy equation was solved considering 20 intermediate species equilibrium chemistry and a non-premixed droplet combustion model for simulating the combustion of the liquid fuels. Compressible flow was considered and the viscosity was calculated using Sutherland’s law. Specific heats were defined as a function of the temperature (piecewise-polynomial). A P1 radiation model was used. Constant mass-flow inlet condition normal to the boundary surface was applied at air inlets, and a pressure outlet based boundary condition was applied at the exit. No-slip wall and constant temperature boundary conditions were applied at the walls. Non-premixed droplet evaporation and combustion, following the spherical law was considered with PDF droplet evaporation. A single component surrogate, \( C_{12}H_{23} \) was used to simulate kerosene with a density of 780 kg/m³.
Fuel injection was simulated as a solid cone type spray with a droplet diameter of 36 µm and a cone angle of 45°. The amount of heat removal from the combustor walls is 3.2, 8.3, and 12.9 kW respectively, for three higher heat intensities of 10.2, 16.3 and 21.1 MW/m³. The heat removal through wall cooling is considered by applying heat-loss through combustor walls as heat flux boundary condition for higher heat intensity cases. The solution is considered to be converged when RMS residuals of the system were less than 1×10⁻⁶. A number of computations were carried out using hexa mesh with different mesh sizes varying from 1.1-2.5 mm. The number of cells for computations was varied from 2 to 4.5 million elements. A mesh size of 1.2 mm was considered sufficient to obtain grid-independent results with approximately 3.6 million grid points. The grid convergence was calculated based on the Grid Convergence Index (GCI) criteria. If the GCI for two successive grid sizes was below 3%, it was considered that grid convergence has been achieved [15].

2.2 Reactants dilution ratio \( (R_{dil}) \)

\( R_{dil} \) was calculated at different axial planes of the combustor. For the case of \( Q_{th} = 21.5 \) kW (\( R_C = 0 \) mm) with exit port diameter of 25 mm, a maximum \( R_{dil} \) of 3.2 was achieved. Complete flameless combustion with low emissions was observed experimentally. \( R_{dil} \) was calculated for higher thermal inputs (\( Q_{th} = 40.8, 65.1 \) and 84.7 kW) with different \( R_C \) of 10, 15, 20, 25 and 30 mm and results are shown in Fig. 2. It was observed that, for constant thermal input and increasing \( R_C \), the degree of flow reversal increased in the combustor. The resulting \( R_{dil} \) increased with \( R_C \). For instance, at \( Q_{th} = 21.5 \) kW, a maximum \( R_{dil} \) of 5.22, 5.77, 6.26 and 6.75 was obtained for \( R_C = 10, 15, 20 \) and 25 mm respectively (Fig. 2a). The curved profile of the combustor dome and chamfer near the exit combined to form curved vanes promoted a large degree of flow reversal. Hence, \( R_{dil} \) increased with increased \( R_C \). For a constant \( R_C \) and
increasing thermal input, \( R_{dil} \), was calculated as shown in Fig 2a-d. For example, at \( R_c=25 \) mm, the maximum \( R_{dil} \) calculated were 6.77, 3.75, 3.51 and 2.71 respectively, for 21.5, 40.8, 65.1 and 84.7 kW. Therefore, it was observed that with increasing thermal input, the chamfer radius must be increased appropriately to maintain a constant \( R_{dil} \) for all thermal inputs. The zone length of \( R_{dil} > 2.71 \), which is the lower limit for achieving flameless combustion is calculated for all computational conditions and shown in Fig. 2e. It was observed experimentally that an \( R_c=20, 25 \) and 30 mm were sufficient to achieve flameless combustion at higher heat intensities (10.2, 16.3 and 21.1 MW/m\(^3\) respectively).

2.3 Residence Time Distribution

The residence time of the reactants in the combustion chamber is a significant parameter to achieve flameless combustion [23]. Three basic time parameters were considered to calculate the residence time of reactants.

1. Average residence time; \( \tau_{avg} = \left( \frac{V}{\dot{V}} \right) \); \( V= \) combustor volume and \( \dot{V}= \) volume flow rate of reactants. However, since the present combustor operates with a swirl flow, the residence time was calculated computationally for different cases by injecting particles from air/fuel inlets in the combustor.

2. Swirl based residence time with \( R_c=0 \) mm; \( \tau_{s(Rc=0mm)} \).

3. Swirl based residence time with \( R_c=25 \) mm; \( \tau_{s(Rc=25mm)} \).

The calculated \( \tau_{avg} \) decreased from 0.61 to 0.15 s as the thermal input increased from 5.37 to 21.1 MW/m\(^3\). The calculated \( \tau_{s(Rc=0mm)} \) with swirl flow, decreased from 0.76 to 0.29 s and \( \tau_{s(Rc=25mm)} \) decreased from 0.98 to 0.69 s for this same range of thermal inputs. For the case of 21.1 MW/m\(^3\), the percentage increase in residence time is 93 and 360 % for \( \tau_{s(Rc=0mm)} \) and
respectively as compared with $\tau_{\text{avg}}$. It was observed from the computational study that the residence time increased with both swirl flow pattern and increased chamfer radius ($R_C$). Residence time distribution, $E(t)$ [23] was calculated for all cases by considering the combustor as a well-stirred reactor and shown in Fig. 3. The $E(t)$ of the reactor is the probability density function of a particle in the reactor. If $E(t)$ of a reactor is high, the residence time of the particle is large. It is observed from Fig. 3 that $E(t)$ increases with swirl flow, and increases further with chamfer plus swirl flow.

3 Details of experimental methodology

3.1 Experimental setup

Figure 4 shows a schematic diagram of the experimental setup. The combustor was placed vertically on a test stand. Kerosene was stored at a pressure of 9 bar ($\Delta P$) in a pressurized stainless-steel tank. The fuel injector was located at the center of the combustor. The fuel injector imparts a clockwise rotation to fuel spray; hence a counter-clockwise air injection was selected to impart more shear force to the flow resulting in enhanced mixing and evaporation of droplets. Air supply to the combustor was regulated through electric mass flow controllers (accuracy $\pm 1.5\%$ of full scale).

3.2 Experimental procedure and instruments

Initially, the premixed LPG-air mixture was ignited with a spark and combustor was run for 2-3 min to preheat the combustor. The kerosene fuel is injected at 5 bar pressure by opening the ball-valve in the fuel line. The LPG flow rate was then gradually reduced and the kerosene injection pressure was simultaneously raised to 9 bar. A stable flame was established in conventional combustion mode with stoichiometric kerosene-air mixture for next 4-5 min. After an initial
start-up time of 7-8 min, the combustor wall temperature reached ~ 900 K. A chamfered flange was placed at the top to effectively reduce the exhaust port diameter from 90 mm to a diameter (D) for the particular heat intensity (Table 2). The conventional flame then gradually shifted to a flameless combustion mode. This strategy was adapted to understand and evaluate the effect of exit port diameter variation on transition between conventional (90 mm) and flameless combustion mode (30 mm). The present combustor can be started with the top components in place for a real practical application.

Exhaust gas composition was measured with a gas analyzer which included O\textsubscript{2} analyzer (0-25\% range, 0.1\% accuracy), CO analyzer (0-10000 ppm, ±5 ppm accuracy), NO analyzer (0-5000 ppm, ±1 ppm accuracy), C\textsubscript{x}H\textsubscript{y} analyzer (0-50,000 ppm), and CO\textsubscript{2} analyzer. Temperature measurements were carried out with R-type (\(d_{\text{junction}}=1\) mm) thermocouples. The sound level at the exit (100 mm away from axis) of the combustor was measured for different combustion modes with a fast response (Resolution=0.1 dB, \(\tau_{\text{response}}=200\) ms) sound level instrument.

4 Results and discussion

4.1 Spray characteristics

In the present study, four nozzles N1 - N4 with mass flow rates of 1.72, 3.27, 5.21 and 6.78 kg/h respectively, were used to provide 21.5, 40.8, 65.1 and 84.7 kW thermal inputs respectively. An injection pressure of 9 bar was maintained for all experiments. Various details of the spray characteristics such as \(D_{10}\), \(D_{32}\) (SMD), \(D_{V10}\), \(D_{V50}\) and \(D_{V90}\), droplet distribution, droplet number density (DND) were measured with a particle shadowgraphy technique. 7000-9000 droplets were considered in each sample size. A count of 150 pictures was selected for each sample at an axial position of 45 mm from the nozzle tip.
It was observed that for all four nozzles, SMD was in the range of 35-37 μm and variation in other diameters was relatively very small. Since the spray cone angle and droplet diameters were nearly the same for all four nozzles, the DND increased for higher mass flow nozzles, the measured DND for N1-N4 nozzles was $32 \times 10^3$, $64 \times 10^3$, $110 \times 10^3$ and $167 \times 10^3$ n/cm$^3$ respectively. Therefore, entrainment of hot gases needed to be increased significantly with the increasing DND to achieve complete evaporation of all droplets. The DND distribution for all four nozzles is shown in Fig. 5.

4.2 Temperature distribution

Temperature variation in the radial direction of the combustor at an axial location of 120 mm was measured for different heat intensities at $\Phi=0.92$ and comparison with predicted results is shown in Fig. 6. Due to larger thermocouple response time (~0.25 s) as compared to integral turbulence time-scales (~3 ms), it is difficult to measure actual temperature variation in the combustor. However, temperature variation with time is measured at a given location and the mean was calculated from recorded temperatures over a period of 10 – 20 seconds. The measured temperature was corrected by considering convection and radiation losses from the thermocouple junction. For the case of 5.37 MW/m$^3$, the wall temperature of the combustor was ~800 K. When the combustor was operated at 10.2 MW/m$^3$, the walls became red hot. Hence, cooling of outer walls of the combustor was mandatory for higher heat densities, achieved through water circulation through copper tubes brazed on the outer walls of the combustor. A constant wall temperature of ~950 K was maintained for higher heat intensities (10.2-21.1 MW/m$^3$). The heat removal through wall cooling is 3.2, 8.3, and 12.9 kW respectively for three
higher heat intensities of 10.2, 16.3 and 21.1 MW/m$^3$. Fresh air at ambient temperature entered the combustor and circulated on the inner walls; a sharp rise in temperature of the air was observed near the walls of the combustor (Fig. 6). Temperature at all radial locations increased with increasing heat intensity of the combustor. As expected, the temperature increased from the walls to the center line of the combustor. The temperature difference across the plane, from axis to near wall (0.0975 m) for 5.37 MW/m$^3$ with $R_c=0$ mm was 443 K. The temperature difference for higher heat intensities (10.2-21.1 MW/m$^3$) was 319, 293 and 245 K respectively. With increased heat intensity, the overall temperature of the combustor and the temperature of the fresh air circulating increased. Hence the temperature gradient across the radial direction decreased significantly. Maximum temperature at the center of the combustor increased from 1633 to 1741 K as heat intensity increased from 5.37 to 21.1 MW/m$^3$. The temperature fluctuations around the mean value were in the range of 1.3-1.8% for all cases (variation bands shown in Fig. 6). A low temperature gradient and smaller fluctuations are representative characteristics of flameless combustion. For all thermal input conditions, the maximum temperature is below 1800 K. Therefore, NO$_x$ emissions were expected to be relatively very low. The predicted temperatures in the central zone are slightly lower than the measured temperatures for all thermal inputs. For the outer region (next to the central zone), the predicted temperatures are slightly higher than measured temperatures. Uniformly distributed temperature with low temperature gradients is observed in computational studies.

4.3 Pollutant emissions

The CO, NO$_x$ and HC emissions were measured for the range of operating conditions and emission levels were corrected to 15% O$_2$ level and shown in Fig. 7. CO emissions increased with a decrease in $\Phi$ from 1 to 0.6 and increase in heat intensity. However, the specific
emissions index (ppm/kW) decreased with increasing heat intensity. For $R_C=20$ mm and $\hat{Q}'' = 5.37$, 21.1 MW/m$^3$, CO emissions varied from 11 to 21 ppm and 25 to 41 ppm respectively, as $\Phi$ varied from 1 to 0.6. The specific CO emissions for these cases varied from 0.51 to 0.977 ppm/kW and 0.3 to 0.48 ppm/kW respectively. The emission release rate decreased with increasing heat intensity, indicating a positive outcome for higher heat density combustion systems. NO$_x$ emissions decreased with decreasing $\Phi$, as expected. For lean mixtures, the average measured temperature in the combustor decreased with a decrease in $\Phi$. This led to a reduction in the NO$_x$ emissions, however, CO emissions increase slightly. For the case of $R_C=20$ mm and $\hat{Q}''' = 5.37$, 21.1 MW/m$^3$, NO$_x$ varied from 9 to 6 ppm and 19 to 12 ppm respectively, for $\Phi$ varied from 1 to 0.6. The specific NO$_x$ emissions for these cases varied from 0.42 to 0.28 ppm/kW and 0.22 to 0.14 ppm/kW respectively.

HC emissions increased with decreasing $\Phi$ from 1 to 0.6 and the specific emissions decreased with increasing heat intensity. For the case of $R_C=20$ mm and $\hat{Q}''' = 5.37$, 21.1 MW/m$^3$, HC emissions varied from 0 to 3 ppm and 3 to 9 ppm respectively, for $\Phi = 1$ to 0.6. The specific HC emissions for these cases varied from 0 to 0.14 ppm/kW and 0.03 to 0.1 ppm/kW respectively. The overall variation of CO, NO$_x$ and HC emissions for all heat intensities ($\Phi = 1$ to 0.6) were measured to be 11-41, 6-19 and 0-9 ppm respectively. These emissions are well within the range of emissions from flameless combustion with gaseous fuels reported in the literature.

A combustor with a chamfer radius of $R_C = 25$ mm is tested for all thermal inputs (21.5-84.7 kW) conditions. Flameless combustion mode is observed for all cases without any issues related to combustion stability. Minimum recirculation required for each case of thermal input is determined experimentally and computationally by varying from $R_C = 10$ - 30 mm.
4.4 Acoustic emissions

Figure 8 shows the variation of acoustic emissions of the combustor in various combustion modes. Base level acoustic emissions of 84 dB were measured initially for cold flow conditions. After ignition, initially the combustor operated in the conventional mode with exit diameter of 90 mm and the level of acoustic emissions increased to an average value of 102 dB. After 3 min of conventional combustion, the chamfered portion was mounted and the exit diameter was reduced to $D$ mm (Table 2). Immediately after reducing the diameter, the sound level increased. After a time of 2-3 min, the swirl flow was well stabilized in the combustor and flameless combustion was observed. The sound level reduced dramatically to a level well below the conventional combustion mode. For the case of 21.1 MW/m$^3$, 113.5 and 93.6 dB of sound level was observed in the transition and flameless modes respectively. It was observed that with increased heat intensity, the sound level increased during the operation of the combustor in transition mode. However, for all heat intensities, almost a same sound level of approximately 94 dB was observed during the flameless combustion mode. The overall net sound level reduction from conventional to flameless mode for all combustors was in the range of 8-9 dB. A similar reduction has been reported in the literature [7, 14].

5 Conclusions:

In the present work, a new combustor configuration was designed and scaled-up to achieve flameless combustion with liquid fuels at high heat intensities for various industrial and gas turbine applications. Observations are summarized below.

1. Flameless combustion was stabilized in the base combustor with 21.5 kW thermal input (5.37 MW/m$^3$) and maximum $R_{dil}$ of 3.2 with very low emissions. However, flameless
combustion was not achieved and unburned fuel accumulated in the combustor for higher fuel flow rates.

2. A chamfer added near the exit in the modified combustor configuration helped increase the $R_{dil}$ and residence time, permitting flameless combustion at higher intensities. The curved profile of the combustor dome and chamfer combined to form a curved vane which helps increase the degree of flow reversal. A computational investigation with experimental evidence suggests that a chamfer radius of 20, 25 and 30 mm was sufficient to achieve flameless combustion for $\dot{Q}'' = 10.2, 16.3$ and 21.1 MW/m$^3$, respectively.

3. The peak temperature increases in the combustor and the temperature gradients decreases with an increase in the heat intensities. The temperature fluctuations were very small (1.3-1.8% of the mean value) for all cases.

4. The overall variation of CO, NO$_x$ and HC emissions for all heat intensities ($\Phi = 1$ to 0.6) were 11-41, 6-19 and 0-9 ppm respectively. These emissions are well within the range of emissions from flameless combustion with gaseous fuels operating at high intensity in the literature. Specific emissions (ppm/kW) decrease with an increase in heat intensity.

5. The outstanding performance of the burner with very low chemical and acoustic emissions at high heat release rates indicate the potential for use in various industrial and gas turbine applications.

Acknowledgements: Authors acknowledge the support received from ‘Aeronautics Research and Development Board’ (ARDB), Bangalore, India through Grant-in-Aid scheme.
References


Table 1 Variation of heat intensities reported in literature (SJ: Straight Jet, Forward Flow, FF (i.e. reactants enters from one side and products leave from opposite side), Reverse Flow, RF (i.e. reactants and products from same side of the combustor), $Q_{th}$: Thermal input (kW) and $\dot{Q}'''$: Heat intensity (MW/m$^3$), S: Solid, L: Liquid, G: Gas

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<th>Ref.</th>
<th>$Q_{th}$</th>
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<td>[9]</td>
<td>15</td>
<td>0.3</td>
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Table 2 Dimensional details of the combustor

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<th>D</th>
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<th>$d_2$</th>
<th>$l_1$</th>
<th>$l_2$</th>
<th>$R_c$</th>
<th>$d_{in}$</th>
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<td>25</td>
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<td>8.4</td>
<td>4.4</td>
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<td>0.2</td>
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<td>10.2</td>
<td>7.5</td>
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<td>37</td>
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<td>1.621</td>
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Figure 1 Dimensional details of the combustor
Figure 2 Variation of $R_{\text{dil}}$ with $R_C$ (a) 5.37 MW/m$^3$ (b) 10.2 MW/m$^3$ (c) 16.3 MW/m$^3$ (d) 21.1 MW/m$^3$ (e) Minimum and maximum $R_{\text{dil}}$ for all cases and zone length of $R_{\text{dil}}>2.72$ (in parenthesis)
Figure 3 Residence time distribution (E(t)) for three cases based on $\tau_{avg}$, $\tau_{s(Rc=0mm)}$ and $\tau_{s(Rc=25mm)}$. 
Figure 4 Schematic diagram of experimental setup
Figure 5 Distribution of DND for nozzles of different fuel flow rates
Figure 6 Temperature distribution comparison of experimental and computational measurements

(- ■ - 5.37 MW/m³_R_C=0  ••• 5.37 MW/m³_R_C=20  ••• 10.2 MW/m³_R_C=25  ▲ 16.3 MW/m³_R_C=25  ••• 21.1 MW/m³_R_C=30)

实验室测量：
- 5.37 MW/m³_R_C=0
- 5.37 MW/m³_R_C=20
- 10.2 MW/m³_R_C=25
- 16.3 MW/m³_R_C=25
- 21.1 MW/m³_R_C=30

计算结果：
- 5.37 MW/m³_R_C=0
- 5.37 MW/m³_R_C=20
- 10.2 MW/m³_R_C=25
- 16.3 MW/m³_R_C=25
- 21.1 MW/m³_R_C=30
Figure 7 Variation of emissions with equivalence ratio for different heat intensities
Figure 8 Variation of acoustic emissions for all heat intensities
List of Tables

1. Variation of heat intensities reported in literature (SJ: Straight Jet, Forward Flow, FF (i.e. reactants enters from one side and products leave from opposite side), Reverse Flow, RF (i.e. reactants and products from same side of the combustor), $Q_{th}$: Thermal input (kW) and $\dot{Q}''':$ Heat intensity (MW/m$^3$), S: Solid, L: Liquid, G: Gas

2. Dimensional details (in mm) of the air inlet ($d$), exit port (D) and chamfer radius ($R_C$)

List of Figure Captions

1. Dimensional details of the combustor

2. Variation of $R_{dil}$ with $R_C$ (a) 5.37 MW/m$^3$ (b) 10.2 MW/m$^3$ (c) 16.3 MW/m$^3$ (d) 21.1 MW/m$^3$ (e) Minimum and maximum $R_{dil}$ for all cases and zone length of $R_{dil} > 2.72$ (in parenthesis)

3. Residence time distribution (E(t)) for three cases based on $\tau_{avg}$, $\tau_s(R_C=0\text{mm})$ and $\tau_s(R_C=25\text{mm})$

4. Schematic diagram of experimental setup

5. Distribution of DND for nozzles of different fuel flow rates

6. Temperature distributions along the radial coordinate for different heat intensities and comparison of experimental and computational measurements ($\cdot$- 5.37 MW/m$^3$ with $R_C=0$ mm $\cdot\square\cdot$ 5.37 MW/m$^3$ with $R_C=20$ mm $\cdot\diamond\cdot$ 10.2 MW/m$^3$ with $R_C=25$ mm $\cdot\Delta\cdot$ 16.3 MW/m$^3$ with $R_C=25$ mm $\cdot\bigcirc\cdot$ 21.1 MW/m$^3$ with $R_C=30$ mm $\bigtriangleup$ 5.37 MW/m$^3$ with $R_C=20$ mm Comp $\rightarrow$ 10.2 MW/m$^3$ with $R_C=25$ mm Comp $\blacktriangle$ 16.3 MW/m$^3$ with $R_C=25$ mm Comp $\blacklozenge$ 21.1 MW/m$^3$ with $R_C=30$ mm Comp.

7. Variation of emissions with equivalence ratio for different heat intensities

8. Variation of acoustic emissions for all heat intensities
Rebuttal

Reviewer #1: Very Good

The English in this paper needs to be improved? (1 = Yes; 2 = No; 3 = See comment below) [1-3] 2

This paper requires review by a native English speaker or a translation service? (1 = Yes; 2 = No; 3 = See comment below) [1-3] 2

The manuscript is concerned with scaling of flameless/mild combustion of liquid fuels. Indeed, each application of mild combustion requires careful considerations on firing density. Generally, the lower the firing density, the lower are the NOX and soot/particulates emissions. Attempts to apply mild combustion to (high firing density) gas turbines have failed although in some publications some success has been claimed. The scaling, from low to high firing densities, is only poorly understood. Thus, the manuscript is welcome, indeed. I recommend its publications. Below provided comments may be used to improve the manuscript further.

Response: Authors are happy to note that reviewer understands and appreciates the present work. Authors are thankful to reviewer for recommending the acceptance of this manuscript.

Point by point response to reviewer’s comments is given below and the proposed changes have been made in the revised manuscript.

(a) Cole's scaling approach is not well known. I suggest you either explain or remove it. Perhaps the papers of Spalding (the ninth Comb. Symp), 1962, pp. 833 or Weber (the 26th Comb. Symp.), 1996, pp. 3343-3354 can be of assistance.

Response: As per the reviewer suggestion, scaling approaches from the papers of Spalding [22] and Weber [12] are explained in the revised manuscript. This information has been added in the revised manuscript on page 8, line 11-19.

(b) Table 1 is incomplete. For ref#3, the following numbers are applicable. Thermal input 580 kW - Furnace volume 2x2x6=24m3 so that firing density is 24 kW/m3 (for details see R. Weber et al. "Combustion of light and heavy fuel oils in high-temperature air" Journal of the Institute of Energy, June 2001, 74, pp. 38-47. Generally, check again the values in Table 1

Response: We appreciate the reviewer's suggestions. The information suggested by the reviewer has been appended to Table 1 on page 21.

(c) Abstract. …. To increase the …. (?)

Response: The abstract is rewritten to make this part more meaningful in the revised manuscript.
Reviewer #2: Good

The English in this paper needs to be improved? (1 = Yes; 2 = No; 3 = See comment below) [1-3] 1

This paper requires review by a native English speaker or a translation service? (1 = Yes; 2 = No; 3 = See comment below) [1-3] 2

PROCI-D-13-00649

Title: SCALING FOR HIGH INTENSITY SWIRL BASED ULTRA-LOW EMISSION FLAMELESS COMBUSTOR OPERATING WITH LIQUID FUELS

Authors: Reddy, Katoch, Roberts, Kumar

This manuscript combines experiments and numerical investigations aimed at increasing the power density of an existing enclosed flameless combustor. The over-arching motivation of the work is said to be the scaling of the combustor, though it actually seems to be related to increasing the power density. In either case, I fully support the motivation of the project. The paper certainly presents some interesting findings and the ability to operate at higher power density in a notable contribution to the emerging field of flameless combustion for gas turbine applications. However, the generalities of the work seem limited. How would the high-density combustor be scaled to a physically larger system? How would this be implemented in a practical system? What range of operating conditions and turn-down ratios are possible? Whilst these are rhetorical questions that do not need a response, as a reader I am left wanting at the end of the paper. This is a great project and a good start to a paper, but I think that more work would turn this from a good to an excellent manuscript of interest to a wider community. In its current form, I don't believe this paper to be worthy of presentation.

I strongly encourage the authors to continue this work, and have some feedback to help strengthen future submissions;

Response: Authors are happy to note that the reviewer understands and appreciates the present work and graded as ‘Good’. We gracefully accept the reviewer’s positive comments and criticism on present work. Reviewer’s constructive criticism is invaluable and will indeed help in improving the quality of this manuscript to make it a good contribution to the field.

Point by point response to reviewer’s comments is given below and proposed changes have been made in the revised manuscript.
1) Although only a minor point, the instructions clearly indicate that it is necessary to add a statement on the use of color figures in the printed version, yet such a statement is missing.

Response: Authors will opt for color printing in online version. This information has been added in the title page of the revised manuscript.

2) There are many minor grammatical errors throughout the manuscript that should have been identified through thorough proof-reading.

Response: The minor grammatical mistakes have been corrected in the revised manuscript with the help of a professional English language expert.

3) The introduction seems rather brief (perhaps excessively short), and tends to reiterate that the work is too focused on one particular burner rather than contributing more general knowledge to the field.

Response: Although authors partially agree with the reviewer on this issue that introduction is brief and concise, however, authors disagree that the focus is only on one burner. The introduction of the paper has been focused on different issues/aspects related to the scaling of the mild combustion burners and significant information on various issues related to mild combustors has been presented in a concise manner due to word limit for symposium paper. More information has been added in the introduction section on page 8, line 11-17.

4) Section 2.1, dot point 3: "…droplet evaporation is expected to be slower in this mode as compared to conventional combustion…". The justification for this statement seems to be that under flameless conditions the temperature peak is lower. Whilst true, the fuel stream is likely to encounter more hot products and spend more time in hot regions in flameless mode than in conventional combustion. I therefore question this statement.

Response: Authors agree with reviewer that peak temperature in flameless combustor is lower than conventional combustion mode. The reviewer has misunderstood the statement which points towards the slower droplet evaporation rate. The increased dilution of the mixture from hot combustion products results in reduced reaction rate. Therefore, the fuel droplets need to spend more time (droplet residence time) in flameless combustion mode as compared to conventional mode. The residence time of droplets is improved by adopting swirl flow configuration in the present work. Increased heat intensity in the same burner requires higher residence time for complete evaporation/ mixing/ combustion of fuel droplets. Hence, top lid chamfer radius increased with increased thermal intensity. This information has been added in the introduction section on page 6, line 15-21.

5) Section 2.1.1, first sentence: should be written as "… (without chamfer, i.e. Rc=0mm)…”
Response: As per the reviewer suggestion, it has been changed in the revised manuscript on page 7, line 17.

6) The introduction talks about scaling of the combustor, yet all the changes in geometry are quoted in millimeters. If the focus is indeed on scaling, then the geometry should be non-dimensionalized.

Response: In this present study, a basic combustor configuration developed for 20 kW input is scaled for higher heat intensities in flameless combustion mode. The volume (dimensions) of the chamber is kept unchanged, except the chamfer (top-lid) radius to maintain the recirculation rates in same range. Recirculation rate decreases with an increase in the thermal input at a constant $R_C$ as shown in Fig. 2. Therefore, the variation in the dimensions is compared with a reference dimension and maintained in the same units. This information has been added in the revised manuscript on page 24, Fig 1, and page 22 Table 2.

Perhaps, this parameter can be non-dimensionalized with exit port diameter $D$, shown in Figure and table below. This information has been updated in the revised manuscript.

<table>
<thead>
<tr>
<th>$Q_{th}$ (kW)</th>
<th>$\dot{Q}''$ (MW/m$^3$)</th>
<th>$d$ (mm)</th>
<th>$D$ (mm)</th>
<th>$d_1$</th>
<th>$d_2$</th>
<th>$l_1$</th>
<th>$l_2$</th>
<th>$R_C$</th>
<th>$d_{in}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>21.5</td>
<td>5.37</td>
<td>5</td>
<td>25</td>
<td>3.2</td>
<td>8.4</td>
<td>4.4</td>
<td>2.4</td>
<td>0.4</td>
<td>0.2</td>
</tr>
<tr>
<td>40.8</td>
<td>10.2</td>
<td>7.5</td>
<td>29</td>
<td>2.758</td>
<td>7.241</td>
<td>3.793</td>
<td>2.068</td>
<td>0.689</td>
<td>0.258</td>
</tr>
<tr>
<td>65.1</td>
<td>16.3</td>
<td>9</td>
<td>34</td>
<td>2.325</td>
<td>6.176</td>
<td>3.235</td>
<td>1.764</td>
<td>0.735</td>
<td>0.264</td>
</tr>
<tr>
<td>84.7</td>
<td>21.1</td>
<td>11</td>
<td>37</td>
<td>2.162</td>
<td>5.675</td>
<td>2.972</td>
<td>1.621</td>
<td>0.81</td>
<td>0.297</td>
</tr>
</tbody>
</table>
7) Section 3.2: The start-up process sounds unnecessarily complex: why can't it be started with the top components in place? How would this combustor be operated in a practical system?

Response: The present combustor can be started with the top components in place. However, the present strategy of different exit diameters during the starting process is adopted to understand and evaluate the effect of exit diameter variation on transition between conventional (90 mm) and flameless combustion mode (30 mm). This information has been added in the revised manuscript on page 12, line 17 to page 13, line 7.

8) Section 3.2: It is stated that temperature fluctuations were measured, yet the diameter of the thermocouple is 1mm. A thermocouple bead of this size would have a very slow thermal response. How does the response time of the thermocouple compare to the turbulent time scale in the combustor?

Response: The response time of the thermocouple (~0.25 s) is much larger than the integral turbulence time scales (~ 3 ms) due to larger bead size. In the present work, the variation of mean temperature in radial direction is reported. Since the temperature at a given location is varying with time, the mean is calculated from a set of recorded temperature values over 10 – 20 seconds and presented. This information has been appropriately modified to remove the ambiguity in the revised manuscript on page 14, line 11-17.

9) Section 4.1: It is noted that a range of details of the spray were measured, but only the droplet number density is presented (in Fig. 5). If the other measurements are not reported or mentioned, then it seems inappropriate to say what other characterization was done.

Response: Detailed spray diagnostics have been carried out; however it could not be included in the manuscript due word limits for paper. More details are shown in the figure and table below. Since the word limit, this information not added in the revised manuscript.
Figure: Spray characteristics of all four nozzles (N1 to N4)

Table 3: Spray characteristics of all four nozzles

<table>
<thead>
<tr>
<th>Parameter</th>
<th>N1</th>
<th>N2</th>
<th>N3</th>
<th>N4</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\dot{m}_f$ (kg/h)</td>
<td>1.72</td>
<td>3.27</td>
<td>5.21</td>
<td>6.78</td>
</tr>
<tr>
<td>$D_{10}$ (µm)</td>
<td>28</td>
<td>27</td>
<td>28</td>
<td>26</td>
</tr>
<tr>
<td>$D_{32}$ (µm)</td>
<td>36</td>
<td>35</td>
<td>37</td>
<td>35</td>
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<tr>
<td>$D_{V10}$ (µm)</td>
<td>29</td>
<td>29</td>
<td>30</td>
<td>29</td>
</tr>
<tr>
<td>$D_{V50}$ (µm)</td>
<td>39</td>
<td>39</td>
<td>40</td>
<td>39</td>
</tr>
<tr>
<td>$D_{V90}$ (µm)</td>
<td>60</td>
<td>62</td>
<td>64</td>
<td>63</td>
</tr>
</tbody>
</table>

Section 4.2: For higher power density cases the walls were cooled: how is this non-adiabatic behavior accounted for in the models?
Response: For all cases of higher thermal inputs, heat loss through water cooling and combustor walls is considered during the modeling. This information has been clearly brought out in the revised manuscript on page 9, line 21 to page 10, line 5 and page 15, line 2-4.

11) Section 4.2: If the combustor is operated in non-adiabatic conditions, surely it is necessary to have either a constant wall temperature, or constant removal of heat from the system. However, it seems that neither is constant. The authors need to expand on this issue.

Response: For a given thermal input, the heat removal rate during the burner operation is maintained constant. The amount of heat removal from the combustor walls is 3.2, 8.3, and 12.9 kW respectively, for heat intensities of 10.2, 16.3 and 21.1 MW/m³. This heat removal rate has considered by applying heat loss from the walls of the combustor. This information has been added in the revised manuscript on page 9, line 21 to page 10, line 5 and page 15, line 2-4.

12) Section 4.2: The temperature fluctuations are reported as 1.3-1.8% -- this certainly seems a low fluctuation, but how much of this because of the thermal inertia of the large bead? (see comment #8).

Response: The intention of the authors is only to report the variation of the mean temperature along in radial direction. Since the thermocouple response time (~0.25 s) is much larger than the integral turbulence time scales (~ 3 ms) due to larger bead size, it is difficult to record the temporal variation of temperature at a particular location. Thermal inertia of the thermocouple is expected to play an insignificant role in the measured temperature. This information has been appropriately appended to remove the ambiguity in the revised manuscript on page 14, line 11-17.

13) Section 4.2: How do the experimental measurements of temperature compare to the numerical simulations?

Response: The computational and experimental temperatures are compared and shown in the figure below. The predicted temperatures in the central zone of the combustor are slightly lower than the measured temperatures for all thermal input conditions. For the outer region (next to the central zone) predicted temperatures are higher than the measured temperatures. This is because uniformly distributed temperature with low temperature gradients is observed in computational analysis. These details and modified Fig. 6 has been added in the revised manuscript on page 15, line number 19-23.
14) Table 2: If the burner geometry needs to change for different operating conditions, how could this combustor be used for practical applications? If not a practical combustor, how could these results be used for the development of a practical combustor?

Response: This discussion reported in the paper shows that minimum recirculation rate is must for achieving flameless combustion mode. For instance, in a practical combustor with fixed upper limit of thermal input (84.7 kW), the chamfer radius can be fixed at $R_C = 25$ mm and same combustor can be used for lower thermal inputs (21.5 – 84.7 kW) without any issue related to combustion stability. However, it needs to be changed for higher thermal inputs. This information added in the revised manuscript in page No 17, line number 1-5.
Reviewer #3: Excellent

The English in this paper needs to be improved? (1 = Yes; 2 = No; 3 = See comment below) [1-3] 2

This paper requires review by a native English speaker or a translation service? (1 = Yes; 2 = No; 3 = See comment below) [1-3] 2

The paper reports an interesting and clearly written study to scale up a flameless oxidation system for kerosene. While the real progress seems to have been made through experimentation, the authors used CFD in an intelligent fashion to guide the experimental work. The changes made to achieve flameless oxidation at high thermal input are all motivated physically and insightfully. "Despite" the more engineering character of the work presented, the work is in my opinion original, thoughtful and of the high quality suitable for the symposium The clear documentation and argumentation assure the work having impact in the field of flameless oxidation systems. I recommend acceptance.

Response: Authors are happy to note that the reviewer understands and appreciates the work presented in the paper. Authors are thankful to reviewer for recommending this paper for acceptance at symposium and graded the paper as an excellent contribution. We gracefully accept the reviewer’s comments to improve the quality of the present manuscript.

Point by point response to reviewer’s comments is given below and the proposed changes have been incorporated in the revised manuscript.

1. One small point: while the paper seems within the word limit, I found the last paragraph of the Introduction a significant repeat of the abstract. As such, in my opinion this paragraph may be shortened, allowing the reader to get to the "meat" of the work.

Response: The repetitive sentences pointed out by the reviewer in the introduction section have been removed in the revised manuscript.