Synthesis, characterization and self-assembly of linear and miktoarm star copolymers of exclusively immiscible polydienes†

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Introduction

Diblock copolymers constitute a highly investigated topic, due to their exceptional properties, rendering them suitable for various applications.1–4 Their unique potential is attributed to their self-assembly in several nanostructures, which is determined by the value $\chi N$ (where $\chi$: Flory–Huggins interaction parameter and $N$: degree of polymerization) and the volume fraction of at least one of the blocks ($\varphi_A$ since $\varphi_B = 1 - \varphi_A$). Recently, linear diblock copolymers, exhibiting high segment incompatibility, have been thoroughly studied due to their prospective use in nanotechnology,6,7 optoelectronics8 etc. Advances on anionic and controlled/living radical polymerization techniques provide the opportunity of synthesizing complex architecture copolymers and terpolymers,9–13 leading to enhanced properties of these materials when compared to their linear analogues.14 Microphase separation of miktoarm star copolymers particularly of the AB$_n$ type (where $n = 2, 3, etc.$) results in differentiations on the expected self-assembly topologies, and unique morphologies are obtained, due to the restrictions imposed by the single junction point on which all chains are connected.12,15,16

The morphologies adopted from miktoarm star copolymers depend on the total degree of polymerization ($N$), the volume fraction ($\varphi$), the A/B segment–segment Flory–Huggins interaction parameter ($\chi$), the molecular architecture and the elasticity parameter ($\epsilon$), which describes the effect of both chain architecture and elastic asymmetry in the strong-segregation regime.17–19 Although, synthesis and microphase separation of complex architecture systems, containing a number of different dissimilar segments, have been analytically investigated in the literature,9 only a few cases involving elastomeric
blocks and specifically polyisoprene (PI) and polybutadiene (PB)have been reported. The possible segment microstructures for PB are: 1,4-cis, 1,4-trans and 1,2, while for PI are: 1,4-cis, 1,4-trans, 3,4-a and 1,2. When the 3,4-microstructure of PI is significantly increased (~55–60%), then the 1,2-microstructure is increased as well (15–25%) leading to a small percentage for the 1,4 linear segments. In general, the possible combinations of microstructures for PB and PI in a diblock copolymer result in the following sequences: \( \text{PB}_{1,4} \cdot \text{b-PI}_{1,4} \), \( \text{PB}_{1,2} \cdot \text{b-PI}_{1,4} \), \( \text{PB}_{1,2} \cdot \text{b-PI}_{3,4} \) and \( \text{PB}_{1,4} \cdot \text{b-PI}_{3,4} \).

For block copolymers, the type and relative amount of the specific stereoisomers should always be taken into consideration, since local structure influences the segment–segment interaction parameter. The aforementioned combinations of polydiene chains, namely \( \text{PB}_{1,4} \cdot \text{b-PI}_{1,4} \), \( \text{PB}_{1,2} \cdot \text{b-PI}_{1,4} \) and \( \text{PB}_{1,2} \cdot \text{b-PI}_{3,4} \), have been explored, and the interaction parameters were found sufficiently low, concluding to mixed homogeneous phases, either for copolymers or even blends of the polydiene pairs in typical molecular weights. The \( \chi \) interaction parameter of diblock copolymers of predominantly 1,4-PB and predominantly cis-1,4 PI with either or both of the corresponding linear homopolymers has been determined. Cohen and Wilfong reported the first time for an ABC miktoarm star terpolymer consisting of PS, PB and PI, where the two polydienes exhibited respective microstructures (~92% 1,4-microstructure for PB and ~55–60% 3,4-microstructure for PI). Apart from their self-assembly capability, copolymers consisted of at least one elastomeric unit exhibit interest in the field of rheology, due to their fatigue resistance and viscoelastic properties, rendering them appealing materials as adhesives for industrial applications.

In this study, we report the synthesis of four (4) linear diblock copolymers of the \( \text{PB}_{1,4} \cdot \text{b-PI}_{3,4} \) sequence, four (4) asymmetric miktoarm star copolymers of the \( \text{PB}_{1,4} \cdot \text{b-PI}_{3,4} \) and four (4) of the \( \text{PB}_{1,4} \cdot \text{b-PI}_{3,4} \) type. The synthesis procedure and properties of such non-linear copolymers have not been reported in the literature yet.

The molecular characterization of all samples was performed through size exclusion chromatography (SEC), to confirm the dispersity (\( D \)), and membrane osmometry (MO) to calculate the number average molecular weight, \( (M_n) \) values. Moreover, proton nuclear magnetic resonance spectroscopy \((^{1}H\text{-NMR})\) was employed to verify the characteristic ratios of stereochimical microstructures for the polydienes as well as to identify the composition of each segment. Thermal analysis \textit{via} differential scanning calorimetry (DSC) was also performed to examine the glass transition temperatures \( (T_g) \) of the two blocks, their potential microphase separation when studied in bulk, and the dependence of the architecture on the \( T_g \) of each system.

Morphological characterization was carried out exclusively through bright-field transmission electron microscopy (TEM), to verify the microphase separation and provide significant information concerning the dependence of the complex architecture on the adopted morphology. It should be mentioned that the total average molecular weight of the PB block, as well as the volume fraction, remained almost identical in both linear and non-linear copolymer systems in order to compare their structure/properties relationship and verify the influence of non-linear architecture in the self-assembly of such systems.

### Experimental
#### Materials

1,3-Butadiene (99%), trichloromethylsilane \((\text{CH}_3\text{SiCl}_3)\) (99%), tetrachlorosilane \((\text{SiCl}_4)\) (99%), and calcium hydride \((\text{CaH}_2)\)
(95%) were purchased from Sigma-Aldrich, isoprene (98%), sec-butyllithium, n-butyllithium and styrene (99%) from Acros Organics, benzene (99.7%) from Chem-Lab, tetrahydrofuran (THF) (99.9%) from Carlo Erba, toluene (99.7%) from Honeywell and methanol (99%) from Fluka. The purification methods of all reagents involved in the polymerizations were carried out based on the requirements of anionic polymerization and are well elaborated elsewhere.41,42

Instrumentation

Size exclusion chromatography (SEC) measurements were carried out using a SpectraSystem P1000 equipped with an isocratic pump, column oven (LabAlliance) heated at 30 °C, three columns in series (PLgel 5 mm Mixed-C, 3007.5 mm), refractive index (RI, Shodex RI-101) and ultraviolet absorbance (UV, SpectraSystem UV1000) detectors. Tetrahydrofuran (THF) was the eluent at a flow rate of 1.0 mL min⁻¹ and the system was calibrated with eight PS standards (M_p: 4300 to 3 000 000 g mol⁻¹).

Membrane osmometry (MO) was adopted to determine the number average molecular weight by using a Gonotec Osmomat 090 in 35 °C using toluene as solvent.

Proton nuclear magnetic resonance (¹H-NMR) spectroscopy was carried out in CDC13 at 25 °C using Bruker AVANCE II spectrometers operating at 250 and 400 MHz and data were processed using UXNMR (Bruker) software.

Differential scanning calorimetry (DSC) measurements were performed on a Q20 TA instrument. The heating ramp was 5 °C min⁻¹ and the temperature range from −120 °C to 40 °C. A small amount of 5 mg was used from each sample. Two heating and one cooling cycles were performed and the results of the second heating were reported and analysed using Advantage v5.4.0 (TA instruments) software.

Transmission electron microscopy (TEM) experiments were performed in a JEOL 2100 TEM using 200 keV as the acceleration voltage. Cryo-ultramicromoting of the as-cast films was performed in a Leica EM UC7 ultramicrotome, in order to obtain very thin sections (≈40 nm) at −100 °C (below the lowest T_g of both PB₁,₄ and PI₃,₄, being approximately −90 °C and −10 °C respectively) and the sections were picked up on 600 mesh copper grids. Since both blocks are exclusively consisting of carbon and hydrogen atoms, selective staining with osmium tetroxide (OsO₄) 4% aqueous solution was employed for ≈60 minutes (based on the aging of the stain solution).

Synthesis of linear and non-linear diblock copolymers

A thorough description of the synthetic protocol for the linear diblock copolymers of the PB₁,₄-b-PI₃,₄ type has already been mentioned in the literature by Zapsas et al.22 However, the novel synthesis of the miktoarm star copolymers consisting of only polydiene segments is documented for the first time. Specifically, four (4) miktoarm star copolymers of the PB₁,₄(PI₃,₄)₂ and four (4) of the PB₁,₄(PI₃,₄)₃ type were synthesized following the justified synthetic protocols of anionic polymerization and chlorosilane chemistry, under high vacuum conditions. The anionic polymerization and linking reactions were carried out in evacuated, n-BuLi washed custom-made glass reactors, at room temperature. Reagents were added via break-seals and aliquots for characterization were taken by heat-sealing of constrictions at all steps.

The analytical adopted synthetic procedure for the preparation of the miktoarm star copolymers of the PB₁,₄(PI₃,₄)₂ type belonging to set no. 1 is described: following the purification of 1,3-butadiene (15 g, 0.27 mol), the monomer was distilled in the apparatus, containing purified benzene (500 mL) and subsequently, sec-BuLi (0.34 mmol) was introduced to the solution leading to initiation of the 1,3-butadiene polymerization, which was completed after 24 hours at room temperature (Fig. 1a). A small aliquot was taken for the molecular characterization of the PB segment via SEC, MO and ¹H-NMR. The living PB₁,₄ chains reacted instantly and under continuous stirring with excess (at least 500-fold excess ∼0.17 mol) of linking chlorosilane reagents (either CH₃SiCl₃ or SiCl₄) to exclusively substitute just one chlorine atom as shown in Fig. 1b for the case of CH₃SiCl₃ and in Fig. 1c for SiCl₄. After the complete removal of the excess of the linking reagent on the high vacuum line, a substantial amount of purified benzene was distilled in the apparatus to re-dilute the PB₁,₄-SiCl₃ or the PB₁,₄-SiCl₄ intermediate product. To a separate glass apparatus, an appropriate amount of isoprene (21.5 g, 0.31 mol) and sec-BuLi (0.6 mmol) in a mixture of non-polar solvent (benzene, 500 mL) and polar solvent (THF, 1 mL) were introduced under high vacuum and were left to react at room

Fig. 1 Schematic illustration of the synthesis of the PB₁,₄(PI₃,₄)₂ and PB₁,₄(PI₃,₄)₃ miktoarm star copolymers. (a) Synthetic route for the living PB precursor. PB₁,₄⁻¹Li⁺, (b) coupling reaction between trichloromethylsilane and PB₁,₄⁻¹Li⁺, (c) coupling reaction between silicon tetrachloride and PB₁,₄⁻¹Li⁺, (d) synthesis reaction of the living PI chains, PI₃,₄⁻¹Li⁺, (e) linking reaction for the synthesis of miktoarm star copolymer of the PB₁,₄(PI₃,₄)₂ type and (f) corresponding linking reaction for miktoarm star copolymer of the PB₁,₄(PI₃,₄)₃ type.
temperature for 24 hours (Fig. 1d) to synthesize the living PI3.4-Li (I) exhibiting the required 3,4-microstructure (∼55–60%). In the case of PB1,4(Li,Sl), different amount of isoprene was employed, specifically 14.5 g of monomer (0.21 mol) were reacted with 0.6 mmol sec-BuLi. An excess of the PI3.4-Li(I) (∼20% excess compared to the Si–Cl living ends of the PB1,4-Si-Cl2 or PB1,4-Si-Cl3) was introduced in the polymerization reactor substituting all remaining chlorine atoms evident in the PB1,4-Si-Cl2 or the PB1,4-Si-Cl3 intermediate products, leading eventually to the desired PB1,4(Li,Sl) and PB1,4(SI3.4)3 miktoarm star copolymers respectively (Fig. 1e and f).

Results and discussion

Molecular characterization results of linear diblock and non-linear miktoarm star copolymers

The molecular characterization results for all samples [linear diblock copolymers of the PB1,4-b-PI3,4 type and miktoarm star copolymers of the PB1,4(PI3,4)2 and PB1,4(PI3,4)3 type respectively] are presented in Table 1 indicating compositional and molecular homogeneity. The mass fraction, \( f_b \), was calculated via \(^1\)H-NMR measurements. For comparison reasons, the samples were divided into 4 different sets, where each set includes one linear diblock copolymer with similar molecular characteristics to the corresponding PB1,4(PI3,4)2 and PB1,4(PI3,4)3 miktoarm stars. The glass transition temperatures for all final materials were determined via DSC. The dispersity indices were retrieved by SEC measurements and the number average molecular weights (\( M_n \)) for the individual blocks and the final copolymers were calculated by MO.

All diblock copolymers were synthesized through anionic polymerization by using the sequential monomer addition method and high vacuum techniques, while for the non-linear copolymers, selective chlorosilane chemistry was employed. High 3,4-microstructure was adopted for all PB blocks by using a small amount (~1 mL) of a polar additive (THF). The total number average molecular weight of the final copolymers, in all cases, was kept constant at approximately 100 kg mol\(^{-1}\), to compare the molecular and morphological characteristics of the linear diblock copolymers with the respective miktoarm stars. Furthermore, such diblock copolymers with the specific segments and microstructure content have been sparsely synthesized and studied in bulk up to date.\(^{22}\) It is important to mention that these types of miktoarm star copolymers were synthesized for the first time and have never been reported in the literature. In all cases, PB was the first block (PB1,4-b-PI3,4 sequence) since it is not possible to synthesize well-defined PI3.4-b-PB1,4 taking into account that the presence of THF from the beginning of the polymerization (when PI is the first block) would increase the 1,2-microstructure of PB and no microphase separation would be observed.

As already reported in the literature, microphase separation between the two blocks is evident only when the 3,4-microstructure content of the PI is high (∼55–60%), and that of the PB block shows high 1,4-microstructure (∼92%).\(^{22-24,31}\)

The monomodal molecular weight distributions of the four linear diblock copolymers of the PB1,4-b-PI3,4 type, indicating high molecular and compositional homogeneity, as well as the absence of any undesired by-products during the synthetic procedure, are observed in Fig. 2a. In the ESI, (Fig. S1 and S2†), two representative chromatographs of the linear samples (PB1,4-b-PI3,4-3 and PB1,4-b-PI3,4-4) are depicted separately along with the initial PB precursors.

For all miktoarm star copolymer samples, the total number average molecular weight varied between 88–109 kg mol\(^{-1}\), in agreement with the corresponding values mentioned already for the linear diblock copolymers. Additionally, the number average molecular weight of the PB arms for each set is kept constant. Accordingly, narrow dispersity indices for all miktoarm star copolymers are illustrated in Fig. 2b and c, respectively. In the ESI, (Fig. S3 and S4†) the SEC chromatographs of the PB and PI blocks, the unfraccionated and the final fractionated miktoarm star copolymers of the PB1,4(PI3,4)2-S8 and PB1,4(PI3,4)3-S8 are shown separately. The solvent/non-solvent fractionation technique was used to remove the undesired products, which were formed during the linking reactions of the

<table>
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<tr>
<th>Sample sets</th>
<th>Samples</th>
<th>( M_n )bb ( ^a ) (kg mol(^{-1}))</th>
<th>( M_n )bb ( ^a ) (kg mol(^{-1}))</th>
<th>( M_n )total ( ^a ) (kg mol(^{-1}))</th>
<th>( D_{\text{total}} ^b )</th>
<th>( f_{PB} ^c )</th>
<th>( \varphi_{PB} ^d )</th>
<th>( (T_g)_Pb ^e (°C) )</th>
<th>( (T_g)_Sb ^f (°C) )</th>
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<td>38.2</td>
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<td>PB1,4(PI3,4)2</td>
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<td></td>
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<td>23.2</td>
<td>109.4</td>
<td>1.07</td>
<td>0.40</td>
<td>0.40</td>
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<td>1.05</td>
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<td></td>
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<tr>
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<tr>
<td></td>
<td>PB1,4(PI3,4)2</td>
<td>55.2</td>
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<td>PB1,4(PI3,4)2</td>
<td>27.5</td>
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<td>94.5</td>
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<tr>
<td></td>
<td>PB1,4(PI3,4)3</td>
<td>27.5</td>
<td>25.7</td>
<td>101.6</td>
<td>1.05</td>
<td>0.28</td>
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\(^a\) MO in toluene at 35 °C. \(^b\) SEC in THF at 30 °C. \(^c\) \(^1\)H-NMR measurements in CDCl3 at 25 °C. \(^d\) From the equation \( \varphi_{PB} = \frac{f_{PB}}{f_{PB} + f_{PI} + f_{S}} \). \(^e\) DSC measurements.
living blocks with the corresponding chlorosilane (CH$_3$SiCl$_3$ or SiCl$_4$). The molecular characterization via $^1$H-NMR spectroscopy was necessary to verify the composition results as revealed by SEC and MO, as well as to confirm the existence of the desirable 3,4-microstructure at high values (>55%) for the PI segments and the 1,4-microstructure for the PB blocks (∼92%) in all synthesized materials.

In Table S1, the type and number of protons with the corresponding chemical shifts for protons incorporated in the monomeric units of polybutadiene and polyisoprene are presented. Three representative spectra corresponding to samples PB$_{1,4}$-b-PI$_{3,4}$, PB$_{1,4}$(PI$_{3,4}$)$_2$-S$_7$, and PB$_{1,4}$(PI$_{3,4}$)$_3$-S$_8$ (corresponding to set no. 4) are given in Fig. 3. For each sample, the corresponding $^1$H-NMR spectrum of initial block PB$_{1,4}$, intermediate PI$_{3,4}$, and the final linear or non-linear copolymer is given for comparison reasons. The mass fractions and characteristic microstructure content of each arm (PB and PI), as calculated directly from the $^1$H-NMR spectra, are shown in Table S2. High 3,4-microstructure (57–62%) was obtained for all the PI blocks of the twelve (12) synthesized materials, while all PB blocks were enriched in 1,4-microstructure (90–92%).

Thermal characterization results of linear diblock and non-linear miktoarm star copolymers

Analysing the DSC results of all samples, two endothermic transitions were obtained, corresponding to the $T_g$ of PB$_{1,4}$ and PI$_{3,4}$. Crystallization and melting temperatures ($T_m$) are not evident in any thermograph, since both PB and PI, as synthesized by anionic polymerization with the specific microstructures, exhibit $T_m$ above 40 °C and the non-linear microstructures (−1,2 and −3,4) are mostly atactic with very low degree of crystallization. The existence of two $T_g$ similar to the $T_g$ of the corresponding homopolymers$^{27}$ leads to the con-
Toluenes employed. PI chains are stained less, since the double bonds
involved.33,43
almost identical electron density of the two polydiene seg-
ments was accomplished exclusively by TEM studies. It should
be noted that this type of copolymers cannot be studied with
small angle X-ray scattering (SAXS) due to the similar and
be noted that this type of copolymers cannot be studied with
SAXS measurements in order to calculate the interaction parameter \( \chi \), by studying the order-

disorder transition as a function of temperature.

**Set no. 1**
The TEM images obtained from the stained sections of PB\(_{1,4}\)-b-
PB\(_{1,4}\)-1 diblock copolymer after being thermally annealed are presented in Fig. 5. As far as the
PB\(_{1,4}\)-b-PB\(_{1,4}\)-1 diblock copolymer is concerned, alternating lamellae of the two different phases were adopted as illus-
trated in the TEM image (Fig. 5a). Alternating dark grey and
white/grey layers are evident in which the dark layer (PB\(_{1,4}\)) is slightly smaller in dimensions when compared with the other
layer, PB, verifying therefore the volume fraction (0.42 for PB\(_{1,4}\)) as calculated from \(^1\)H-NMR. Moreover, no discrepancy is
encountered with the morphology predicted by the phase
diagram of the PS-b-PI diblock copolymer system.45-47 In the
TEM image (Fig. 5b) from thin sections of the annealed PB\(_{1,4}\)
(PB\(_{1,4}\))\_2 sample with PB\(_{1,4}\) volume fraction equal to 0.41, hex-
agonally close-packed cylinders of the dark grey phase (PB\(_{1,4}\))
in the white matrix (PI\(_{3,4}\)) are evident. The TEM image (Fig. 5c)
from the annealed PB\(_{1,4}\)(PI\(_{3,4}\))\_2 sample, with PB\(_{1,4}\) volume
fraction equal to 0.40, indicates bcc spheres of the dark grey
PB\(_{1,4}\) domains in a white PI\(_{3,4}\) matrix.

The image does not show any alternating layers (as in the
hcp cylinders), and since no SAXS experiments are possible,
based on the phase diagram for non-linear copolymers of the

**Morphological characterization results of linear diblock and
non-linear miktoarm star copolymers**
The morphological characterization of all synthesized poly-
mers was accomplished exclusively by TEM studies. It should
be noted that this type of copolymers cannot be studied with
small angle X-ray scattering (SAXS) due to the similar and
almost identical electron density of the two polydiene seg-
ments involved.13,43

The sample preparation used to investigate the morphology
of all final copolymers in bulk is a crucial and important pro-
cedure. The casting was performed in a non-selective solvent
for several days to promote the formation of equilibrium
morphologies.22,44 Initially, for the preparation of the thin
films, a 5% w/v solution of each sample in toluene was pre-
pared. The samples were casted for approximately 5-7 days in
a properly established saturated environment. Films with a
thickness approximately 1 mm were formed and parts of them
were placed in an oven for thermal annealing (50 °C) for 5
days. Afterwards, each film was removed from the annealing
oven and immersed in liquid nitrogen for a few seconds to
keep the adopted structure at a high annealing temperature.

The quenched films were directly cryo-ultramicrotomed, and
thin films of approximately 40 nm were collected on copper
grids. In order to enhance the intrinsic difference in electron
density between the PB and PI blocks, selective staining with
aqueous solution of OsO\(_4\) for approximately 1 hour, was
employed. PI chains are stained less, since the double bonds
of PI\(_{3,4}\) segments are sterically hindered compared to those of
PB\(_{1,4}\) domains.23,27,13

Another important aspect of the PB\(_{1,4}\)/PI\(_{3,4}\) copolymers
system is that the interaction parameter \( \chi \) is yet unknown.
Furthermore, the restrictions concerning the electron densities
of both PB and PI, do not allow SAXS measurements in order
to calculate the interaction parameter \( \chi \), by studying the order-

**Fig. 4** DSC thermograph for samples constituting set no. 4, where
PB\(_{1,4}\)-b-PB\(_{1,4}\)-4, PB\(_{1,4}\)(PI\(_{3,4}\))\_2-S\(_{7}\) and PB\(_{1,4}\)(PI\(_{3,4}\))\_3-S\(_{8}\) are the black, blue
and red colour curves respectively. In the blue frame the glass transition
temperatures for all the PB blocks are presented and in the red frame
the glass transition temperatures of the PI block are depicted.

**Fig. 5** Bright-field TEM images of the first set of the PB\(_{1,4}\)(PI\(_{3,4}\))\_n diblock copolymer type samples after thermal annealing at 50 °C for 5 days followed by
microtoming and staining with vapors of OsO\(_4\) for approximately 1 hour corresponding to: (a) PB\(_{1,4}\)-b-PB\(_{1,4}\)-1 diblock copolymer, (b) PB\(_{1,4}\)(PI\(_{3,4}\))\_2-
S\(_{7}\) miktoarm star copolymer and (c) PB\(_{1,4}\)(PI\(_{3,4}\))\_3-S\(_{8}\) miktoarm star
copolymer.
PS/PI system, the TEM is significantly indicating bcc spheres of minority component (PB) in the matrix of the majority (PI).

Set no. 2

In Fig. 6 the TEM images obtained from the stained sections of samples PB_{1,4}-b-PI_{3,4}-2, PB_{1,4}(PI_{3,4})_2-S_3 and PB_{1,4}(PI_{3,4})_3-S_4, after being thermally annealed are presented. In all cases, the PB_{1,4} domains are the majority component since the volume fractions (Table 1) for PB_{1,4} are 0.71, 0.67 and 0.69, respectively. For the linear diblock copolymer PB_{1,4}-b-PI_{3,4}-2, hexagonally close-packed cylinders of the minority component (PI) in the matrix of the majority (PB) are evident (Fig. 6a). A cubic structure based on the G minimal surface (double gyroid) is expected at the SSL (strong segregation limit) for the PS-b-PI diblock copolymer for similar volume fraction (0.29 of the minority component) taking into consideration the relevant phase diagram $\chi N$ vs. $f(\psi)$, where $\chi$ is the Flory–Huggins interaction parameter, $N$ the total degree of polymerization and $\psi$ the volume fraction of the minority component.\(^{45-47}\) For both annealed miktoarm star copolymers PB_{1,4}(PI_{3,4})_2-S_3 and PB_{1,4}(PI_{3,4})_3-S_4 alternating lamellar structures were observed, where the dark grey area corresponds to the PB_{1,4} phase and the white to the PI_{3,4} domains (Fig. 6b and c respectively).

Set no. 3

Further TEM studies were conducted and are presented in Fig. 7, for the third set of copolymers, specifically for the PB_{1,4}-b-PI_{3,4}-3 PB_{1,4}(PI_{3,4})_2-S_3 and PB_{1,4}(PI_{3,4})_3-S_6 after thermal annealing at 50 °C for 5 days. Similar to the PB_{1,4}-b-PI_{3,4}-1, alternating lamellae of the two different phases was evident for sample PB_{1,4}-b-PI_{3,4}-3 (Fig. 7a). The only difference in the PB_{1,4}-b-PI_{3,4}-3 lies on the reversibility of the layer thickness where in this case the PB_{1,4}(\psi_{PB} = 0.59) layer (dark grey) is slightly larger than the PI layer, verifying, the volume fraction from the molecular characterization studies. No discrepancy is encountered with the adopted morphology for sample PB_{1,4}-b-PI_{3,4}-3 from that expected for a PS-b-PI diblock copolymer sample with identical molecular characteristics and composition.\(^{45-47}\) Similarly, TEM micrographs (Fig. 7b) from thin sections of the annealed PB_{1,4}(PI_{3,4})_2-S_3 sample with PB volume fraction equal to 0.57 showcase alternating lamellae of the dark grey phase (PB_{1,4}) and the white phase (PI_{3,4}). The TEM (Fig. 7c) image of the annealed PB_{1,4}(PI_{3,4})_3-S_6 sample with PB volume fraction equal to 0.56 illustrates hexagonally close-packed cylinders [dark grey phase (PB_{1,4}) in a white matrix (PI_{3,4})]. For this sample, despite thermal annealing, no long-range order could be observed, as evident in the other related samples with different volume fractions. A possible explanation could be allocated to the fact that the thin sections were slightly mechanically deformed as taken from the microtome and were placed on the TEM grid. For all samples [except PB_{1,4}(PI_{3,4})_3-S_6] the TEM images are indicating distinct and straightforward microdomains with relevant long-range order.

Set no. 4

TEM results for samples PB_{1,4}-b-PI_{3,4}-4, PB_{1,4}(PI_{3,4})_2-S_2 and PB_{1,4}(PI_{3,4})_3-S_8 after thermal annealing, are presented in Fig. 8. These materials compose the last set of samples with the lowest volume fraction of PB (0.32, 0.30 and 0.28 respectively). For the linear diblock PB_{1,4}-b-PI_{3,4}-4, dark grey hexagonally packed cylinders of PB_{1,4} in the white/grey matrix of the PI phase was the adopted morphology (Fig. 8a). Since the volume fraction of PB_{1,4} is equal to 0.32, according to the morphological behaviour of the already studied PS-b-PI system, a cubic
structure (double gyroid), with networks of the minority component (PB) in the matrix of the majority (PI) should be observed.45-47

Since PB1,4 and PI3,4 are very flexible chains, the adaptation of such a complex 3D morphology may not be possible due to entropic and enthalpic constrains, leading to a less thermodynamically demanding 2D topology. Therefore, hexagonally close-packed (hcp) cylinders of the minority phase (PB) in the matrix of the majority (PI) are preferred. In this case, it would be interesting to prepare binary blends of the diblock copolymers, with either homopolymer PB1,4 or homopolymer PI3,4 in order to explore whether the double gyroid morphology will appear in the volume fraction regime 0.25–0.32. If not, then the specific studied system indicates a major discrepancy with the microphase separation of the well-studied PS-b-PI12-45 diblock copolymer system.

For the PB1,4(PI3,4)2-S8, the TEM image (Fig. 8b) clearly indicates hexagonally close-packed cylinders of the dark grey phase (PB1,4) in the white matrix (PI3,4), whereas the corresponding image of the annealed PB1,4(PI3,4)3-S8 shows bcc spheres of the dark grey phase (PB1,4, \( \phi_{PB} = 0.28 \)) in a white matrix (PI3,4). The image does not show any alternating layers (as in the hcp cylinders), and since no SAXS experiments are possible, we rely on the fact (by tilting) that the TEM micrograph in Fig. 8c indicates exclusively bcc spheres of the minority component (PB) in the matrix of the majority (PI).

In Table 2, the molecular characteristics, volume fractions, degree of polymerization (N), theoretically predicted morphologies and verification of the adopted morphology for all the linear and non-linear polydiene copolymers PB(PI)n (where \( n = 1, 2, 3 \)) system,42,44,45 are summarized.

It is straightforward from Table 2 that for each set of samples, copolymers with identical molecular characteristics (almost constant total number average molecular weight) have been synthesized in order to be compared based on the complexity of the architecture, as well as on the differentiation in adopted topology for identical samples indicating different volume fractions. It is the first time that such a study is being reported directly for linear and non-linear materials composed exclusively of immiscible polydienes (PB1,4 and PI3,4), which microphase separate.

The results between the theoretically predicted morphology,47 and the experimentally observed by TEM, did not lead to any discrepancies for the novel miktoarm stars, when compared with the corresponding results for similar linear and non-linear PS/PI systems, as evident from the last column of Table 2. It was expected that such an agreement would occur only for the linear diblock copolymers, or even for the least complex architecture [samples of the PB1,4(PI3,4)2 type]. The fact that PB1,4(PI3,4)3 type of copolymers also showed similar agreement is of great importance, since it verifies our assumption regarding identical Kuhn lengths between the two polydiene, leading to elasticity parameters (\( \epsilon \)) exclusively dependent on the number of chains.

### Table 2  Molecular characteristics, volume fractions, degrees of polymerization (N), theoretically predicted morphologies and verification of morphology for all the copolymers synthesized (the symbol * indicates morphology of low long-range order)

<table>
<thead>
<tr>
<th>Sample sets</th>
<th>Samples</th>
<th>( \langle M_n \rangle_{local} ) (kg mol (^{-1} ))</th>
<th>( \phi_{PB} )</th>
<th>( \phi_{PI} )</th>
<th>( N_{PB1,4/PI3,4} )</th>
<th>Morphology from theory</th>
<th>Verified morphology</th>
</tr>
</thead>
<tbody>
<tr>
<td>Set no. 1</td>
<td>PB1,4-b-PI3,4-1</td>
<td>93.6</td>
<td>0.42</td>
<td>0.58</td>
<td>1522</td>
<td>CYL</td>
<td>✓</td>
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<td>PB1,4-b-PI3,4-2</td>
<td>107.3</td>
<td>0.41</td>
<td>0.59</td>
<td>1836</td>
<td>CYL</td>
<td>✓</td>
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<td>PB1,4-b-PI3,4-3</td>
<td>109.4</td>
<td>0.40</td>
<td>0.60</td>
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<td>SPH</td>
<td>✓</td>
</tr>
<tr>
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<td>PB1,4-b-PI3,4-4</td>
<td>92.4</td>
<td>0.71</td>
<td>0.29</td>
<td>1606</td>
<td>DG</td>
<td>CYL</td>
</tr>
<tr>
<td></td>
<td>PB1,4-b-PI3,4-5</td>
<td>92.4</td>
<td>0.67</td>
<td>0.33</td>
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<td>LAM</td>
<td>✓</td>
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<td>PB1,4-b-PI3,4-6</td>
<td>88.2</td>
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<td>0.31</td>
<td>1571</td>
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<td>PB1,4-b-PI3,4-7</td>
<td>98.5</td>
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<td>0.41</td>
<td>1670</td>
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<td>1692</td>
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<td>PB1,4-b-PI3,4-9</td>
<td>100.3</td>
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<td>0.44</td>
<td>1709</td>
<td>CYL</td>
<td>✓</td>
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<td>PB1,4-b-PI3,4-10</td>
<td>107.9</td>
<td>0.32</td>
<td>0.68</td>
<td>1722</td>
<td>DG</td>
<td>CYL</td>
</tr>
<tr>
<td></td>
<td>PB1,4-b-PI3,4-11</td>
<td>95.5</td>
<td>0.30</td>
<td>0.70</td>
<td>1523</td>
<td>CYL</td>
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<td>0.28</td>
<td>0.72</td>
<td>1643</td>
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</tbody>
</table>

LAM, alternating lamellae; CYL, hexagonally packed cylinders; SPH, spheres; DG, double gyroid.
The only cases where different results were obtained from the relevant PS/PI system, was for two linear copolymers where in both samples, the expected morphology should have been the DG cubic structure (sample-2 and sample-4). In contrast, hexagonally close-packed cylinders of the minority component (PB or PI for $\varphi_{PB} = 0.71$ and $0.32$ respectively) in the matrix (PI or PB) were observed.

As already described for the specific diblock copolymers, since PB$_{1,4}$ and PI$_{3,4}$ exhibit high chain flexibility, their ability to adopt such a complex architecture (DG) may not be possible due to entropic as well as enthalpic constrains. As a result, this leads to a less thermodynamically demanding topology such as the hcp cylinders of the minority phase in the matrix of the majority.

Moreover, rheological studies of the aforementioned synthesized materials would be of great scientific interest, since elastomers are materials which are capable of undergoing extremes on stress/strain mechanical properties studies and will provide further insight into polymer dynamics. We aim, in order to complete the structure property relationship of the specific copolymer system, to calculate the $\chi_{eff}$ with SANS and rheology experiments as well as conclude to a more detailed phase diagram by including the morphologies adopted from the binary blends of the pure linear and non-linear copolymers with corresponding homopolymers of hPB$_{1,4}$ or hPI$_{3,4}$ respectively.

Conclusions
A series of model linear and non-linear copolymers of the PB$_{1,4}$(PI$_{3,4}$)$_n$ type (where $n = 1, 2, 3$) was successfully synthesized by employing anionic polymerization high-vacuum techniques in combination with selective chlorosilane chemistry. Specifically, twelve (12) samples were prepared and divided into four (4) different sets, where each set includes one linear diblock copolymer with similar molecular characteristics to the corresponding PB$_{1,4}$(PI$_{3,4}$) and PB$_{1,4}$(PI$_{3,4}$) miktoarm stars. Molecular characterization was performed through SEC, MO, and $^1$H-NMR measurements, indicating a high degree of molecular and compositional homogeneity in all cases. DSC and TEM studies verified the microphase separation and provide significant information concerning the influence of the architecture (linear or non-linear) on the adopted topology. Morphological characterization studies also revealed the coherence of theoretical [for the PS[PI]$_h$ system] and experimental [for the PB$_{1,4}$(PI$_{3,4}$)$_n$ system] results for the complex architectures. The only discrepancies from the relevant PS/PI system were found for two linear copolymers, where in both samples, hcp cylinders of the minority phase in the matrix of the majority were observed, instead of the expected DG cubic structure morphology.

Author contributions
The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

Conflicts of interest
There are no conflicts to declare.

Acknowledgements

Notes and references