

Secrecy Analysis in SWIPT Systems Over Generalized- K Fading Channels

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Abstract—In this letter, we investigate the secrecy performance of the simultaneous wireless information and power transfer (SWIPT) system over generalized- K fading channels. After analyzing the communications scenario, we derive the closed-form expression for the secrecy outage probability (SOP), and give some simplified expressions for SOP in some special cases. Effective secrecy throughput is also investigated to capture the amount of secure transmitted information. To derive the diversity order, the asymptotic SOP is also analyzed when the average signal-to-noise ratio is large sufficiently. Finally, numerical results are used to validate the correctness of our derived expressions.

Index Terms—Effective secrecy throughput, secrecy outage probability, SWIPT, and generalized- K fading channels.

I. INTRODUCTION

Some simultaneous wireless information and power transfer (SWIPT) based transmission schemes have recently received significant attention [1], because SWIPT acts as an alternative method to prolong the lifetime of energy-constrained communication works and energy supply. Although power control can also extend the battery's lifetime, the system has to use self-energy, so the effect of extending battery's lifetime is limited, compared to SWIPT. Under SWIPT schemes, time switching (TS) method in [2] was proposed to decode information and extract power simultaneously through communications. The harvesting receiver switches in time between harvesting energy and decoding information in TS systems.

Due to the open access in wireless communications [3], [4], physical layer security is an unavoidable and important issue in SWIPT systems [5]-[7]. [5]-[7] investigated the secrecy performance of SWIPT systems over Rayleigh fading channels, i.e., small-scale fading. However, the shadowing impact should be also considered in the power transfer system in wireless communications, which accounts for the large-scale fading. The composite fading (small-scale fading plus large-scale fading) should be investigated in SWIPT systems to capture the wireless fading channel more accurately.

Shadowing is usually modeled by a log-normal distributed random variable. However, there is normally no closed-form expression for some important metrics, such as secrecy outage

probability (SOP), in many common communications scenarios [8]. [9] proposed a K distributed variable to approximate the log-normal variable, which is known as generalized- K (GK) fading model. Moreover, small-scale fading is modeled by Nakagami- m distribution in GK fading model. However, the final expressions for some metrics usually include Meijer-G or other special functions, and the Meijer-G function is not viewed as a closed-form in many cases, especially in the engineering field [10]. To make the GK model more tractable, an approximate GK model was proposed in [11] by approximating the form $\int_0^\infty \exp(-t)g(t)dt$ as $\sum_{i=1}^L \omega_i g(t_i)$, where t_i, ω_i and L are the abscissas, weight factor, and number of summation terms for the Gaussian-Laguerre integration, respectively. This approximation involves only elementary functions, and the high accuracy has been proved in [11].

In this letter, the secrecy performance of TS SWIPT systems is investigated in terms of SOP. Some simplified expressions for SOP are provided in some special cases, including the high signal-to-noise ratio (SNR) region of the main link, which gives us some important and useful insights in the secrecy outage performance of SWIPT systems. Moreover, in order to capture the amount of secure transmitted information, the effective secrecy throughput (EST) is also investigated.

II. SYSTEM MODEL

A. Communications Scenario

In the TS SWIPT system, a source (S) has limited energy due to its small size, such as the sensor in wireless sensor communications, and needs to acquire energy from a beacon (B) to delivery its information bits to a destination (D). S employs self-energy for channel estimation of $S-D$ link, and harvests energy for signal transmission. However, an eavesdropper (E) wants to overhear the transmitted information from S to D .

From [2], the received energy of S from B is $E_S = P_B g_{BS} T_1$, where T_1 is the duration of energy harvesting, P_B is the transmit power of B , and g_{BS} is the channel power gain between S and B .

After acquiring adequate energy, the transmit power (P_S) from S to D can be given as $P_S = \frac{E_S}{T_2} = \frac{P_B g_{BS} T_1}{T_2}$, where T_2 is the duration of the signal transmission.

Thus, the SNRs at D and E are

$$\gamma_D = \frac{P_S g_{SD}}{N_0} = \frac{P_B T_1 g_{BS} g_{SD}}{N_0 T_2} = \alpha g_{BS} g_{SD}, \quad (1)$$

$$\gamma_E = \frac{P_S g_{SE}}{N_0} = \frac{P_B T_1 g_{BS} g_{SE}}{N_0 T_2} = \alpha g_{BS} g_{SE}, \quad (2)$$

respectively, where $\alpha = \frac{P_B T_1}{N_0 T_2}$, N_0 is the Gaussian noise power, and g_{SD} (or g_{SE}) is the channel power gain of $S-D$ link (or $S-E$ link).

B. Channel Model

We assume that all links undergo independent GK fading, where the probability density function (PDF) and cumulative

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density function (CDF) of g_{SD} are [12]

$$f_{g_{SD}}(x) = \frac{G_{0,2}^{2,0} \left(\frac{k_d m_d x}{\mu_d} \middle| \begin{matrix} - \\ k_d, m_d \end{matrix} \right)}{\Gamma(k_d) \Gamma(m_d) x}, \quad (3)$$

$$F_{g_{SD}}(x) = \frac{G_{1,3}^{2,1} \left(\frac{k_d m_d x}{\mu_d} \middle| \begin{matrix} 1 \\ k_d, m_d, 0 \end{matrix} \right)}{\Gamma(k_d) \Gamma(m_d)}, \quad (4)$$

respectively, where μ_d is the average of g_{SD} , and m_d, k_d are parameters of GK fading. $G_{\cdot, \cdot}^{a, b}(\cdot)$ and $\Gamma(\cdot)$ denote the Meijer-G and Gamma functions [15], respectively. To avoid Meijer-G function in the final SOP expression, we adopt the approximate PDF proposed by [11], [13],

$$f_{g_{SD}}(x) = \sum_{j_d=1}^L a_{d,j_d} x^{m_d-1} \exp(-\zeta_{d,j_d} x), \quad (5)$$

where $a_{d,j_d} = \frac{\theta_{d,j_d}}{\sum_{n=1}^L \theta_{d,n} \Gamma(m_d) \zeta_{d,n}^{-m_d}}$, $\zeta_{d,j_d} = \frac{k_d m_d}{\mu_d t_{j_d}}$, $\theta_{d,j_d} = \left(\frac{k_d m_d}{\mu_d t_{j_d}} \right)^{m_d} \frac{\omega_{j_d} t_{j_d}^{k_d - m_d - 1}}{\Gamma(m_d) \Gamma(k_d)}$, ω_{j_d} , t_{j_d} and L are the weight factor, the abscissas, and summation terms for the Gaussian-Laguerre integration.

We can also get the PDFs of g_{SE}, g_{BS} in similar forms to (5), where the definition of $\mu_t, m_t, k_t, a_{t,j_t}, \zeta_{t,j_t}$, $t \in \{e, s\}$, is similar to that of $\mu_d, m_d, k_d, a_{d,j_d}, \zeta_{d,j_d}$, respectively.

III. SECRECY OUTAGE PROBABILITY

If the transmitter knows the channel state information (CSI) of the wiretap channel, the transmitter can adjust the rate of confidential information (R_s) without exceeding the instantaneous secrecy capacity (C_s) according to the instantaneous CSI of the wiretap channel to achieve the perfect security, where C_s is defined as $C_s = \max\{C_d - C_e, 0\}$, where $C_d = \log_2(1 + \gamma_D)$ and $C_e = \log_2(1 + \gamma_E)$ denote the channel capacity of the main channel and wiretap channel, respectively.

We assume that S only knows the CSI of $S - D$ link, and does not have access to the CSI of $S - E$ link, i.e., silent eavesdropping. In this case, there exists a secrecy outage, because of the constant R_s . Here, we adopt the definition of SOP in [3]

$$\begin{aligned} \text{SOP} &= \Pr \{ \log_2(1 + \gamma_D) - \log_2(1 + \gamma_E) \leq R_s \} \\ &= \Pr \{ \gamma_D \leq \lambda - 1 + \lambda \gamma_E \} \\ &= \int_0^\infty \int_0^{\lambda-1+\lambda y} f_{\gamma_D, \gamma_E}(x, y) dx dy, \end{aligned} \quad (6)$$

where $f_{\gamma_D, \gamma_E}(\cdot, \cdot)$ is the joint PDF of γ_D and γ_E , and $\lambda = 2^{R_s}$.

After some mathematical manipulations, the approximate joint PDF of γ_D and γ_E can be derived as

$$\begin{aligned} f_{\gamma_D, \gamma_E}(x, y) &\approx \sum_{j_d=1}^L a_{d,j_d} \sum_{j_e=1}^L a_{e,j_e} \sum_{j_s=1}^L a_{s,j_s} \zeta_{s,j_s}^m \sum_{i=1}^L \omega_i \frac{t_i^{-m-1}}{\alpha^2} \\ &\left(\frac{x}{\alpha} \right)^{m_d-1} \left(\frac{y}{\alpha} \right)^{m_e-1} \exp \left(-\frac{\zeta_{d,j_d} \zeta_{s,j_s} x}{\alpha t_i} \right) \exp \left(-\frac{\zeta_{e,j_e} \zeta_{s,j_s} y}{\alpha t_i} \right), \end{aligned} \quad (7)$$

where ω_i and t_i represent the weight factor and abscissas of the Gaussian-Laguerre integration, respectively.

From $\int_0^\infty \int_0^\infty f_{\gamma_D, \gamma_E}(\gamma_D, \gamma_E) d\gamma_D d\gamma_E = 1$, we have $\frac{1}{\Gamma(m_s)} \sum_{i=1}^L \omega_i t_i^{m_s-1} = 1$, which can be used to simplify our following expressions.

By using some mathematical manipulations, SOP can be finally derived as

$$\begin{aligned} \text{SOP} &= 1 - \sum_{j_d=1}^L \sum_{j_e=1}^L \sum_{j_s=1}^L \sum_{i=1}^L \omega_i a_{s,j_s} a_{e,j_e} a_{d,j_d} (m_d - 1)! \\ &\sum_{k=0}^{m_d-1} \frac{1}{k!} \sum_{n=0}^k \binom{k}{n} (\lambda - 1)^{k-n} \lambda^n \frac{(m_e + n - 1)!}{(\zeta_{e,j_e} + \zeta_{d,j_d} \lambda)^{m_e+n}} \\ &\zeta_{s,j_s}^{-m_s+k-n} \zeta_{d,j_d}^{-m_d+k} t_i^{m_s-1-k+n} \alpha^{-k+n} \\ &\exp \left(-\frac{\zeta_{d,j_d} \zeta_{s,j_s} (\lambda - 1)}{\alpha t_i} \right). \end{aligned} \quad (8)$$

Although the closed-form expression for SOP includes many summation terms, there are only elementary functions, which is easier to calculate and analyze, compared to Meijer-G and other special functions. Moreover, there is a debate about whether the Meijer-G function is a closed-form outcome, especially in the engineering field [10].

A. Special Cases

The expression for SOP is complicated and not easy to get some insights. In the following, we will present some simplified expressions for SOP in some special cases.

When $\alpha \rightarrow \infty$, SOP becomes

$$\begin{aligned} \text{SOP} &= 1 - \sum_{j_d=1}^L \sum_{j_e=1}^L a_{e,j_e} a_{d,j_d} (m_d - 1)! \\ &\sum_{k=0}^{m_d-1} \frac{\lambda^k (m_e + k - 1)!}{k! (\zeta_{e,j_e} + \zeta_{d,j_d} \lambda)^{m_e+k}} \zeta_{d,j_d}^{-m_d+k}, \end{aligned} \quad (9)$$

which shows that there is no impact of $B - S$ link on SOP as $\alpha \rightarrow \infty$.

When $m_d = m_e = m_s = 1$, i.e., Log-normal-Rayleigh composite fading, SOP becomes

$$\begin{aligned} \text{SOP} &= 1 - \sum_{j_d=1}^L \sum_{j_e=1}^L \sum_{j_s=1}^L \sum_{i=1}^L \omega_i a_{s,j_s} a_{e,j_e} a_{d,j_d} \\ &\frac{\exp \left(-\frac{\zeta_{s,j_s} \zeta_{d,j_d} (\lambda - 1)}{\alpha t_i} \right)}{(\zeta_{e,j_e} + \zeta_{d,j_d} \lambda) \zeta_{s,j_s} \zeta_{d,j_d}}. \end{aligned} \quad (10)$$

It is easy to see that SOP is a decreasing function with respect to α . If we want to make SOP lower, α should be larger, i.e., increasing the transmit power at B or the ratio of T_1 to T_2 . In real communications systems, there normally exists a maximal transmit power constraint at B , and thus, improving the transmit power at B may not be always an effective way to achieve a lower SOP. The increase in the ratio of T_1 to T_2 can alternatively achieve a lower SOP, instead of enhancing the transmit power at B . However, when α is large sufficiently, larger α will not achieve a much better SOP, because of the lower bound in (9).

The probability of non-zero secrecy capacity (PNSC) is another important secrecy performance metric, which can be

easily derived by using the expression for SOP,

$$\begin{aligned} \text{PNSC} &= \Pr\{C_s > 0\} = 1 - \text{SOP}|_{R_s=0} \\ &= \sum_{j_d=1}^L \sum_{j_e=1}^L a_{e,j_e} a_{d,j_d} (m_d - 1)! \\ &\quad \sum_{k=0}^{m_d-1} \frac{1}{k!} \frac{(m_e + k - 1)! \zeta_{d,j_d}^{-m_d+k}}{(\zeta_{e,j_e} + \zeta_{d,j_d})^{m_e+k}}, \end{aligned} \quad (11)$$

where the impact of $B - S$ link vanishes.

B. Effective Secrecy Throughput

Due to the fact that the CSI of $S - D$ link is available at S , S can adopt the maximal code rate (i.e., C_d) for the signal transmission to D , which is denoted as adaptive transmission scheme in the Subsection III-A of [16]. In this adaptive transmission scheme, the EST is defined as [16]

$$\begin{aligned} \Psi(R_e) &= (C_d - R_e) \Pr\{\gamma_e < 2^{R_e} - 1\} \\ &= (C_d - R_e) F_{g_{SE}}\left(\frac{g_{SD}}{\lambda}\right), \end{aligned} \quad (12)$$

where $\lambda = 2^{R_s}$, $F_{g_{SE}}(\cdot)$ denotes the CDF of g_{SE} , and the redundancy rate $R_e = C_d - R_s$ is used to secure message transmission against eavesdropping.

IV. ASYMPTOTIC ANALYSIS

The asymptotic behaviour over GK fading channels is normally complicated [14], because the diversity order of SOP in high SNRs in this work depends on k_d , m_d , k_s and m_s , and the asymptotic CDF for γ_D is not a line function with respect to $\log(\mu_d)$ for $k_d = m_d$ or $k_s = m_s$.

Here, we only consider a special case where the diversity order of $S - D$ link is less than that of $B - S$ link, i.e., $\min\{k_d, m_d\} < \min\{k_s, m_s\}$. When the average channel power gain of $S - D$ link (μ_d) approaches infinity, i.e., $\zeta_{d,j_d} \rightarrow 0$, the asymptotic PDF of g_{SD} is¹ [14]

$$f_{g_{SD}}^\infty(x) = \frac{\Gamma(|k_d - m_d|) (k_d m_d)^{v_d} x^{v_d-1}}{\Gamma(k_d) \Gamma(m_d) \mu_d^{v_d}} = \frac{\Delta x^{v_d-1}}{\mu_d^{v_d}}, \quad (13)$$

where $v_d = \min\{k_d, m_d\}$, and $k_d \neq m_d$.

The corresponding joint PDF of γ_D and γ_E becomes

$$\begin{aligned} f_{\gamma_D, \gamma_E}(x, y) &= \frac{\Delta}{\mu_d^{v_d}} \sum_{j_e=1}^L a_{e,j_e} \sum_{j_s=1}^L a_{s,j_s} \left(\frac{x}{\alpha}\right)^{v_d-1} \left(\frac{y}{\alpha}\right)^{m_e-1} \\ &\quad \frac{2}{\alpha^2} \left(\frac{\zeta_{e,j_e} y}{\alpha \zeta_{s,j_s}}\right)^{-\frac{v_d - m_e + m_s}{2}} K_{-v_d - m_e + m_s} \left(2\sqrt{\frac{\zeta_{s,j_s} \zeta_{e,j_e} y}{\alpha}}\right), \end{aligned} \quad (14)$$

where $K(\cdot)$ denotes the second modified bessel function [15].

By substituting the joint PDF into the SOP definition, SOP becomes (16), shown on the top of next page, where the integral can be derived in closed-form for $m_s > v_d$. When $m_s > v_d$, the asymptotic SOP (ASOP) in high SNRs can be derived as (17), shown on the top of next page, which shows that the diversity order is v_d .

Due to the page limitation, we only give some comments for ASOP in the general case. When $v_d > v_s$, where $v_s =$

$\min\{k_s, m_s\}$, the diversity order of ASOP is v_s . When $v_d > v_s$ and $k_s = m_s$ (or $v_d < v_s$ and $k_d = m_d$), the ASOP is not a line function with respect to $\log(\mu_d)$, although the diversity order is still v_s (or v_d). To summarize, the diversity order (O) of ASOP is

$$O = \begin{cases} v_d, & v_d \leq v_s; \\ v_s, & v_d > v_s. \end{cases} \quad (15)$$

This conclusion for the diversity order is also valid over Nakagami- m fading channels (no shadowing).

V. NUMERICAL RESULTS

Fig. 1 plots SOP versus μ_d for different k_d and m_d , where the decreasing trend of SOP is presented with μ_d (m_d or k_d) increasing, due to the improved $S - D$ link. This decreasing trend of SOP is also obvious in Fig. 2 as μ_e decreases, due to the worse $S - E$ link. The difference of the diversity order for different k_d and m_d is shown in the different slope in Figs. 1-2, where we only consider the case of $v_d < v_s$.

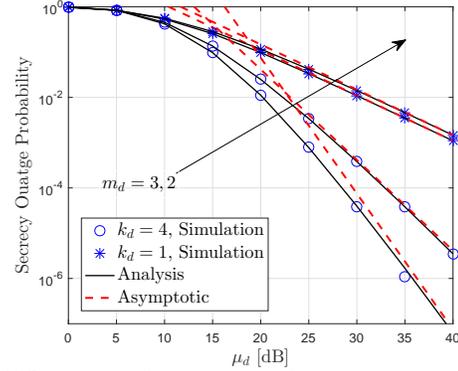


Fig. 1. SOP versus μ_d for $\mu_s = \mu_e = 1$, $k_e = k_s = 4$, $m_e = m_s = 4$, $P_B = 5$ dB, $T_1 = 1$, $T_2 = 2$, and $R_s = 2$.

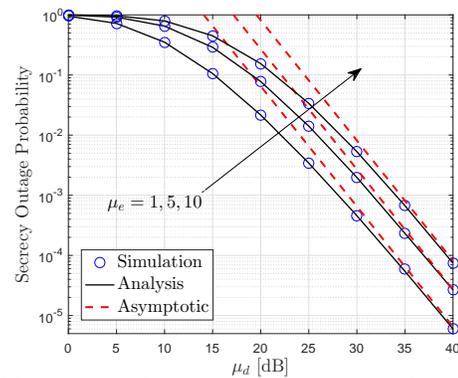


Fig. 2. SOP versus μ_d for $m_d = 2$, $m_e = m_s = 4$, $k_d = k_e = k_s = 3$, $P_B = 1$ dB, $T_1 = 1$, $T_2 = 2$, $\mu_s = 1$, and $R_s = 1$.

As presented in Fig. 3, we can see that SOP is in decline with α increasing, because the transmit power at B (or the ratio of T_1 to T_2) increases, resulting in the improved transmit power at S . However, when α is large sufficiently, there is no obvious improvement in SOP for a larger α , which means that the impact of $B - S$ link vanishes. The lower bound for SOP is smaller when the number of multi-path clusters becomes larger.

¹There is no asymptotic expression for $m_d = k_d$ [14], because the asymptotic CDF of g_{SD} is not a line function with respect to $\log(\mu_d)$, although the diversity order is still v_d .

$$\text{SOP}^\infty = \frac{\Delta}{\mu_d^{v_d}} \sum_{j_e=1}^L a_{e,j_e} \sum_{j_s=1}^L a_{s,j_s} \frac{2}{\alpha^{v_d+m_e+m_s}} \frac{1}{v_d} \left(\frac{\zeta_{e,j_e}}{\zeta_{s,j_s}} \right)^{\frac{-v_d-m_e+m_s}{2}} \int_0^\infty y^{-\frac{v_d+m_e+m_s}{2}-1} (\lambda-1+\lambda y)^{v_d} K_{-v_d-m_e+m_s} \left(2\sqrt{\frac{\zeta_{s,j_s} \zeta_{e,j_e} y}{\alpha}} \right) dy. \quad (16)$$

$$\text{SOP}^\infty = \left\{ \Delta \sum_{j_e=1}^L a_{e,j_e} \sum_{j_s=1}^L a_{s,j_s} \frac{\zeta_{e,j_e}^{-m_e} \zeta_{s,j_s}^{-m_s}}{\alpha^{v_d} v_d} \sum_{n=0}^{v_d} \binom{v_d}{n} (\lambda-1)^{v_d-n} \lambda^n \left(\frac{\alpha}{\zeta_{s,j_s} \zeta_{e,j_e}} \right)^n \Gamma(m_e+n) \Gamma(m_s-v_d+n) \right\} \mu_d^{-v_d}. \quad (17)$$

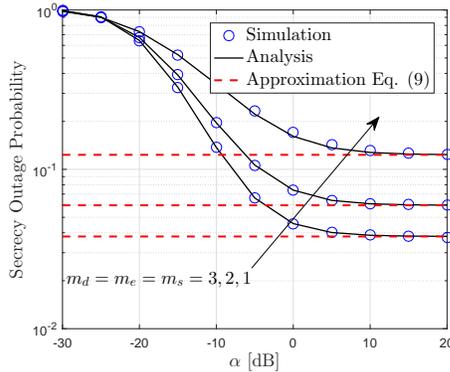


Fig. 3. SOP versus α for $k_d = k_e = k_s = 3$, $P_B = 1$ dB, $T_1 = 1$, $\mu_d = 10$, $\mu_e = \mu_s = 1$, and $R_s = 0.1$.

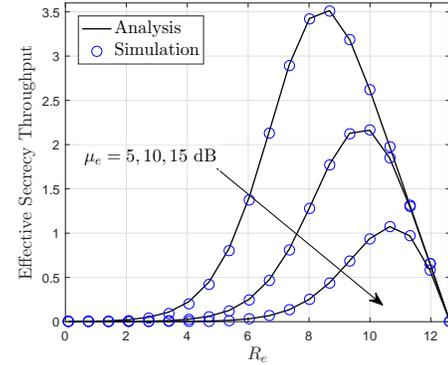


Fig. 5. EST versus R_e for $m_d = m_e = m_s = 2$, $k_d = k_e = k_s = 4$, $P_B = 10$ dB, $T_1 = 2$, $T_2 = 1$, $g_{SD} = 20$ dB, and $g_{BS} = 5$ dB.

The increasing trend of PNSC is shown in Fig. 4 as μ_d increases, because of the improved main link. In the low μ_d region, PNSC is reduced as $k_d = k_e = k_s$ increases, although the shadowing becomes lighter.

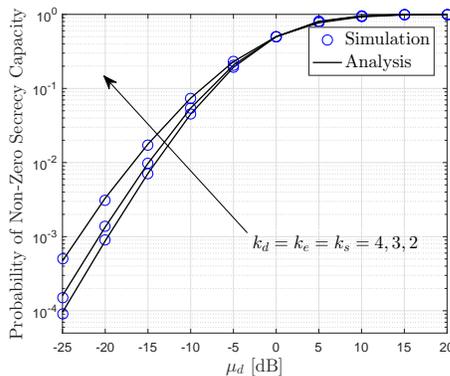


Fig. 4. PNSC versus μ_d for $m_d = m_e = m_s = 2$, $P_B = 5$ dB, $T_1 = 1$, $T_2 = 2$, $\mu_e = \mu_s = 1$, and $R_s = 1$.

As shown in Fig. 5, when R_e changes, there is a locally maximum point for EST, which becomes large for a large μ_e . It is also obvious that EST is a decreasing function with respect to μ_e , due to the improved wiretap channel.

REFERENCES

- [1] S. Sudevalayam and P. Kulkarni, "Energy harvesting sensor nodes: Survey and implications," *IEEE Commun. Surveys Tuts.*, vol. 13, no. 3, pp. 443-461, Oct. 2011.
- [2] R. Zhang, and C. K. Ho, "MIMO broadcasting for simultaneous wireless information and power transfer," *IEEE Trans. Wireless Commun.*, vol. 12, no. 5, pp. 1989-2001, May 2013.
- [3] M. Bloch, J. Barros, M. R. D. Rodrigues, and S. W. McLaughlin, "Wireless information-theoretic security," *IEEE Trans. Inf. Theory*, vol. 54, no. 6, pp. 2515-2534, Jun. 2008.
- [4] H. Zhao, Y. Tan, G. Pan, Y. Chen, and N. Yang, "Secrecy outage on transmit antenna selection/maximal ratio combining in MIMO cognitive radio networks," *IEEE Trans. Veh. Technol.*, vol. 65, no. 12, pp. 10236-10242, Dec. 2016.
- [5] G. Pan, C. Tang, T. Li, and Y. Chen, "Secrecy performance analysis for SIMO simultaneous wireless information and power transfer systems," *IEEE Trans. Commun.*, vol. 63, no. 9, pp. 3423-3433, Sep. 2015.
- [6] G. Pan, H. Lei, Y. Deng, L. Fan, J. Yang, Y. Chen, and Z. Ding, "On secrecy performance of MISO SWIPT systems with TAS and imperfect CSI," *IEEE Trans. Commun.*, vol. 64, no. 9, pp. 3831-3843, Sep. 2016.
- [7] G. Pan, J. Ye, and Z. Ding, "Secure hybrid VLC-RF systems with light energy harvesting," *IEEE Trans. Commun.*, vol. 65, no. 10, pp. 4348-4359, Oct. 2017.
- [8] G. Pan, C. Tang, X. Zhang, T. Li, Y. Weng, and Y. Chen, "Physical-layer security over non-small-scale fading channels," *IEEE Trans. Veh. Technol.*, vol. 65, no. 3, pp. 1326-1339, Mar. 2016.
- [9] P. S. Bithas, N. C. Sagias, P. T. Mathiopoulos, G. K. Karagiannidis, and A. A. Rontogiannis, "On the performance analysis of digital communications over generalized- K fading channels," *IEEE Commun. Lett.*, vol. 10, no. 5, pp. 353-355, May 2006.
- [10] H. Lei, H. Zhang, I. S. Ansari, G. Pan, and K. A. Qaraqe, "Secrecy outage analysis for SIMO underlay cognitive radio networks over generalized- K fading channels," *IEEE Signal Process. Lett.*, vol. 23, no. 8, pp. 1106-1110, Aug. 2016.
- [11] S. Atapattu, C. Tellambura, and H. Jiang, "A mixture Gamma distribution to model the SNR of wireless channels," *IEEE Trans. Wireless Commun.*, vol. 10, no. 12, pp. 4193-4203, Dec. 2011.
- [12] H. Lei, C. Gao, I. S. Ansari, Y. Guo, G. Pan, and K. A. Qaraqe, "On physical-layer security over SIMO generalized- K fading channels," *IEEE Trans. Veh. Technol.*, vol. 65, no. 9, pp. 7780-7785, Sep. 2016.
- [13] H. Lei, H. Zhang, I. S. Ansari, C. Gao, Y. Guo, G. Pan, and K. A. Qaraqe, "Performance analysis of physical layer security over generalized- K fading channels using a mixture Gamma distribution," *IEEE Commun. Lett.*, vol. 20, no. 2, pp. 408-411, Feb. 2016.
- [14] H. Y. Lateef, M. Ghogho, and D. McLernon, "On the performance analysis of multi-hop cooperative relay networks over generalized- K fading channels," *IEEE Commun. Lett.*, vol. 15, no. 9, pp. 968-970, Sep. 2011.
- [15] I. S. Gradshteyn and I. M. Ryzhik, *Table of Integrals, Series and Products*, 7th ed., Academic, San Diego, C.A., 2007.
- [16] S. Yan, N. Yang, G. Geraci, R. Malaney, and J. Yuan, "Optimization of code rates in SISOME wiretap channels," *IEEE Trans. Wireless Commun.*, vol. 14, no. 11, pp. 6377-6388, Nov. 2015.