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## Enhancing Temperature Stability in Potassium-Sodium Niobate Ceramics through Phase Boundary and Composition Design

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**Abstract:** Phase boundaries and composition design were explored to achieve both high piezoelectricity and favorable temperature stability in potassium-sodium niobate ceramics, using  $(1-x)(\text{K},\text{Na})(\text{Nb},\text{Sb})\text{O}_3-x\text{Bi}(\text{Na},\text{K})(\text{Zr},\text{Sn},\text{Hf})\text{O}_3$  ceramics. A rhombohedral-tetragonal (R-T) phase boundary was constructed at  $x=0.035-0.04$  by co-doping with  $\text{Sb}^{5+}$  and  $\text{Bi}(\text{Na},\text{K})(\text{Zr},\text{Sn},\text{Hf})\text{O}_3$ . More importantly, a superior temperature stability was observed in the ceramics with  $x=0.035$ , accompanying with a stable unipolar strain at room temperature to 100 °C. The ceramics with  $x=0.035$  also exhibited improved piezoelectric properties (e.g., piezoelectric coefficient  $d_{33}\sim 465$  pC/N and electromechanical coupling factor  $k_p=0.47$ ) and Curie temperature ( $T_c\sim 240$  °C). The Rietveld refinement and *in-situ* temperature-dependent piezoresponse force microscopy (PFM) results indicated that the enhancement of the

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piezoelectric properties was caused by the easy domain switching, high tetragonal fraction, and tetragonality, while the improved temperature stability mainly originated from the stable domain structures.

abbreviation:  $I_{002}$ ) was obviously higher (two times stronger) than that of  $(200)_{pc}$  (abbreviation:  $I_{200}$ ), suggesting the existence of an orthorhombic (O) phase [24]. As  $x$  increased, the intensities of these two peaks varied oppositely, i.e.,  $I_{002}$  decreased when  $I_{200}$  increased, suggesting that the tetragonal (T) phase gradually dominated [25]. In the ceramics with  $x=0.05$ , a ratio of 2:1 between  $I_{200}$  and  $I_{002}$  was observed, indicating a dominant T phase. Fig. 2(c) shows the enlarge XRD patterns of 0.965KNNS-0.035BNKM (M=Zr, Hf, and Sn) ceramics. 0.965KNNS-0.035BNKM (M=Zr and Hf) ceramics exhibited a phase structure similar to that of 0.965KNNS-0.035BNKZSH ceramics, while 0.965KNNS-0.035BNKS ceramics showed a single peak in the  $2\theta$  range of  $44-47^\circ$ , indicating the existence of a pseudocubic phase [26]. Hence, it is necessary to further analyze the phase structure of each component, for example the permittivity against temperature ( $\epsilon_r-T$ ) curves.

**Keywords:** Lead-free ceramics; Temperature stability; KNN; R-T phase boundary

## 1. Introduction

Potassium-sodium niobate (KNN)-based lead-free ceramics have been extensively investigated in last two decades as one of the most promising candidates to replace the environmentally harmful lead-based piezoelectric materials in electronic devices [1-3]. However, lead-based piezoelectric ceramics still outperform those based on KNN in terms of piezoelectricity and temperature stability, the key parameters determining the overall performance of a piezoelectric material [1-3]. Studies show that it is

difficult to achieve high piezoelectricity and temperature stability simultaneously in KNN-based ceramics [4]. Different strategies, such as engineering phase boundaries, new sintering methods, etc., have been employed to meet the requirements of practical applications [4].

Among these strategies, engineering the phase boundary is the most promising to simultaneously achieve high piezoelectricity and good temperature stability in KNN-based ceramics [4]. In 2004, Saito *et al.* reported a large  $d_{33}$  (~416 pC/N) and a high  $T_c$  (~253 °C) in highly textured LF4T ceramics that possessed an orthorhombic-tetragonal (O-T) phase boundary [5]. The excellent temperature stability observed in these textured LF4T ceramics was comparable to that of commercial lead-based PZT-4 ceramics [5]. Although the highly textured LF4T ceramics satisfying the practical applications were synthesized by the high cost reactive template grain growth (RTGG) method, the results ignited the researchers' passion of studying KNN-based ceramics, particularly the construction of phase boundary [4]. Among the different phase boundaries, e.g., rhombohedral-orthorhombic (R-O), O-T, and rhombohedral-tetragonal (R-T), the R-T phase boundary is the most effective for enhancing the temperature stability and piezoelectricity of KNN-based ceramics [6-8].

Recent studies have shown that, in addition to the phase boundary, composition design also significantly affects the temperature stability and piezoelectric properties of KNN-based ceramics with an R-T phase boundary [9,10]. For example, in  $0.96(\text{K,Na})(\text{Nb,Sb})\text{O}_3-0.04(\text{Bi,K})(\text{Zr,Sn})\text{O}_3$  ceramics with an R-T phase boundary and a high  $d_{33}$  of 430 pC/N, the unipolar strain declined from 0.14% to 0.09% (variation less than 40%) as temperature increased from room temperature to 190 °C [9].

However, the ceramics with a different composition of  $(\text{K,Na})\text{NbO}_3-(\text{Bi,Li})\text{TiO}_3-\text{BaZrO}_3$  and a moderate  $d_{33}$  of 348 pC/N, the unipolar strain reduced more than 45%

as temperature increased from 30 °C to 200 °C [10]. Therefore, the R-T phase boundary and composition design are both critical to the overall performance of KNN-based lead-free ceramics [6-10].

Experiments have demonstrated that KNN-based ceramics must be doped with additives in order to construct the R-T phase boundary at or near room temperature by elevating the R-O phase transition temperature ( $T_{R-O}$ ) and decreasing the O-T phase transition temperature ( $T_{O-T}$ ) [4]. For instance, the addition of  $Sb^{5+}$ ,  $Bi_{0.5}Na_{0.5}ZrO_3$ , or  $Bi_{0.5}Na_{0.5}HfO_3$  simultaneously increases the  $T_{R-O}$  and reduces the  $T_{O-T}$  of KNN-based ceramics [4,11-13]. Recently, the addition of  $Sn^{4+}$  was reported to greatly improve the piezoelectric properties of barium titanate ( $BaTiO_3$ , BT) based ceramics [14-16].

More encouragingly, the giant  $d_{33}$  values of 500-697 pC/N were achieved by substituting  $Ti^{4+}$  with  $Sn^{4+}$  in BT-based ceramics [14-16]. Experiments proved that the addition of  $Sn^{4+}$  could quickly construct the phase coexistence and increase the diffuseness of phase transition, resulting in the ultrahigh dielectric and piezoelectric properties in  $Ba(Ti,Sn)O_3$  ceramics [14-16]. Moreover, it is worth noting that the increased diffuseness of phase transition could also enhance the temperature stability [17]. Motivated by the above successes, both improved piezoelectricity and favorable temperature stability are highly anticipated in KNN-based ceramics using  $Sn^{4+}$  substitution.

In this work, we developed a new additive,  $Bi_{0.5}(Na_{0.5}K_{0.5})_{0.5}Zr_{0.8}Sn_{0.1}Hf_{0.1}O_3$ , with the purpose of simultaneously enhancing piezoelectricity and temperature stability of KNN-based ceramics. Our design was inspired by the outstanding performance of  $Sn^{4+}$  substitution in BT-based, particularly the ultrahigh piezoelectric properties and increased diffuseness of phase transition. In addition, the similar ionic radii of  $Zr^{4+}$ ,  $Hf^{4+}$ , and  $Sn^{4+}$  ions (CN=6,  $r_{Zr}=0.072nm$ ,  $r_{Hf}=0.071nm$ , and  $r_{Sn}=0.069nm$ ) could

guarantee the sinterability of KNN-based ceramics [18], which further manifested the reliability of designed additive. In this work, we synthesized (1- $x$ )(K<sub>0.5</sub>Na<sub>0.5</sub>)(Nb<sub>0.955</sub>Sb<sub>0.045</sub>)O<sub>3</sub>- $x$ Bi<sub>0.5</sub>(Na<sub>0.5</sub>K<sub>0.5</sub>)<sub>0.5</sub>Zr<sub>0.8</sub>Sn<sub>0.1</sub>Hf<sub>0.1</sub>O<sub>3</sub> {(1- $x$ )KNNS- $x$ BNKZSH} ceramics using the conventional solid-state reaction method. Our results showed that co-doping with Sb<sup>5+</sup> and BNKZSH simultaneously improved the electrical properties of the KNN-based ceramics and guaranteed good temperature stability.

## 2. Experimental procedure

In this work, (1- $x$ )KNNS- $x$ BNKZSH ( $x=0.01-0.05$ ) ceramics were fabricated by the conventional solid-state method. For comparison, 0.965KNNS-0.035BNKM (M=Zr, Hf, and Sn) ceramics were also prepared. The raw materials were K<sub>2</sub>CO<sub>3</sub> (99%), Na<sub>2</sub>CO<sub>3</sub> (99.8%), Nb<sub>2</sub>O<sub>5</sub> (99.5%), Bi<sub>2</sub>O<sub>3</sub> (99.999%), Sb<sub>2</sub>O<sub>3</sub> (99.99%), HfO<sub>2</sub> (99.9%), and SnO<sub>2</sub> (99.5%) (Sinopharm Chemical Reagent Co., Ltd, CN). Mixtures of the raw materials with the designed compositions were ball-milled for 24 h with zirconia ball media and alcohol in plastic jars. Then, the dried slurry was calcined at 850 °C for 6 h. The calcined powder was pressed into disks of 10 mm diameter and 1 mm thickness under 10 MPa using PVA as a binder. After burning off the PVA at 500 °C, the disks were sintered at 1060-1120 °C for 3 h under a corundum crucible in air.

The structures of the ceramics were explored using X-ray diffraction (XRD) characterization (Bruker D8 Advanced XRD, Bruker AXS Inc., Madison, WI, CuK<sub>α</sub>).

For the Rietveld refinement, a high-resolution XRD instrument, X' Pert Pro MPD (DY 120 PANalytical, Netherlands), was used to collect the XRD data from the polished and annealed samples. The Maud software package and KNbO<sub>3</sub> mode was used to perform the Rietveld refinement. The parameters that were considered for

Rietveld refinement were lattice parameters, atomic positions, crystalline sizes, structural factors and phase fraction [19]. The temperature-dependent Raman spectra were measured using a Horiba Aramis Raman spectrometer (Horiba Scientific, France) with an excitation source of 473 nm. The temperature was controlled by a Linkam cell (Linkam Scientific Instruments, UK).

To characterize the electric properties of the materials, silver paste was printed on both sides of the as-sintered disks, which were then baked at 600 °C for 30 min to form reliable electrodes. Then, the disks were poled at room temperature in a silicone oil bath by applying an electric field of 4 kV/mm for 30 min. After aging for 24 h, the  $d_{33}$  values of the poled disks were measured using a quasi-static piezo- $d_{33}$  meter (ZJ-3 A, China), and the  $k_p$  values were measured using an impedance analyzer (HP 4299A, Palo Alto, CA). The polarization-electric field ( $P$ - $E$ ) loops and strain-electric field ( $S$ - $E$ ) curves were measured using a ferroelectric analyzer (aixACCT TF Analyzer 2000, Germany) with a laser interferometer vibrometer (SP-S120/500, sios Mebtechnik GmbH, Germany), at a frequency of 1 Hz. The room-temperature permittivity ( $\epsilon_r$ ) and loss factor ( $\tan \delta$ ) were measured using an LCR meter (Agilent 4294, USA) at a frequency of 10 kHz. The temperature dependence of  $\epsilon_r$  was measured using a broadband dielectric spectrometer (Novocontrol Technologies GmbH, Germany).

The as-sintered samples were broken into two pieces. The cross-section of sample was mechanically polished and then thermally etched at a temperature that is lower 100 °C than sintering temperature for 15 min. Field emission scanning electron microscopy (FE-SEM, JSM-7500F, Hitachi, Japan) was used to observe the morphologies of thermally etched cross-section and perform the energy dispersive spectroscopy (EDS) analysis. To perform the piezoresponse force microscopy (PFM), the as-sintered disks were mechanically polished to a thickness of about 20  $\mu\text{m}$ . The

PFM observations were conducted on a commercial atomic force microscope (MFP-3D, Asylum Research, Goleta, CA) with a conductive Pt-Ir-coated cantilever PPP-NCHPt (Nanosensors, Switzerland). To write the domains, the selected areas were poled at a bias voltage of  $\pm 10$  V to completely switch the surface domains. Both the piezoresponse and phase images were recorded by applying an AC voltage (i.e.,  $U_{ac}=\pm 1$  V and  $f_{ac}=50$  kHz). The *in situ* temperature-dependent piezoresponse images and phase images were recorded by applying an AC voltage (i.e.,  $U_{ac}=\pm 1$  V and  $f_{ac}=50$  kHz) at different temperatures.

The *ab initio* calculations were carried out using the CASTEP program (Dassault Systèmes BIOVIA) [20]. The generalized gradient approximation (GGA) of Perdew, Burke, and Ernzerhof (PBE) was used to determine the exchange-correlation potential. The cut-off energy was set to 660 eV and the Brillouin zone was sampled using a  $6\times 6\times 6$  Monkhorst-Pack grid. For each phase, the experimental lattice constant of the  $(K_{0.5}Na_{0.5})NbO_3$  cell was fixed while the atomic sites were fully relaxed to a force tolerance of 0.01 eV/Å. The virtual crystal approximation (VCA) method was utilized to simulate the real atom distribution in the disordered crystals [21].

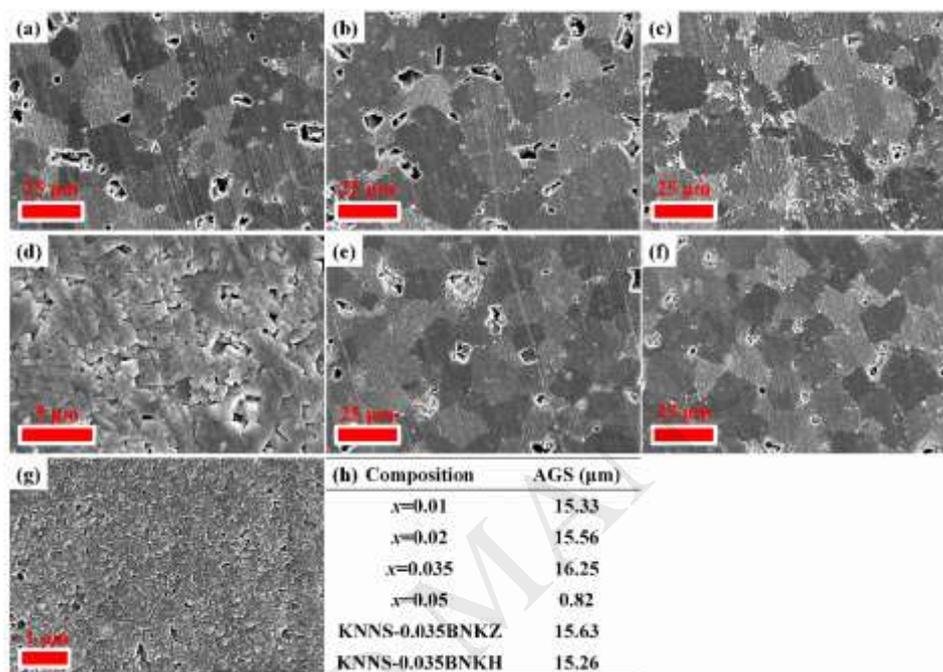
### 3. Results and discussion

Figs. 1(a)-(d) show the FE-SEM images of polished and thermally etched cross-sections of  $(1-x)KNNS-xBNKZSH$  ceramics. Except for the ceramics with  $x=0.05$ , all other compositions showed a bimodal distribution containing “large” and “small” grains, and the grain sizes of the ceramics depended strongly on the doping contents. Some pores occurred in the ceramics with  $x=0.01-0.02$  [Figs. 1(a) and (b)], which were easily found in lead-free ceramics due to the different growth rates in samples

[22]. Therefore, these pores were responsible for the relatively low density [see Table S1 in Supporting Information]. As  $x$  increased up to 0.035, the relatively dense cross-section was observed, as shown in Fig. 1(c). Thus, the appropriate addition of BNKZSH could promote the density of KNN-based ceramics, as proved by increased relative density [see Table S1 in Supporting Information]. Furthermore, some small grains were also found to attach to the large grains [Fig. 1(c)], indicating the promoted bimodal distribution. The enlarged view of small grains can be clearly seen in Figure S1(c) [see Supporting Information]. While the ultra-fine grains were observed in the ceramics with  $x=0.05$ , probably owing to the excess addition of additive (i.e., BNKZSH) that gathered at the grain boundaries and hindered grain growth [23]. Fig. 1(h) shows the evolution of average grain size (AGS) of  $(1-x)\text{KNNS}-x\text{BNKZSH}$  ceramics varying with  $x$ . The detailed statistics of grain size distribution were shown in Figure S1 [Supporting Information]. With an increase of  $x$ , AGS firstly increased slightly at  $x=0.01-0.035$ , and then reduced sharply at  $x=0.035-0.05$ .

Figs. 1(e)-(g) display the FE-SEM images of polished and thermally etched cross-sections of  $0.965\text{KNNS}-0.035\text{BNKM}$  ( $M=\text{Zr}$ ,  $\text{Hf}$ , and  $\text{Sn}$ ) ceramics. It was found that  $0.965\text{KNNS}-0.035\text{BNKM}$  ( $M=\text{Zr}$  and  $\text{Hf}$ ) ceramics exhibited the similar cross-section morphology with respect to that of  $(1-x)\text{KNNS}-x\text{BNKZSH}$  ceramics with  $x=0.01-0.02$ . Therefore, these compositions exhibited the similar AGS [Fig. 1(h)]. While  $0.965\text{KNNS}-0.035\text{BNKM}$  ( $M=\text{Zr}$  and  $\text{Hf}$ ) ceramics exhibited the slightly higher density than those of  $(1-x)\text{KNNS}-x\text{BNKZSH}$  ceramics with  $x=0.01-0.02$ , owing to less pores [see Table S1 in Supporting Information]. However, no clear grain boundaries could be observed in  $0.965\text{KNNS}-0.035\text{BNKS}$  ceramics [Fig. 4(g)]. The similar phenomenon was also reported in other KNN-based ceramics with a high  $\text{Sn}^{4+}$  concentration [23]. Considering the abnormal grains in  $0.965\text{KNNS}-0.035\text{BNKS}$

ceramics, the EDS analysis was performed to check the element distribution [see Figures S2 and S3 in Supporting Information]. The results demonstrated that all elements exhibited a homogeneous distribution, manifesting that  $\text{Sn}^{4+}$  completely diffused into the crystal lattice of the KNN-based ceramics instead of forming other secondary phases.

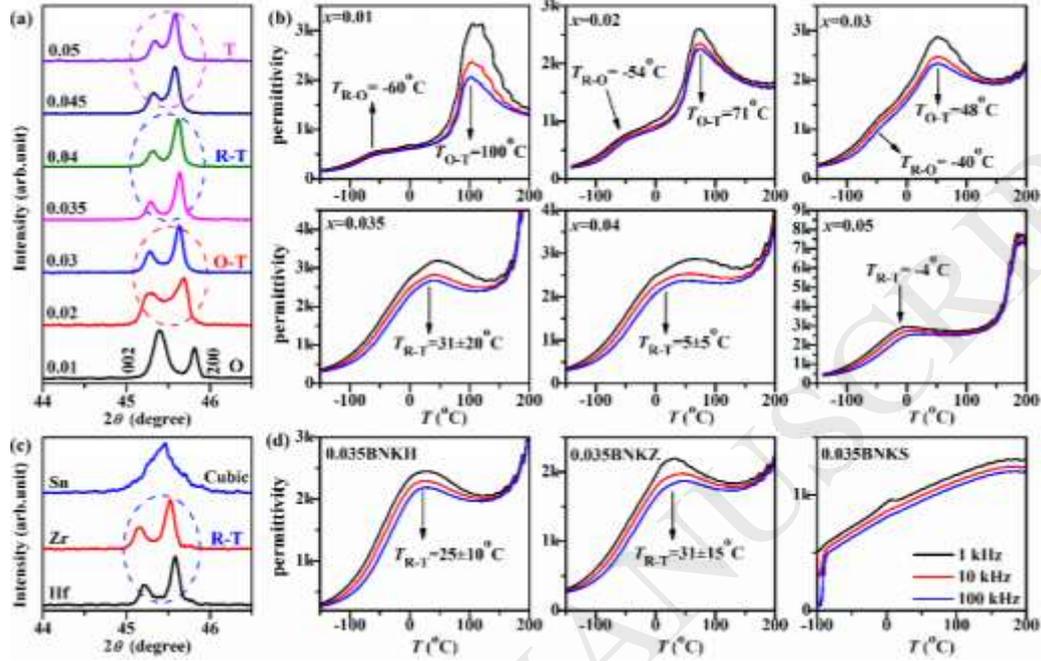


**Figure 1.** FE-SEM images of polished and thermally etched cross-sections of KNNS- $x$ BNKZSH ceramics with (a)  $x=0.01$ , (b)  $x=0.02$ , (c)  $x=0.035$ , (d)  $x=0.05$ , and 0.965KNNS-0.035BNKM ceramics with (e) M=Zr, (f) M=Hf and (g) M=Sn. (h) Average grain size (AGS) of the ceramics in this work.

A typical and pure perovskite structure was observed in all of the samples [see Figure S1 in Supporting Information]. Figs. 2(a) and (c) display the enlarged XRD patterns for  $2\theta=44-46^\circ$ . The phase structure of the ceramics was strongly dependent on the additive content. For  $(1-x)\text{KNNS}-x\text{BNKZSH}$  ceramics with  $x=0.01$ , the peak intensity of  $(002)_{\text{pc}}$  (Figs. 2(b) and (d) show the  $\varepsilon_r-T$  curves of the ceramics. The addition of  $\text{Sb}^{5+}$ ,  $\text{Bi}_{0.5}\text{Na}_{0.5}\text{ZrO}_3$ , or  $\text{Bi}_{0.5}\text{Na}_{0.5}\text{HfO}_3$  increased the  $T_{\text{R-O}}$  and decreased the  $T_{\text{O-T}}$  of

(1-x)KNNS-xBNKZSH ceramics, in agreement with the results reported previously [11-13]. For the  $x=0.01$  ceramics, the  $T_{R-O}$  and  $T_{O-T}$  values were identified as  $-60\text{ }^{\circ}\text{C}$  and  $100\text{ }^{\circ}\text{C}$ , respectively, indicating the existence of a single O phase at room temperature. As  $x$  increased up to 0.02 and 0.03,  $T_{R-O}$  rose to  $-54\text{ }^{\circ}\text{C}$  and  $-40\text{ }^{\circ}\text{C}$ , respectively, and  $T_{O-T}$  dropped to  $71\text{ }^{\circ}\text{C}$  and  $48\text{ }^{\circ}\text{C}$ , respectively. For the ceramics with  $x=0.02$ , its  $T_{R-O}$  value was more far away from room temperature than that of  $T_{O-T}$  value. Furthermore,  $I_{200}$  of the ceramics with  $x=0.02$  was obviously higher than  $I_{002}$ , suggesting the involvement of T phase [27]. Thus, it can be inferred that the ceramics with  $x=0.02$  possessed an O-T phase at room temperature [27]. For the ceramics with  $x=0.03$ , its  $T_{R-O}$  value was much lower than room temperature, while the  $T_{O-T}$  value was slightly above room temperature, indicating an O-T phase coexistence at room temperature [27]. As  $x$  further increased up to 0.035,  $T_{R-O}$  and  $T_{O-T}$  overlapped with each other, leading to the formation of an R-T phase boundary at  $T_{R-T}$  [23,25,26]. The  $T_{R-T}$  of the ceramics with  $x=0.035$  and 0.04 was very near room temperature at  $31\pm 20\text{ }^{\circ}\text{C}$  and  $5\pm 5\text{ }^{\circ}\text{C}$ , respectively, suggesting the coexistence of the R and T phases at the room temperature [23,25,26]. For the ceramics with  $x=0.05$ , its  $T_{R-T}$  of  $-4\text{ }^{\circ}\text{C}$  was much lower than room temperature. Therefore, only a single T phase should be seen in the ceramics with  $x=0.05$  at room temperature. From the  $\varepsilon_r$ - $T$  curves shown in Fig. 2(d), the values of  $T_{R-T}$  were identified as  $31\pm 15\text{ }^{\circ}\text{C}$  and  $25\pm 10\text{ }^{\circ}\text{C}$  for  $M=\text{Zr}$  and  $\text{Hf}$ , respectively, in the 0.965KNNS-0.035BNKM ceramics. Since the  $T_{R-T}$  values of these two compositions were very close to room temperature, both the R and T phases should coexist at room temperature. It is worth noting that the  $T_{R-T}$  ranges of these two compositions were slightly narrower with respect to that of 0.965KNNS-0.035BNKZSH ceramics, indicating that  $\text{Sn}^{4+}$  substitution could also enhance the diffuse nature of phase transition of KNN-based ceramics [14-16]. However, no

anomalies were observed in the  $\epsilon_r$ - $T$  curves of 0.965KNNS-0.035BNKS ceramics [Fig. 2(d)], which further confirmed that 0.965KNNS-0.035BNKS ceramics exhibited a pseudocubic phase [23].



**Figure 2.** Enlarged XRD patterns of (a)  $(1-x)$ KNNS- $x$ BNKZSH ceramics and (c) 0.965KNNS-0.035BNKM (M=Hf, Zr, and Sn) ceramics with  $2\theta=44-46^\circ$ ; and the  $\epsilon_r$ - $T$  (-150  $^\circ\text{C}$ -200  $^\circ\text{C}$ ) curves of (b)  $(1-x)$ KNNS- $x$ BNKZSH and (d) 0.965KNNS-0.035BNKM (M=Hf, Zr, and Sn) ceramics. The enlarged XRD patterns were indexed according to the pseudo-cubic phase structure axes.

Raman experiments, which are highly sensitive to changes in crystal structure, were performed to further analyze the phase transition [28]. Fig. 3(a) shows the temperature-dependent Raman spectra of 0.965KNNS-0.035BNKZSH ceramics. The vibrations of  $\text{NbO}_6$  octahedra have six modes,

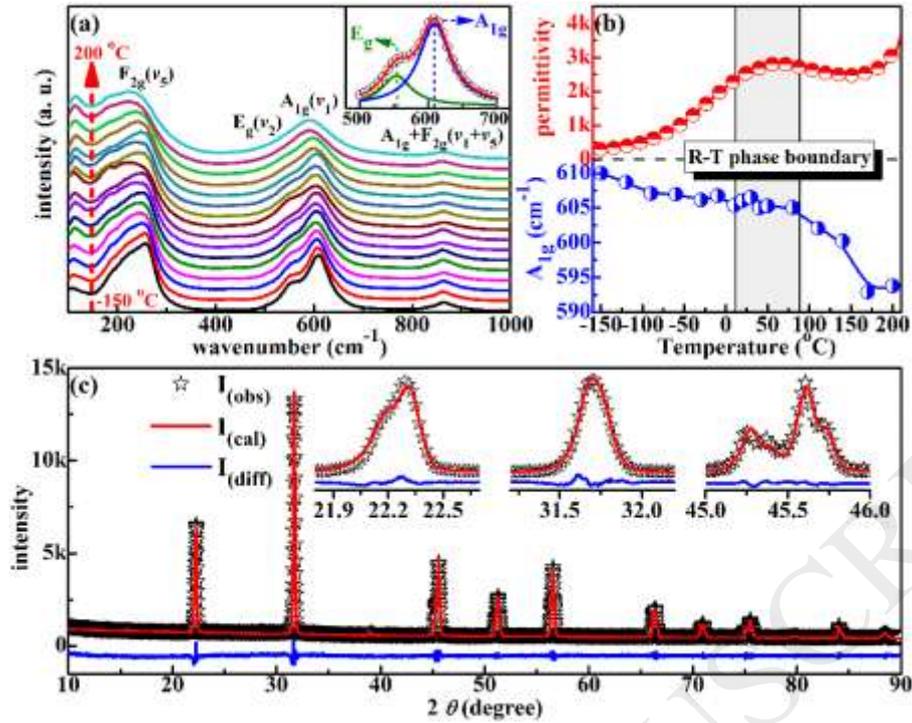
$1A_{1g}(\nu_1)+1E_g(\nu_2)+2F_{1u}(\nu_3,\nu_4)+F_{2g}(\nu_5)+F_{2u}(\nu_6)$ , where the stretching modes are  $1A_{1g}(\nu_1)+1E_g(\nu_2)+1F_{1u}(\nu_3)$ , and the rest are bending modes [28]. The  $\nu_1$  mode, which represents a double degenerate symmetric O-Nb-O stretching vibration, is generally

employed to analyze phase transitions in KNN-based ceramics [29]. Here, the spectra within the range of 500-700  $\text{cm}^{-1}$  were fitted to extract the shift of the  $\nu_1$  mode using Lorentz fitting, as shown in the inset of Fig. 3(a) [29]. To clearly show the correlation between the structure and the properties of the ceramics, the Raman shift of the  $\nu_1$  mode and the  $\epsilon_r$ - $T$  curve were plotted together in Fig. 3(b). As the temperature increased from -150 °C to 200 °C, the  $\nu_1$  mode shifted to the lower wavenumber first, and then remained nearly unchanged, forming a plateau in the temperature range  $0\text{ }^\circ\text{C} \leq T \leq 75\text{ }^\circ\text{C}$ . As the temperature increased further, the  $\nu_1$  mode shifted sharply to a lower wavenumber. This abrupt variation was also observed in KNN-LT ceramics [30]. Moreover, the R-T phase boundary observed in both the  $\epsilon_r$ - $T$  curve ( $T_{\text{R-T}}=31 \pm 20\text{ }^\circ\text{C}$ ) [Fig. 2(b)] and the Raman spectra (0 °C-75 °C) [Fig. 3(b)] was inferred to be a gradual phase transition (i.e., a diffused phase boundary) rather than an abrupt one [25]. Therefore, the experiments manifested that the addition of  $\text{Sn}^{4+}$  into KNN-based did construct the diffuse R-T phase boundary, further demonstrating the reliability of our design as mentioned above. Such a diffuse phase boundary highly suggested the possibility of good piezoelectricity and favorable temperature stability [17].

To further prove the existence of the R-T phase boundary, Rietveld refinements of 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, and Hf} ceramics were also carried out. Fig. 3(c) shows the Rietveld refinement of 0.965KNNS-0.035BNKZSH ceramics. The Rietveld refinements of other two compositions were shown in Figures S5 (a-d) [see Supporting Information]. A good match between original data and fitting one was clearly observed, indicating the decent refinement process [Fig. 3(c)]. The detailed refinement results are listed in Table 1. Low values of  $R_w$  (<6.5%) and Sig (<1.6) further guaranteed the reliability of Rietveld refinements [31]. The space groups,  $R3m$  and  $P4mm$ , respectively correspond to the R and T phases, demonstrating the

existence of R-T phase boundary. Moreover, an appreciable difference in the phase ratio was observed among these ceramics, which will be discussed to explain the difference of piezoelectricity among these compositions.

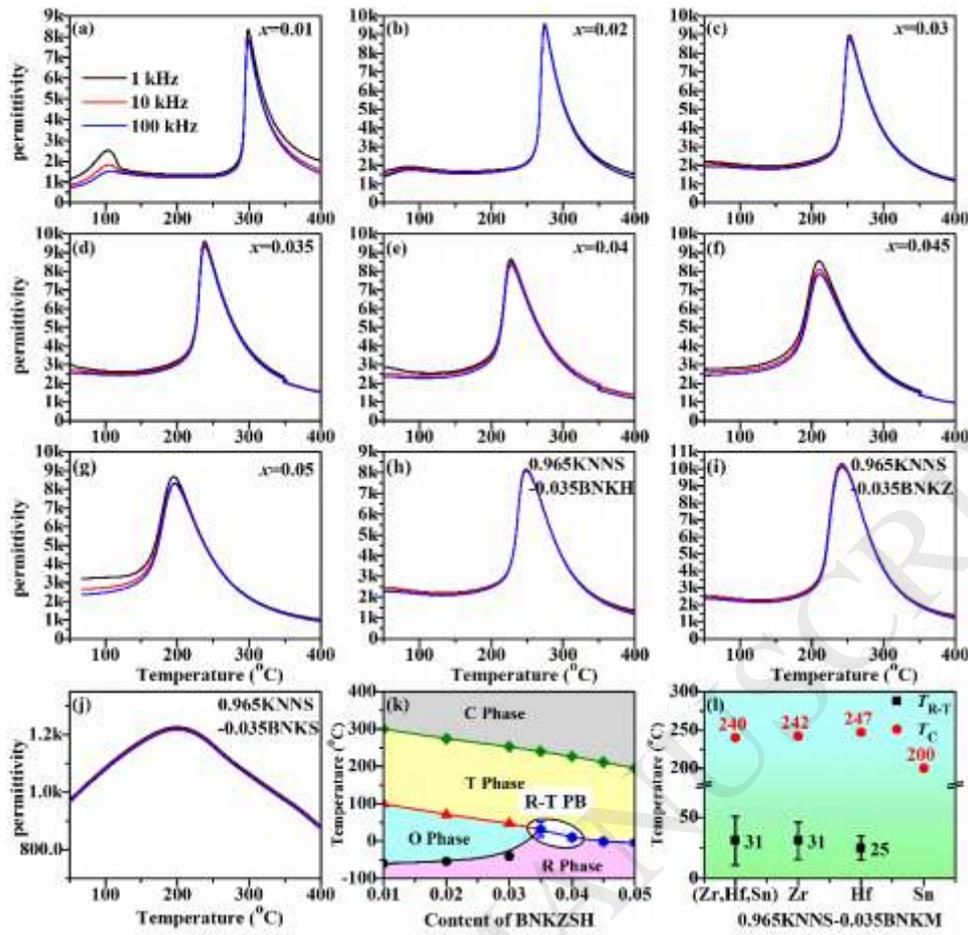
Previously, the flat Gibbs free energy could induce the easy polarization rotation, which accounted for the high piezoelectricity in lead-based piezoelectric ceramics with multiphase coexistence [32]. Here, the energy difference of the R-T phase boundary ( $\Delta U_{R-T}$ ) was calculated using the  $(K_{0.5}Na_{0.5})NbO_3$  mode with the lattice parameters listed in Table 1. The detailed energy value of each phase is listed in Table S2 [see Supporting Information]. The 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, and Hf} ceramics possessed ultralow  $\Delta U_{R-T}$  values of 2.9-5.5 meV. Previously, Cohen *et al.* calculated the energy difference between the R and T phases in  $BaTiO_3$  as  $\Delta U=6.42$  meV [33]. Yao *et al.* reported an R-T phase coexistence in  $(1-x)KNNS-xBNKZ$  ( $0.04 \leq x \leq 0.05$ ) thin films that exhibited an energy difference of  $E_{T-R}=0-0.02$  eV [34]. The ultralow value of  $\Delta U_{R-T}$  obtained in this work is comparable to these previous results, indicating a stable coexistence of the R and T phases. All of our results, from the XRD patterns,  $\epsilon_r-T$  curves, temperature-dependent Raman spectra, and Rietveld refinement, confirmed the existence of an R-T phase boundary.



**Figure 3.** (a) Temperature-dependent Raman spectra of 0.965KNNS-0.035BNKZSH ceramics at different temperatures and fitting of Raman spectrum at  $T=-150$  °C in the wavenumber range of  $500-700$   $\text{cm}^{-1}$ . (b) Raman shift of  $A_{1g}(v_1)$  mode and permittivity of 0.965KNNS-0.035BNKZSH ceramics as a function of temperature. (c) Rietveld refinement of 0.965KNNS-0.035BNKZSH ceramics.

Figs. 4(a-g) and 4(h-j) show the  $\epsilon_r$ - $T$  curves of  $(1-x)\text{KNNS}-x\text{BNKZSH}$  and  $0.965\text{KNNS}-0.035\text{BNKM}$   $\{M=\text{Hf}, \text{Zr}, \text{and Sn}\}$  ceramics, respectively. Previous results showed that the addition of  $\text{Sb}^{5+}$ ,  $\text{Bi}_{0.5}\text{Na}_{0.5}\text{ZrO}_3$ , or  $\text{Bi}_{0.5}\text{Na}_{0.5}\text{HfO}_3$  decreased the  $T_c$  of KNN-based ceramics [11-13]. Although the  $T_c$  of the ceramics in this work also gradually reduced as the BNKZSH content increased,  $T_c$  was still about  $240$  °C at  $x=0.035$ . The  $T_c$  of  $0.965\text{KNNS}-0.035\text{BNKM}$   $\{M=(\text{Hf}, \text{Zr}, \text{Sn}), \text{Zr}, \text{Hf}, \text{and Sn}\}$  ceramics was indeed governed by the doping elements [Figs. 4(d) and (h-j)], i.e.,  $0.965\text{KNNS}-0.035\text{BNKM}$   $\{M=(\text{Hf}, \text{Zr}, \text{Sn}), \text{Zr}, \text{and Hf}\}$  ceramics have a relatively high  $T_c$  in the range of  $240-247$  °C, while  $0.965\text{KNNS}-0.035\text{BNKS}$  ceramics

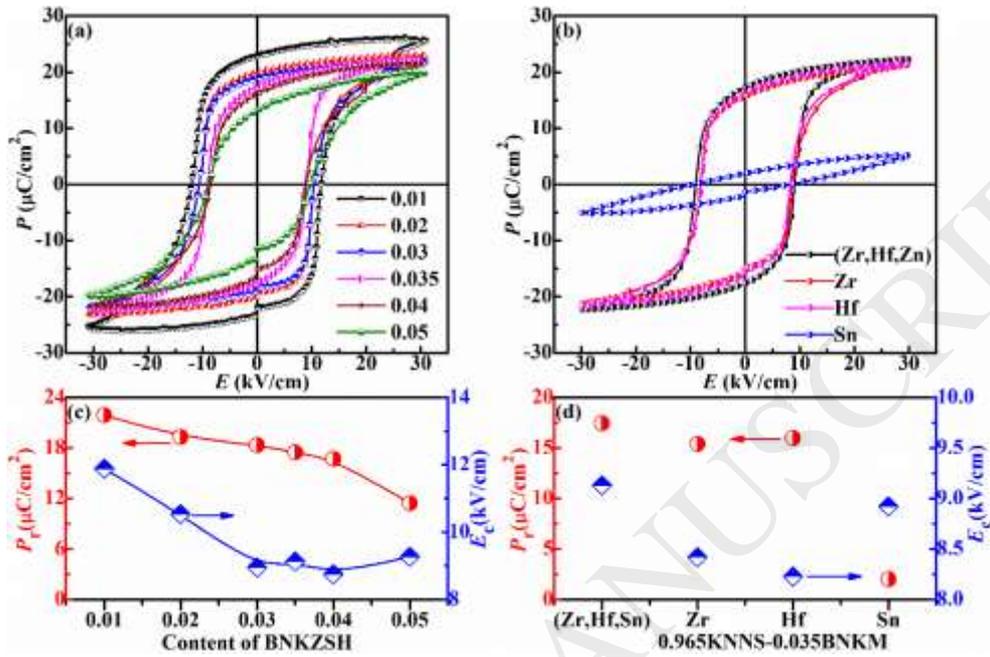
exhibited a lower  $T_c$  of 200 °C. In addition to a lower  $T_c$ , 0.965KNNS-0.035BNKS ceramics also show a much broader and lower peak in the dielectric permittivity [Fig. 4(j)], which might be ascribed to the occurrence of ultra-fine grains [Fig. 1(g)] [35]. It was reported that the decreasing grain size could induce a weak dielectric relaxation and reduce dielectric permittivity [35]. Based on the values of  $T_{R-O}$ ,  $T_{O-T}$ ,  $T_{R-T}$ , and  $T_c$  from Fig. 2(b) and Figs. 4(a-g), a phase diagram was established for  $(1-x)$ KNNS- $x$ BNKZSH ceramics, shown in Fig. 4(k). With increasing  $x$ , both  $T_c$  and  $T_{O-T}$  decreased, but  $T_{R-O}$  increased. Consequently,  $T_{O-T}$  and  $T_{R-O}$  converged, resulting in a direct phase transition between the R phase and the T phase at  $T_{R-T}$ . Since the  $T_{R-T}$  of the ceramics with  $x=0.035$  and 0.04 was very close to room temperature, the R and T phases coexist at room temperature. A single T phase was observed in the ceramics with  $x=0.05$  at room temperature because the  $T_{R-T}$  for these two compositions was much lower. The  $T_{R-T}$  and  $T_c$  values for 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, Hf, and Sn} ceramics are also summarized in Fig. 4(l) for comparison. 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr and Hf} ceramics possessed the similar  $T_c$  values of 240-247 °C, while a low  $T_c$  value of 200 °C was found in 0.965KNNS-0.035BNKS ceramics.



**Figure 4.**  $\epsilon_r$ - $T$  (50 °C-400 °C) curves of (a-g)  $(1-x)$ KNNS- $x$ BNKZSH and (h-j) 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, Hf, and Sn} ceramics. (k) Phase diagram of KNNS- $x$ BNKZSH ceramics. (l)  $T_{R-T}$  and  $T_c$  of 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, Hf, and Sn} ceramics.

Figs. 5(a) and (b) show the  $P$ - $E$  hysteresis loops of  $(1-x)$ KNNS- $x$ BNKZSH and 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, Hf, and Sn} ceramics. As shown in Fig. 5(a), all of the samples showed a typical ferroelectric hysteresis loop. The saturation of  $P$ - $E$  loops gradually reduced as  $x$  increased, suggesting that the addition of BNKZSH deteriorated the ferroelectricity of the KNN-based ceramics to some extent. Both the remanent polarization ( $P_r$ ) and the coercive field ( $E_c$ ) gradually decreased with an increase in  $x$  [Fig. 5(c)]. Saturated  $P$ - $E$  loops were observed in the 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, and Hf} ceramics that possessed an R-

T phase boundary [Fig. 5(b)]. However, an almost linear  $P$ - $E$  loop was observed in 0.965KNNS-0.035BNKS ceramics [Fig. 5(b)], which was due to the high symmetry of the pseudocubic phase [Fig. 2(c)] and ultra-grain size [Fig. 1(g)] [35].

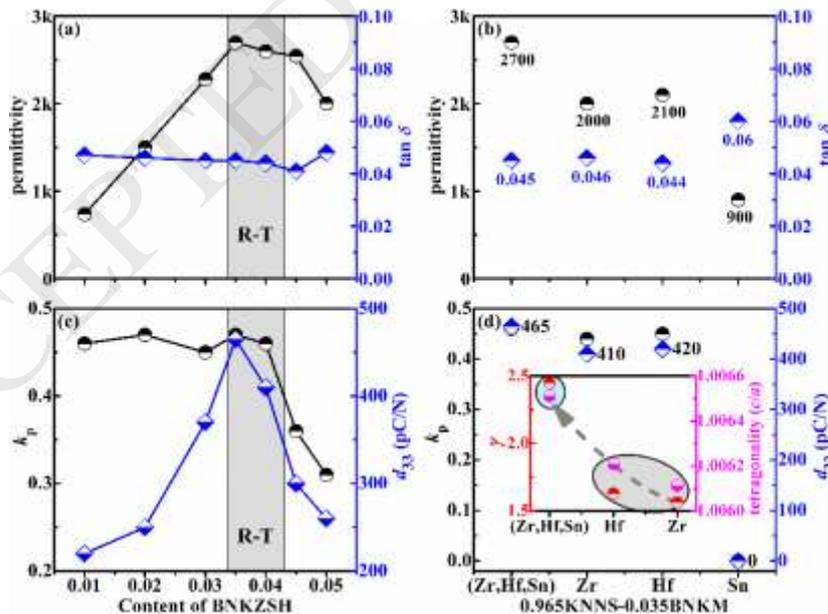


**Figure 5.** Polarization vs. electric field ( $P$ - $E$ ) loops of (a) KNNS- $x$ BNKZSH and (b) KNNS-0.035BNKM  $\{M=(Zr,Hf,Sn), Zr, Hf, \text{ and } Sn\}$  ceramics. Remanent polarization ( $P_r$ ) and coercive field ( $E_c$ ) of (c) KNNS- $x$ BNKZSH and (d) KNNS-0.035BNKM  $\{M=(Zr,Hf,Sn), Zr, Hf, \text{ and } Sn\}$  ceramics.

Figs. 6(a) and (b) show the dependence of  $\epsilon_r$  and  $\tan \delta$  on  $x$  and  $M$  in  $(1-x)$ KNNS- $x$ BNKZSH and 0.965KNNS-0.035BNKM  $\{M=(Zr,Hf,Sn), Zr, Hf, \text{ and } Sn\}$  ceramics, respectively. In  $(1-x)$ KNNS- $x$ BNKZSH ceramics, with increasing  $x$ ,  $\epsilon_r$  first increased and then decreased, leading to a maximum of 2700 at  $x=0.035$  due to the R-T phase boundary [22-26], whereas  $\tan \delta$  ( $\sim 0.045$ ) remained nearly unchanged. In 0.965KNNS-0.035BNKM  $\{M=(Zr,Hf,Sn), Zr, Hf, \text{ and } Sn\}$  ceramics, the values of  $\epsilon_r$  depended on the additives, e.g.,  $\epsilon_r=2700, 2000, 2100,$  and  $900$  for the 0.965KNNS-0.035BNKM ceramics with  $M=(Zr,Hf,Sn), Zr, Hf, \text{ and } Sn,$  respectively. Here, the R-

T phase boundary was mainly responsible for the enhanced  $\varepsilon_r$  in the 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, and Hf} ceramics, while the degraded dielectric properties of 0.965KNNS-0.035BNKS ceramics were mainly caused by the occurrence of ultra-fine grains [Fig. 1(g)] [35]. The composition design (doping with different elements) clearly played an important role in the dielectric properties of the ceramics. Figs. 6(c) and (d) display the variation of  $d_{33}$  and  $k_p$  in (1-x)KNNS-xBNKZSH and 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, Hf, and Sn} ceramics, respectively. With increasing  $x$ ,  $d_{33}$  first increased and then decreased, leading to a maximum of  $d_{33}\sim 465$  pC/N at  $x=0.035$ ;  $k_p$  was nearly independent of  $x$  when  $x<0.035$ , and then decreased when  $x>0.035$  [Fig. 6(c)]. A comparison of  $d_{33}$  and  $k_p$  in 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, Hf, and Sn} ceramics with different additives is shown in Fig. 6(d). All of the ceramics exhibited a large  $d_{33}$  (e.g., 410-465 pC/N) and a high  $k_p$  (e.g., 0.45-0.47), except 0.965KNNS-0.035BNKS ceramics, in which the piezoelectric properties could not be observed due to its pseudocubic phase structure [Fig. 2(c)]. It is widely recognized that both the phase structure and the domain structure are responsible for the piezoelectric properties of piezoelectric ceramics [36]. Generally, the multi-phase coexistence possesses the more possible polarization vectors than that of single phase, which could promote the polarization rotation and then benefit the piezoelectric properties [36]. Furthermore, due to the R-T phase boundary and the ultralow  $\Delta U_{R-T}$  values in this work, a low polarization anisotropy was anticipated, which greatly promoted the polarization rotation and benefited the macroscopic piezoelectric properties [36]. As a result, 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, and Hf} ceramics exhibited higher  $d_{33}$  values (e.g., 410-465 pC/N) than the other compositions due to the R-T phase boundary.

Furthermore, the observed difference of  $d_{33}$  values in 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, and Hf} ceramics could be attributed to the T phase fraction and tetragonality ( $c/a$ ). It was reported that that the piezoelectric properties of the piezoceramics, which possessed an O-T or R-T phase coexistence, were highly dependent on the T phase fraction and tetragonality ( $c/a$ ), owing to the close relationship between piezoelectricity and crystalline symmetry [37-39]. More specifically, the larger piezoelectricity could be obtained in the piezoceramics that exhibited the higher T phase fraction and the larger tetragonality ( $c/a$ ) [37-39]. Here, a comparison between the T/R phase ratio ( $\gamma=T_{\text{fraction}}/R_{\text{fraction}}$ ) and the tetragonality ( $c/a$ ) of 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, and Hf} ceramics (using the refinement results from Table 1) is shown in the inset of Fig. 6(d). Obviously, 0.965KNNS-0.035BNKZSH ceramics exhibited a higher  $\gamma$  and a larger tetragonality ( $c/a$ ) than those of 0.965KNNS-0.035BNKM (M=Zr, Hf) ceramics, which accounted for the higher  $d_{33}$  value in 0.965KNNS-0.035BNKZSH ceramics.

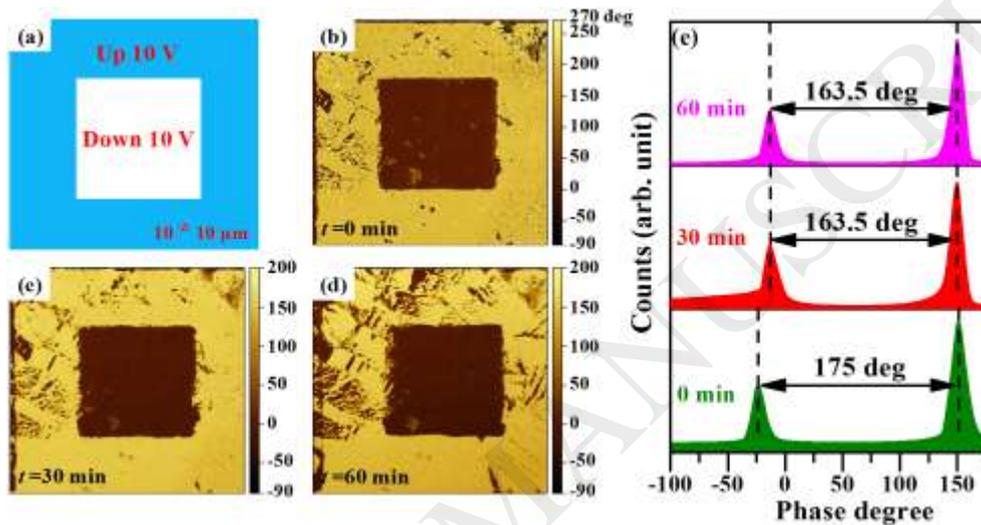


**Figure 6.**  $\epsilon_r$  and  $\tan \delta$  of (a)  $(1-x)\text{KNNS}-x\text{BNKZSH}$  and (b)  $0.965\text{KNNS}-0.035\text{BNKM}$  {M=(Zr,Hf,Sn), Zr, Hf, and Sn} ceramics.  $d_{33}$  and  $k_p$  of (c)  $(1-x)\text{KNNS}-$

$x$ BNKZSH and (d) 0.965KNNS-0.035BNKM  $\{M=(Zr,Hf,Sn), Zr, Hf, \text{ and } Sn\}$  ceramics. The inset of (d) displays a comparison between the T/R phase ratio ( $\gamma=T_{\text{fraction}}/R_{\text{fraction}}$ ) and tetragonality ( $c/a$ ) of 0.965KNNS-0.035BNKM  $\{M=(Zr,Hf,Sn), Zr, Hf, \text{ and } Sn\}$  ceramics.

Since domain structure plays a very critical role in determining the piezoelectricity of materials, vertical piezoresponse force microscopy (VPFM) was used to characterize the 0.965KNNS-0.035BNKZSH samples. The room-temperature piezoresponse and phase images are shown in the section of *in situ* temperature-dependent PFM analysis. Complicated domain structures caused by the coexistence of R and T phases, including striped and irregular domains, were observed at room temperature. Similar phenomena were also observed in the KNNS-BNKZ ceramics with an R-T phase boundary and account for the enhanced piezoelectric properties [40]. To gain a deeper understanding of the properties of the materials, the surface ferroelectric domains were written with a bias voltage of  $\pm 10$  V, as shown schematically in Fig. 7(a). Fig. 7(b) displays the phase image, which was scanned immediately after writing. An appreciable contrast between the bright and dark areas was observed. The phase difference between the dark and bright areas was  $175^\circ$  [Fig. 7(e)], indicating an ideal writing process and easy domain switching. The voltage required to completely switch the surface domains was about 10 V. Such a low driven-voltage was also observed in  $MnO_2$ -modified  $(Na_{0.5}K_{0.5})NbO_3-(Bi_{0.5}Li_{0.5})TiO_3-BaZrO_3$  ceramics with an R-T phase boundary [41]. Figs. 7(c) and (d) show the phase images after writing for 30 and 60 minutes, respectively. The phase contrast faded slightly, indicating relaxation of ferroelectric domains. The corresponding phase histograms also reflected the relaxation, accompanied by a reduced phase difference of  $163.5^\circ$  [Fig. 7(e)]. However, the slight relaxation suggested a good aging resistance because the

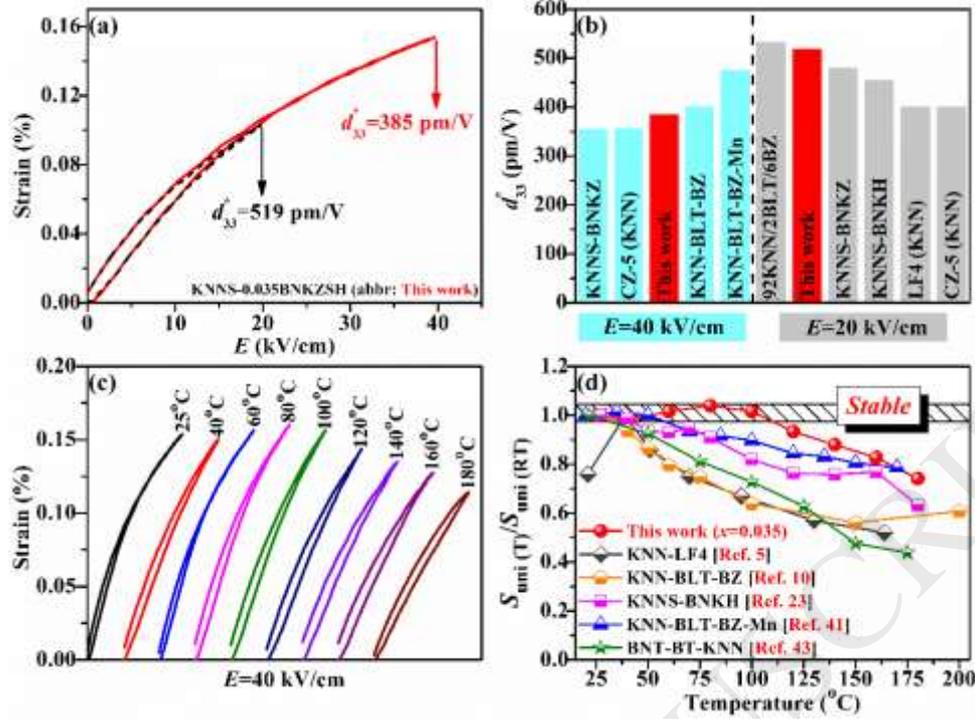
piezoelectricity was closely related to the status of the domains, in terms of quantity and size [42]. Furthermore, the good aging resistance behavior was also experimentally supported by the ultralow  $\Delta d_{33}/d_{33\text{initial}}$  value of 3.3% after aging 21 weeks [see Figure S6 in Supporting Information]. Therefore, the easy switching and slow relaxation of the domains also played an important role in the enhanced piezoelectricity in this work.



**Figure 7.** Vertical piezoresponse force microscopy (VPFM) of 0.965KNNS-0.035BNKZSH ceramics. (a) Sketch of driven electric field; Vertical phase images after writing for (b) 0 min, (c) 30 min, and (d) 60 min; (e) Phase histograms extracted from the VPFM phase images.

Fig. 8(a) displays the unipolar strain curves of 0.965KNNS-0.035BNKZSH ceramics, measured at  $E=20$  kV/cm and 40 kV/cm. Converse piezoelectric coefficient  $d_{33}^*$  ( $d_{33}^* = S_{\text{max}}/E_{\text{max}}$ ) values of 519 and 385 pm/V were respectively obtained at  $E=20$  kV/cm and 40 kV/cm in 0.965KNNS-0.035BNKZSH ceramics, which were comparable to those of other representative KNN-based lead-free piezoceramics, as shown in Fig. 8(b) [5,10,17,23,40,41]. Fig. 8(c) shows the temperature-dependent unipolar strain curves of 0.965KNNS-0.035BNKZSH ceramics at  $E=40$  kV/cm. As

the temperature increased from 25 °C to 80 °C, the maximum unipolar strain ( $S_{\max}$  or  $S_{\text{uni}}$ ) increased slightly. Then,  $S_{\text{uni}}$  gradually decreased at  $T \geq 100$  °C, resulting in a  $S_{\text{uni}(T)}/S_{\text{uni}(RT)}$  value of 1.0 and 0.74 at  $T=100$  °C and 180 °C, respectively [Fig. 8(d)]. The temperature stability of the materials tested here is compared with several representative lead-free piezoceramics systems in Fig. 8(d) [5,10,23,41,43]. In this work, an almost constant  $S_{\text{uni}(T)}/S_{\text{uni}(RT)}$  value of 1.0 was observed across a wide temperature range of 25-100 °C in the 0.965KNNS-0.035BNKZSH ceramics, which was comparable to those of KNN-BLT-BZ-Mn and KNNS-BNKH ceramics that exhibited the pronounced temperature stability and piezoelectricity [23,41]. The  $d_{33}$  and  $T_c$  of our materials, as well as those of several representative lead-free piezoelectric materials and soft PZT-4 ceramics [5-7,24,41,44-46], are presented for comparison in Table 2. Large  $d_{33}$  values ranging from 400 pC/N to 570 pC/N were recently obtained in KNN-based ceramics; however, the  $T_c$  was relatively low (e.g., 190-227 °C). Here, by adequately tuning the R-T phase boundary and composition of 0.965KNNS-0.035BNKZSH ceramics, a high  $d_{33}$  (~465 pC/N) and a high  $T_c$  (~240 °C) were simultaneously achieved. The  $d_{33}$  and  $T_c$  presented here were superior to those of BT- and BNT-based ceramics, and comparable to those of PZT4-based ceramics [see Table 2]. More importantly, a superior temperature stability was observed at  $25$  °C  $\leq T \leq 100$  °C.

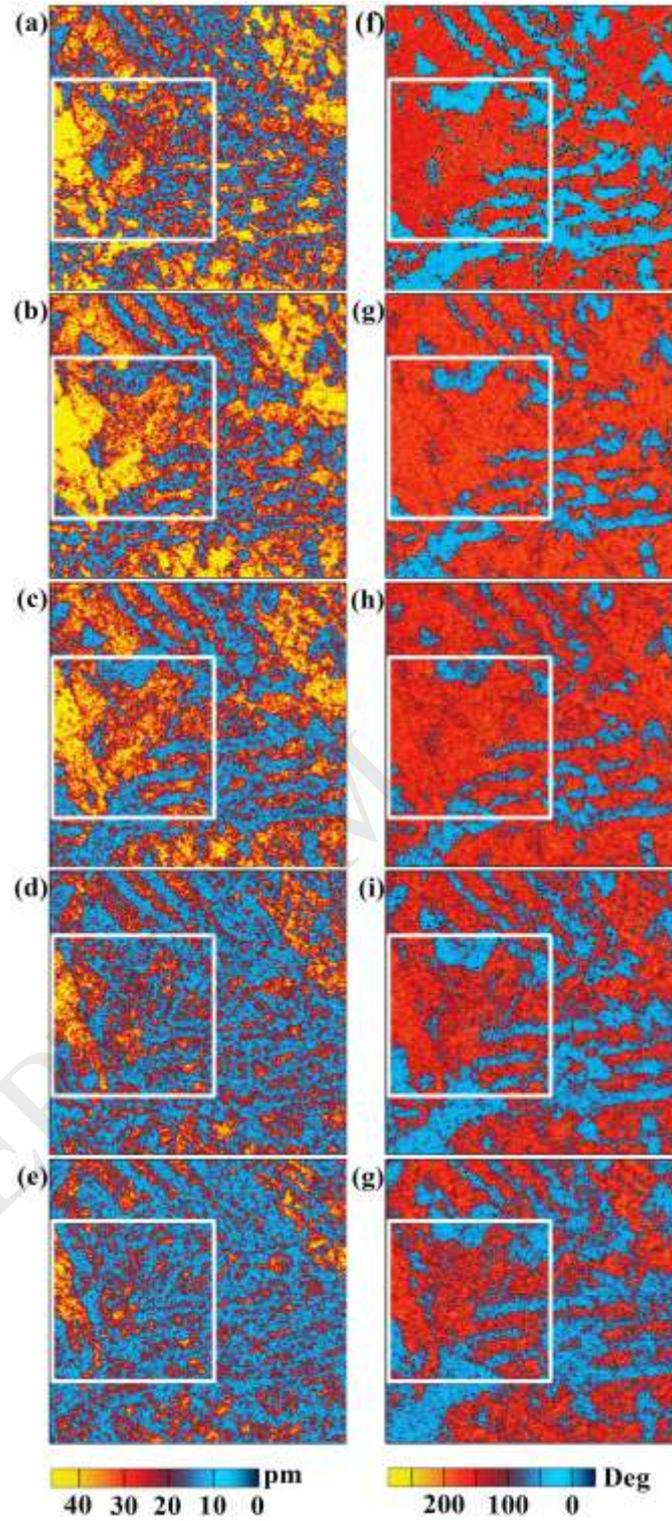


**Figure 8.** (a) Unipolar strain curves of 0.965KNNS-0.035BNKZSH ceramics at  $E=20$  kV/cm and  $40$  kV/cm. (b) Comparison of  $d_{33}^*$  ( $S_{\text{max}}/E_{\text{max}}$ ) among KNNS-0.035BNKZSH and other representative KNN-based lead-free piezoceramics at  $E=20$  kV/cm and  $40$  kV/cm. (c) Temperature-dependent unipolar strain curves of 0.965KNNS-0.035BNKZSH ceramics at  $E=40$  kV/cm. (d) Comparison of  $S_{\text{uni}}(T)/S_{\text{uni}}(\text{RT})$  among KNNS-0.035BNKZSH and other representative lead-free piezoceramic systems.

Here, *in situ* temperature-dependent VPFM measurements were performed to illuminate the physical mechanism behind the enhanced temperature stability. Both the vertical piezoresponse and the phase images were recorded as the temperature increased from  $30^\circ\text{C}$  to  $180^\circ\text{C}$ , as shown in Figs. 9(a-g). A representative area from the PFM images, marked by the white box, was inspected for variations. Within that representative area, both the brightness and sizes of ferroelectric domains were enhanced as the temperatures increased from  $30^\circ\text{C}$  to  $60^\circ\text{C}$ , as shown in the piezoresponse and phase images [Figs. 9(a) and (b) and Figs. 9(f) and (g)], indicating

the improved activity of the domains (e.g., domain switching and domain wall motion) [41,42,47]. Here, the improved activity of the domains was due to the increased thermal energy and diffuse R-T phase boundary in the 0.965KNNS-0.035BNKZSH ceramics, which possessed a broad R-T phase transition temperature of  $T_{R-T}=31\pm 20$  °C [Fig. 2(b)]. Thus, a slight increase in temperature did not substantially affect the phase structure, but did enhance the activity of the domains (e.g., domain switching and domain wall motion). The enhanced activity of the domains also contributed to a slight increase in the unipolar strain at  $25\text{ °C}\leq T\leq 80\text{ °C}$  [Fig. 8(c)] [41,42,47]. When the temperature reached 100 °C, both the piezoresponse and phase images were very similar to those at  $T=30$  °C, indicating a similar activity of the domains. Thus, the  $S_T/S_{RT}$  value of 1.0 was observed at  $T=100$  °C. As temperature increased further, both the brightness and the area of the domains gradually faded in both the piezoresponse and phase images, indicating the reduced domain structure in terms of response and quantity [41,42,47]. Here, the reduced domain structure at  $T\geq 100$  °C originated from the phase transition from R-T phase coexistence to a dominant (or even pure) tetragonal (T) phase and further increasing temperature. Generally, when a piezoelectric undergoes the phase transition from multiphase to a single phase, the domain configurations will inevitably reduce and be simplified owing to the complicated domain structure in multiphase coexistence [36,41,42,47]. Moreover, the further increasing temperature ( $T\geq 100$  °C) will gradually break the long-range order of ferroelectric domain structure [36,41,42,47]. Thus, both two factors are responsible for the reduced domain structure above 100 °C. In spite of the reduced domain structure, a number of domains were still observed in both the piezoresponse and phase images at  $T=180$  °C [Figs. 9(e) and (g)], which accounted for the  $S_T/S_{RT}$  value of 0.74 at  $T=180$  °C [Fig. 8(c)]. In this way, the temperature stability

in 0.965KNNS-0.035BNKZSH ceramics ( $S_T/S_{RT}$  value of 1.0 at  $T=100$  °C) was enhanced by the stable domain structure.



**Figure 9.** Vertical piezoresponse images of 0.965KNNS-0.035BNKZSH ceramics at (a) 30 °C, (b) 60 °C, (c) 100 °C, (d) 140 °C, and (e) 180 °C. Corresponding vertical

phase images at (f) 30 °C, (g) 60 °C, (h) 100 °C, (i) 140 °C, and (j) 180 °C. The measured area (white box) is 5 $\mu$ m $\times$ 5 $\mu$ m.

#### 4. Conclusion

In this work, (1- $x$ )KNNS- $x$ BNKZSH and 0.965KNNS-0.035BNKM (M=Zr, Hf, and Sn) ceramics were synthesized using the conventional solid-state reaction method. The effects of the additive BNKZSH on the microstructure, phase structure, and electrical properties of (1- $x$ )KNNS- $x$ BNKZSH ceramics were systematically investigated. Co-doping with Sb<sup>5+</sup> and BNKZSH decreased  $T_{O-T}$  and increased  $T_{R-O}$ , forming an R-T phase boundary in the ceramics with  $0.035 \leq x \leq 0.04$ . Due to the slight diffuse R-T phase boundary, the ceramics with  $x=0.035$  showed enhanced electrical properties, accompanied by a large piezoelectricity (e.g.,  $d_{33} \sim 465$  pC/N,  $k_p=0.47$ ), a relatively high  $T_c$  of 240 °C, and a superior temperature stability (i.e., unipolar strain remained almost unchanged at  $T=25-100$  °C). The enhanced electrical properties can mainly be attributed to the easy domain switching, high T phase ratio, and tetragonality ( $c/a$ ) in the R-T phase boundary. The superior temperature stability was mainly due to the stable domain structures. Therefore, the construction of an R-T phase boundary and appropriate composition design substantially improved the piezoelectric properties and temperature stability. Thus, this work promotes the understanding of the performance and design of KNN-based lead-free ceramics.

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SEM images.

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**Table 1.** Rietveld refinement results for 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, and Hf} ceramics.

Composition	Spac e group	Lattice parameter*			Phase ratio	$R_w$ (%)	Sig	$\Delta U_{T-R}$ (meV)
		$a=b$ (Å)	$c$ (Å)	$\alpha$ (°)				
	$R3m$	3.9823 (6)		89.97	0.29			
0.965KNNS	$P4m$ $m$	3.9729 (1)	4.0028 (1)	90	0.71	6.05	1.53	5.5

-

0.035BNKZS

H

	<i>R3m</i>	3.9815 (4)	89.98	0.39			
0.965KNNS							
	<i>P4m</i>		4.0013		5.65	1.49	4.4
-0.035BNKZ		3.9770 (7)	90	0.61			
	<i>m</i>		(9)				
	<i>R3m</i>	3.9788 (1)	89.95	0.38			
0.965KNNS							
	<i>P4m</i>		4.0015		6.16	1.57	2.9
-0.035BNKH		3.9768 (3)	90	0.62			
	<i>m</i>		(3)				

\* Due to the intrinsic symmetry,  $a=b=c$  for the *R3m* space group, and  $a=b$  for the *P4mm* space group.

**Table 2:** Comparison among  $d_{33}$ ,  $T_c$ , and phase boundaries of several representative piezoelectric material systems.

Material system	$d_{33}$ (pC/N)	$T_c$ (°C)	Phase boundary	Reference
KNNS-BNKZSH	465	240	R-T	This work
Textured LF4T	416	253	O-T	5
KNNLT-CZ-MnO <sub>2</sub>	300	200	O-T	24
KNNS-BNKZ	490	227	R-T	6
KNNS-BZ-BKH	570	190	R-T	7
KNN-BLT-BZ-MnO <sub>2</sub>	340	243	R-T	41
BNT-BT-KNN	<100	$T_d < 200$	—	44
BNT-BT: ZnO	<200	280	—	45
BZT-BCT	620	90	C-R-T	46
PZT4	410	250	R-T	5

### Figure captions

**Figure 1.** FE-SEM images of polished and thermally etched cross-sections of KNNS- $x$ BNKZSH ceramics with (a)  $x=0.01$ , (b)  $x=0.02$ , (c)  $x=0.035$ , (d)  $x=0.05$ , and 0.965KNNS-0.035BNKM ceramics with (e) M=Zr, (f) M=Hf and (g) M=Sn. (h) Average grain size (AGS) of the ceramics in this work.

**Figure 2.** Enlarged XRD patterns of (a) (1- $x$ )KNNS- $x$ BNKZSH ceramics and (c) 0.965KNNS-0.035BNKM (M=Hf, Zr, and Sn) ceramics with  $2\theta=44-46^\circ$ ; and the  $\epsilon_r$ - $T$  (-150 °C-200 °C) curves of (b) (1- $x$ )KNNS- $x$ BNKZSH and (d) 0.965KNNS-0.035BNKM (M=Hf, Zr, and Sn) ceramics. The enlarged XRD patterns were indexed according to the pseudo-cubic phase structure axes.

**Figure 3.** (a) Temperature-dependent Raman spectra of 0.965KNNS-0.035BNKZSH ceramics at different temperatures and fitting of Raman spectrum at  $T=-150$  °C in the wavenumber range of 500-700  $\text{cm}^{-1}$ . (b) Raman shift of  $A_{1g}$  ( $\nu_1$ ) mode and permittivity of 0.965KNNS-0.035BNKZSH ceramics as a function of temperature. (c) Rietveld refinement of 0.965KNNS-0.035BNKZSH ceramics.

**Figure 4.**  $\epsilon_r$ - $T$  (50 °C-400 °C) curves of (a-g)  $(1-x)\text{KNNS}-x\text{BNKZSH}$  and (h-j) 0.965KNNS-0.035BNKM  $\{M=(\text{Zr,Hf,Sn}), \text{Zr}, \text{Hf}, \text{and Sn}\}$  ceramics. (k) Phase diagram of KNNS- $x\text{BNKZSH}$  ceramics. (l)  $T_{R-T}$  and  $T_c$  of 0.965KNNS-0.035BNKM  $\{M=(\text{Zr,Hf,Sn}), \text{Zr}, \text{Hf}, \text{and Sn}\}$  ceramics.

**Figure 5.** Polarization vs. electric field ( $P$ - $E$ ) loops of (a) KNNS- $x\text{BNKZSH}$  and (b) KNNS-0.035BNKM  $\{M=(\text{Zr,Hf,Sn}), \text{Zr}, \text{Hf}, \text{and Sn}\}$  ceramics. Remanent polarization ( $P_r$ ) and coercive field ( $E_c$ ) of (c) KNNS- $x\text{BNKZSH}$  and (d) KNNS-0.035BNKM  $\{M=(\text{Zr,Hf,Sn}), \text{Zr}, \text{Hf}, \text{and Sn}\}$  ceramics.

**Figure 6.**  $\epsilon_r$  and  $\tan \delta$  of (a)  $(1-x)\text{KNNS}-x\text{BNKZSH}$  and (b) 0.965KNNS-0.035BNKM  $\{M=(\text{Zr,Hf,Sn}), \text{Zr}, \text{Hf}, \text{and Sn}\}$  ceramics.  $d_{33}$  and  $k_p$  of (c)  $(1-x)\text{KNNS}-x\text{BNKZSH}$  and (d) 0.965KNNS-0.035BNKM  $\{M=(\text{Zr,Hf,Sn}), \text{Zr}, \text{Hf}, \text{and Sn}\}$  ceramics. The inset of (d) displays a comparison between the T/R phase ratio ( $\gamma=T_{\text{fraction}}/R_{\text{fraction}}$ ) and tetragonality ( $c/a$ ) of 0.965KNNS-0.035BNKM  $\{M=(\text{Zr,Hf,Sn}), \text{Zr}, \text{Hf}, \text{and Sn}\}$  ceramics.

**Figure 7.** Vertical piezoresponse force microscopy (VPFM) of 0.965KNNS-0.035BNKZSH ceramics. (a) Sketch of driven electric field; Vertical phase images after writing for (b) 0 min, (c) 30 min, and (d) 60 min; (e) Phase histograms extracted from the VPFM phase images.

**Figure 8.** (a) Unipolar strain curves of 0.965KNNS-0.035BNKZSH ceramics at  $E=20$  kV/cm and 40 kV/cm. (b) Comparison of  $d_{33}^*$  ( $S_{\max}/E_{\max}$ ) among KNNS-0.035BNKZSH and other representative KNN-based lead-free piezoceramics at  $E=20$  kV/cm and 40 kV/cm. (c) Temperature-dependent unipolar strain curves of 0.965KNNS-0.035BNKZSH ceramics at  $E=40$  kV/cm. (d) Comparison of  $S_{\text{uni}(T)}/S_{\text{uni}(RT)}$  among KNNS-0.035BNKZSH and other representative lead-free piezoceramic systems.

**Figure 9.** Vertical piezoresponse images of 0.965KNNS-0.035BNKZSH ceramics at (a) 30 °C, (b) 60 °C, (c) 100 °C, (d) 140 °C, and (e) 180 °C. Corresponding vertical phase images at (f) 30 °C, (g) 60 °C, (h) 100 °C, (i) 140 °C, and (j) 180 °C. The measured area (white box) is  $5\mu\text{m}\times 5\mu\text{m}$ .

**Table 1.** Rietveld refinement results for 0.965KNNS-0.035BNKM {M=(Zr,Hf,Sn), Zr, and Hf} ceramics.

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