

Automatic Constraint Detection for Layout Regularization

Haiyong Jiang, Liangliang Nan, Dong-Ming Yan, Weiming Dong, Xiaopeng Zhang, Peter Wonka

Abstract—In this paper, we address the problem of constraint detection for layout regularization. As layout we consider a set of two-dimensional elements where each element is represented by its bounding box. Layout regularization is important for digitizing plans or images, such as floor plans and facade images, and for the improvement of user created contents, such as architectural drawings and slide layouts. To regularize a layout, we aim to improve the input by detecting and subsequently enforcing alignment, size, and distance constraints between layout elements. Similar to previous work, we formulate the layout regularization as a quadratic programming problem. In addition, we propose a novel optimization algorithm to automatically detect constraints. In our results, we evaluate the proposed framework on a variety of input layouts from different applications, which demonstrates our method has superior performance to the state of the art.

Index Terms—layout regularization, constraint detection, constraint analysis, linear integer programming.

1 INTRODUCTION

We propose an algorithm for the regularization of layouts. In this paper, a layout refers to a two-dimensional arrangement of objects. Layouts arise in a variety of applications, for example they can come from digitized architectural floor plans, digitized facade images, image and text layouts on slides, line drawings, and graph drawings. In practice, when a layout is designed or digitized from another source (e.g., images), it is inevitable that noise occurs through imprecise user input. Elements in an idealized layout exhibit some regularities, e.g., they are aligned, of same-size, or uniformly distributed along a specific direction. However, in the aforementioned applications these regularities typically disappear due to the approximate user input. In this work, we want to detect and restore these regularities, eliminating the noise that occurred during the layout design or digitization stage.

We see three reasons why this is an important problem. First, high-level shape analysis is a popular topic in computer graphics. Many available methods rely on correctly extracted relationships to analyze a scene [1]. Even if the input and output of our regularization look visually similar, it is important that correct relationships are extracted. Our motivation for this paper, was to build datasets for

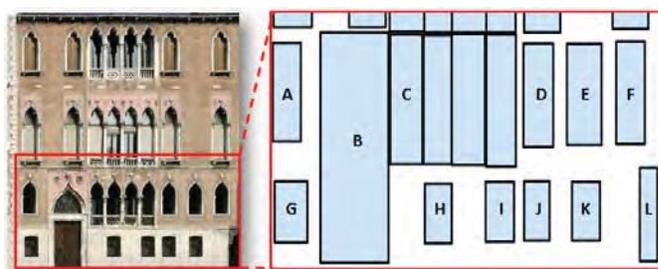


Fig. 1 Complexity and multiformity of constraints in a facade layout. Elements B and C are partially aligned (only top aligned, but not bottom aligned). The large element B is aligned with different objects at the top ($C \dots F$) and bottom (L). Elements are missing from a regular pattern consisting of A , D , E , and F . Spacing between same-sized elements H , I , J , K is irregular.

machine learning techniques for layout synthesis. Second, a regularized layout compresses better than a noisy one. Therefore, regularization is important for representing layouts efficiently. Third, in most cases the visual differences are noticeable and the regularized layout looks better than the original one.

Regularization of layouts is challenging in several ways and we discuss a few selected example challenges: 1) Elements can be partially aligned (e.g., elements are only bottom aligned, but not top aligned). 2) Large elements can be aligned with multiple objects (e.g., top aligned with one and bottom aligned with another). 3) Elements can be missing from a regular pattern. 4) Spacing between rows or/and columns can be irregular. Fig. 1 shows the complexity of possible constraints in an example layout.

A key ingredient in regularization is the design of the layout model. A simple layout model has only a few parameters and therefore the fitting process is fairly robust. These simple models, e.g., a set of regular grids, are popular for

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44 automatic pattern analysis in images [2] and 3D shapes [3],¹⁰³ split grammar to parse the facade images. Teboul et al. [13]
45 [4]. Unfortunately, this simple data model limits the appli-¹⁰⁴ parse facade layouts by using reinforcement learning. Wu et
46 cability to a large class of layouts, e.g., the layout shown in¹⁰⁵ al. [1] extract grammars from labeled facade layouts, and
47 Fig. 1. A complex model typically has many parameters and¹⁰⁶ generate large scale variations by editing the grammars.
48 can fit a large number of layouts. However, the model is not¹⁰⁷ Shen et al. [14] adaptively partition urban facades into a
49 very robust to noise.¹⁰⁸ hierarchical structure based on concatenated and interlaced

50 An initial framework for regularization was presented¹⁰⁹ grids. Musialski et al. [15] developed an interactive tool for
51 by Pavlidis and Van Wyk [5]. They propose a simple greedy¹¹⁰ facade image segmentation, where a significant amount of
52 algorithm to detect constraints from a layout. By contrast,¹¹¹ user interaction is required. While most of these analysis of
53 we use an optimization approach based on four steps.¹¹² the facade layouts use a hierarchical representation, Zhang
54 First, we extract constraint candidates. Second, we score the¹¹³ et. al. [16] proposed to model layouts using layered grids
55 likelihood of constraints using energy functions. Third, we¹¹⁴ with irregular spacing. In our work, we also use grids with
56 use global optimization using linear integer programming¹¹⁵ irregular spacing, but we can avoid the complexity of the
57 to select a subset of the constraint candidates that work well¹¹⁶ layered structure.

58 together. Fourth, we regularize the layout by transforming¹¹⁷ **Geometry structure analysis.** In the 3D space, quite a few
59 the contents of the layout such that the change in both of¹¹⁸ papers focus on discovering regular patterns for geometry
60 the element locations and sizes is minimal while respect-¹¹⁹ structure analysis. Mitra et al. [17] propose a pair matching
61 ing the selected constraints. Our formulation of the layout¹²⁰ based approach to detect partial and approximate symmetry
62 regularization is an energy minimization using quadratic¹²¹ in 3D shapes. Pauly et al. [18] further introduce a framework
63 programming.¹²² for detecting translational, scaling and rotational patterns

64 In our results, we will show that our algorithm has much¹²³ in 3D shapes. Tevs et al. [19] build a connection among
65 better performance than [5] and also better performance¹²⁴ similar shapes via geometric symmetries and regularities.
66 than the independently developed algorithm in [6]. Further,¹²⁵ These approaches have inspired many applications, such as
67 our framework has more types of constraints that can be¹²⁶ shape analysis, reconstruction, and synthesis. For example,
68 considered than previous work. The constraints we consider¹²⁷ Li et al. [20] propose to reconstruct 3D shapes from noisy
69 are constraints on the size, spacing, and alignment of layout¹²⁸ and incomplete point cloud data that simultaneously de-
70 elements.¹²⁹ tects surface primitives and their mutual relationships. This

71 We make the following contributions:¹³⁰ approach involves both local and global shape analysis. We
72 • We propose a formulation of the layout regulariza-¹³¹ refer the reader to the recent survey paper of [21] for more
73 tion problem that has better performance than previ-¹³² related work in this topic.

74 • We extend previous work by including a larger vari-¹³³ **Layout enhancement.** The layout enhancement (regular-
75 ous work, as evaluated on a test dataset consisting of¹³⁴ ization and beautification) has been studied in different
76 layouts from a variety of applications.¹³⁵ areas, e.g., object alignment [22], handwriting and drawing
77 • We extend previous work by including a larger vari-¹³⁶ beautification [23], [24], [25], sketch and drawing beautifi-
78 ety of constraints that can be detected and considered¹³⁷ cation [5], [6], [26], [27], and 3D shape symmetrization [28].
in the layout optimization.¹³⁸ Nan et al. [29] exploit and model conjoining Gestalt rules
¹³⁹ for facade elements grouping and summarization. AlHa-
¹⁴⁰ lawani et al. [30] analyze and edit the facade images with

79 2 RELATED WORK

80 The layout problem can be roughly classified into two major¹⁴¹ (semi-)regular grid structures. Huang et al. [31] combine
81 categories, i.e., seamless layouts without gaps, and layouts¹⁴² patch-based image completion and translational symmetry
82 with gaps between elements. Our work focuses on the latter¹⁴³ detection to fill the missing part of an incomplete planar
83 type of layout problems. We review the most related work in¹⁴⁴ structure. More recently, Xu et al. [32] propose a command-
84 image structure analysis, geometry structure analysis, and¹⁴⁵ based arrangement tool for 2D layouts.
85 layout enhancement.¹⁴⁶ Pavlidis and Van Wyk [5] beautify drawings using a clus-
86 **Image structure analysis.** There is a large amount of struc-¹⁴⁷ tering method, while Xu et al. [6] interactively enhance the
87 ture analysis literature that addresses different aspects of¹⁴⁸ global beautification with user guidance. We will compare
88 image analysis and understanding. A common interest in¹⁴⁹ our approach to these two methods in Sec. 6.

89 both computer graphics and computer vision is the fa-¹⁵⁰ In this work, we are interested in processing digitized
90 cade layout analysis for urban modeling [7]. The image¹⁵¹ 2D images and drawings. By abstracting each layout as a
91 labeling problem has been addressed by considering both¹⁵² set of rectangles, our goal is to regularize the layout of the
92 visual evidence and architectural principles [8]. Based on¹⁵³ elements such that the regularities of the elements in the
93 a perceptual grouping approach, translational symmetry is¹⁵⁴ layout are enforced.

94 exploited for single-view image recognition [9]. A similar
95 approach that uses the repetition information for facade
96 image reconstruction is proposed by Wu et al. [10]. To¹⁵⁵ **3 OVERVIEW**

97 understand the structure of a facade, a set of facade im-¹⁵⁶ Given an image or drawing \mathbf{I} that is characterized by a
98 ages are first recursively split and labeled for training, and¹⁵⁷ set of rectangles, the layout $L = \{e_1, \dots, e_n\}$ of \mathbf{I} can be
99 then the features are extracted from the segmented facades¹⁵⁸ simply described as the locations and sizes of the elements
100 and are used to guide the labeling. Riemenschneider et¹⁵⁹ in \mathbf{I} . Here, an element e_i is defined by a label l_i , and its
101 al. [11] combine both low-level and mid-level classifiers¹⁶⁰ bounding box $b_i = \{x_i, y_i, w_i, h_i\}$ depicting its bottom-left
102 for irregular facade parsing. Yang et al. [12] use a binary¹⁶¹ corner (x_i, y_i) and the size (w_i, h_i) (see Fig. 4). Our goal

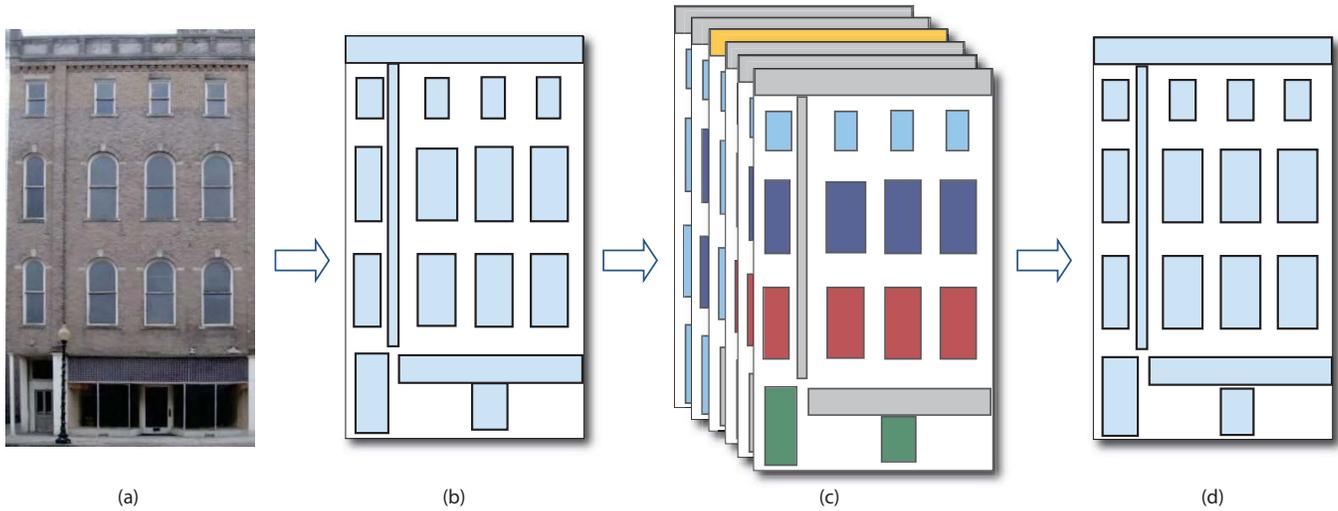


Fig. 2 An overview of our layout regularization approach. Given an input image or drawing (a), we first obtain the initial layout by manually marking and labeling the elements in a pre-processing step (b). Then appropriate constraints are automatically selected (c) and are used to generate the regularized layout (d).

is to regularize the layout of the elements such that the regularities of these elements are enforced.

Our proposed solution to the layout regularization problem uses both discrete and continuous optimization. Fig. 2 shows an overview of our layout regularization method. Our method consists of the following three steps.

Preprocessing. To digitize the layout of a given image, the user manually marks and labels the elements in the input image. The output of the preprocessing step is the initial layout that will be regularized in the next steps. Alternatively, the input can be user generated drawings or slide layouts.

Constraint selection. We first detect a larger set of candidate constraints from the initial layout using a simple thresholding based method. Then we score each constraint using an energy function. Finally, we select a set of constraints from the candidates using global optimization (linear integer programming). Details on constraint selection are described in Section 4.

Layout regularization. To regularize the input layout, we transform the contents of the layout such that the change in both of the element locations and sizes is minimal while respecting the selected constraints. We formulate the layout regularization as energy minimization using quadratic programming (Section 5).

4 CONSTRAINTS SELECTION

Given the user marked elements in a layout, our layout regularization tries to detect and enforce three types of constraints: alignment, same-size, and same-spacing. This problem is challenging in the following ways. First, we have to detect reasonable constraints connecting elements in the layout. Second, there may exist potential conflicts among these constraints. To address these problems, we introduce an optimization-based constraint selection algorithm. The selected constraints are then used in a quadratic programming formulation to regularize the layout (see Section 5).

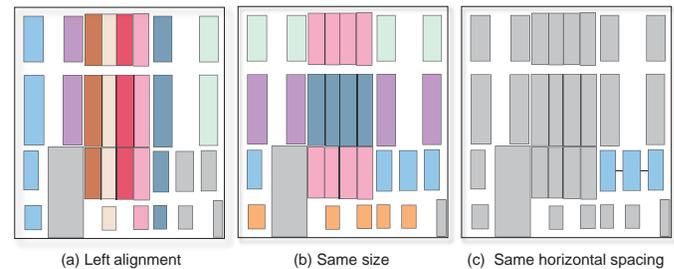


Fig. 3 A subset of constraints in the example layout in Fig. 1. Colors indicate different constraint groups in this figure.

4.1 Constraint Definitions

We consider the following relationships between elements as potential regularity constraints: alignment constraints, same-size constraints, and same-spacing constraints (see Fig. 3 and Fig. 4).

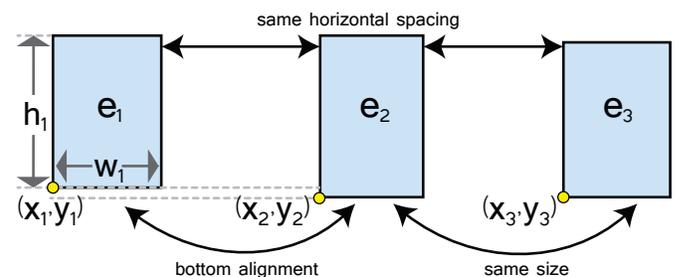


Fig. 4 Illustration of three types of constraints. The bottom alignment of element e_1 and e_2 can be formulated as $y_1 - y_2 = 0$. For the same size constraint of element pair (e_2, e_3) , we have $w_2 - w_3 = 0$ and $h_2 - h_3 = 0$. The horizontal same spacing constraint on element pairs $\{e_1, e_2\}$ and $\{e_2, e_3\}$ will turn out to be $x_2 - (x_1 + w_1) - (x_3 - (x_2 + w_2)) = 0$.

203 **Alignment constraints.** Two elements e_i and e_j can have
204 one or multiple of the following alignment constraints: 205
206 top alignment, middle-Y alignment, bottom alignment, left
207 alignment, middle-X alignment, and right alignment. For
208 example, a bottom alignment between e_i and e_j can be

$$y_i - y_j = 0, \tag{1}$$

209 Other alignment relations are defined in a similar way.

210 **Same-size constraints.** Two elements e_i and e_j may be
211 linked by a same-width constraint or a same-height con-
212 straint or both. Elements with the same label are always
213 considered to hold both same-size constraints. Same size
214 constraints can be formulated as:

$$\begin{aligned} w_i - w_j &= 0, \\ h_i - h_j &= 0. \end{aligned} \tag{2}$$

215 **Same-spacing constraints.** Same-spacing constraints are de-
216 fined on 2–element pairs and can be either in the horizontal
217 or vertical direction. Currently, we only consider same-
218 spacing constraints between elements with the same labels.
219 For example, assume the element pairs (e_i, e_j) and (e_m, e_n)
220 should have the same spacing in the horizontal direction.
221 The equations for same-spacing constraints depend on the
222 relative position of the elements. For the given example
223 assuming $x_i < x_j$ and $x_m < x_n$ would lead to

$$x_i + w_i - x_j - (x_m + w_m - x_n) = 0. \tag{3}$$

224 4.2 Candidate Group Generation

225 The candidate group generation step computes a set of
226 candidate groups $\{g_i\}$, where each group g_i is a set of el-
227 ements that share an alignment, same-size, or same-spacing
228 constraint. In this step, we use a threshold t_a to limit the
229 candidate groups to a reasonably small set. Note that the
230 threshold t_a is a global control mechanism for the number of
231 candidate groups being generated. This threshold is set high
232 enough so that all reasonable candidates are generated. Note
233 t_a is only used for generating the candidate constraints,
234 while the actual constraints are selected using the linear in-
235 teger programming formulation described later. We describe
236 the candidate group generation for each constraint type in
237 the following.

238 **Alignment constraints.** We use top-alignment as an exam-
239 ple. We sort all the elements in the input layout according
240 to the y value of their top edge. Let $\{p_1, \dots, p_n\}$ denote the
241 top positions of the sorted elements. We generate a set of
242 potential groups, such that the difference in the top positions
243 of every pair of the elements in each group are less than the
244 threshold t_a .

245 **Same-size constraints.** For same size constraints, we first
246 group all elements according to their label because we
247 assume that elements with the same label have the same
248 size. Then, we compute the average element size for each
249 label and use this element size to define a distance between
250 labels using the l_1 norm. For each label we find the k -nearest
251 neighboring labels, where k is iterating from 1 to the number
252 of labels. This yields an initial set of candidate groups. Then
253 we filter out candidate groups in which there exists two
254 elements with a size difference larger than the threshold t_a .

Same-spacing constraints. We take horizontal same-spacing
as example. We sort all the element pairs in the input lay-
out according to their horizontal intervals. Then the same-
spacing constrained groups are generated by combining
element pairs so that each group satisfies the following two
conditions: 1) The difference in the interval of every element
pair is less than the threshold t_a ; 2) The elements overlap in
the vertical direction.

4.3 Energy Functions

We now describe how to assign energy values to candidate
groups, so groups with lower energies are more likely to
be selected. We first describe a set of auxiliary heuristic
functions that will then be combined to obtain various
energy functions. In the optimization, we will use a linear
combination of the described energy functions as the objec-
tive function. A constraint group g_i is composed of a set of
elements $\{e_1, \dots, e_n\}$ (2–element pairs for same-spacing). We
define the following functions on g_i :

Standard deviation. The function $stdvar(g_i)$ measures the
standard deviation of positions (for alignment constraints),
sizes (for same-size constraints), or spacings (for same-
spacing constraints). For example, if g_i is a group of top-
aligned elements, $stdvar(g_i)$ is the standard deviation of
the top positions of all elements in group g_i .

Maximal element distance. The function $maxDist(g_i)$ com-
putes the maximal distance between positions, sizes, or
spacings. For example, for a group of top-aligned elements,
 $maxDist(g_i)$ is defined as the difference between the maxi-
mal and the minimal top position in the group.

Group scale. The function $scale(g_i)$ is an intuitive measure
for the scale of group g_i in the relevant direction (x or
 y). This function is evaluated differently for alignment,
same-size, and same-spacing constraints. For example, for
a group g_i with horizontal alignment, $scale(g_i)$ is equal to
the minimal height of elements in group g_i . For same size
constraints, $scale(g_i)$ is the maximum of the minimal width
and minimal height of the elements in group g_i . For same-
spacing constraints, we define $scale(g_i)$ as the minimum
spacing between element pairs in g_i .

In order to measure the quality of a constraint group, we
consider the following energy terms.

Intra-group distance. In our analysis, a good group should
have a small variance and a small maximal element dis-
tance. Further, these values should be normalized by scale:

$$E_d(g_i) = \frac{max(0, stdvar(g_i) + maxDist(g_i) - \epsilon)}{scale(g_i)}, \tag{4}$$

where ϵ is the maximal allowed tolerance value so that
distances smaller than ϵ will be ignored. We set ϵ to 3 pixels
based on our experiments.

Aspect ratio variance. For same size constraints, the aspect
ratio plays an important role. Thus, we use an energy term
 $E_a(g_i)$ that captures the standard deviation of the aspect
ratio of all elements in group g_i . Here the aspect ratio of
an element is defined as $\frac{w}{h}$, where w, h are the width and
height of the element.

4.4 Constraint Selection

We employ linear integer programming to select a set of
constraint groups among the candidate groups. There are

multiple goals: First, the energy values of the selected groups should be low. Second, the complexity of the overall model measured by the number of constraint groups used should also be low. This motivates the use of an additional sparsity term. In our formulation, each constraint type uses a different energy function.

Given an input layout L consisting of n elements, and the candidate constraint groups $G = \{g_1, \dots, g_N\}$ generated from L , our task is to choose a subset of these candidate groups as constraints for the following layout regularization step. Let $C = C_a \cup C_{ss} \cup C_{sp}$ denote all the constraint types, where C_a , C_{ss} , and C_{sp} are alignment, same size, and same-spacing types, respectively. $\mathbf{Z} = \{z_1, \dots, z_N\}$ denotes the binary label for each candidate group (1 for *chosen* and 0 for *not chosen*). We split \mathbf{Z} into three subvectors \mathbf{Z}_a , \mathbf{Z}_{ss} , and \mathbf{Z}_{sp} representing the labels for each type of the constraint groups. Then the energy for these types of constraint groups are defined as follows:

Alignment constraints.

$$E(\mathbf{Z}_a) = \sum_{c_j \in C_a} \sum_{g_i \in G} E_d(g_i) \cdot z_i \cdot \delta(g_i, c_j) + w_a \cdot \|\mathbf{Z}_a\|_0, \quad (5)$$

where $\|\cdot\|_0$ denotes the ℓ^0 -norm, which counts the number of nonzero entries in a vector. We add this term to encourage fewer and larger groups (i.e., groups that have more elements). Since $z_i \in \{0, 1\}$ in our problem, $\|\cdot\|_0$ can be simplified to the sum of all the entries in the vector. $\delta(g_i, c_j)$ is an indicator function that has value 1 if g_i is a candidate group of constraint type c_j , otherwise zero. w_a is a weight that balances the two terms.

Same size constraints. The energy function for same size constraints is similar to that of alignment constraints. To account for aspect ratio of an element in the layout, we also involve the aspect ratio variance E_a into the formulation:

$$E(\mathbf{Z}_{ss}) = \sum_{c_j \in C_{ss}} \sum_{g_i \in G} (E_d(g_i) + w_a \cdot E_a(g_i)) \cdot z_i \cdot \delta(g_i, c_j) + w_{ss} \cdot \|\mathbf{Z}_{ss}\|_0, \quad (6)$$

Same spacing constraints. For same-spacing constraints, the energy function is similar to that of alignment constraints:

$$E(\mathbf{Z}_{sp}) = \sum_{c_j \in C_{sp}} \sum_{g_i \in G} E_d(g_i) \cdot z_i \cdot \delta(g_i, c_j) + w_{sp} \cdot \|\mathbf{Z}_{sp}\|_0, \quad (7)$$

Afterwards, proper constraint groups are selected by minimizing the following constrained objective function:

$$\begin{aligned} & \underset{\mathbf{X}}{\text{minimize}} && E(\mathbf{Z}_a) + E(\mathbf{Z}_{ss}) + E(\mathbf{Z}_{sp}) \\ & \text{subject to} && \sum_{i=1}^N \|g_i\| \cdot z_i \cdot \delta(g_i, c_j) = n, \quad c_j \in C \\ & && z_i + z_j \leq 1, \quad \forall g_i \cap g_j \neq \emptyset, \quad 1 \leq i, j \leq N \\ & && z_i \in \{0, 1\}, \quad 1 \leq i \leq N, \end{aligned} \quad (8)$$

where the constraints $\sum_{i=1}^N \|g_i\| \cdot z_i \cdot \delta(g_i, c_j) = n$ ensure that every element in the layout is assigned to a constraint group of type c_j . The second group of constraints $z_i + z_j \leq 1$ enforce that groups do not have overlapping elements if g_i and g_j are of the same constraint type.

The optimization problem above is a linear integer program that can be efficiently solved using various open source solvers, e.g., [33], [34], [35]. The solution is a set of constraint groups. Each group gives rise to a set of linear equations that serve as constraints during the layout regularization step. For example, for an alignment group $g_i = \{e_{i1}, \dots, e_{iN}\}$, we combine adjacent elements to form the constraint pairs, namely, $(e_{i1}, e_{i2}), \dots, (e_{i(n-1)}, e_{iN})$. Then we generate one linear equation per constraint pair.

5 LAYOUT REGULARIZATION

With the optimal constraints detected and filtered from the constraint selection step, our final goal is to regularize the layout under these constraints. Our regularization process has a similar format with the methods of [36] and [37]. These works both emphasize on the facade structure using a hierarchical layout, while ours deals with a layout of rectangles. We address this regularization problem by transforming the contents of the layout from the input layout L to regularized layout L^* such that the change to element locations C_L and element sizes C_S is minimal while respecting the constraints. The star ($*$ in L^*) indicates the regularized layout.

To facilitate user preferences, we use a weight ω (we set as 2.5 for our preference for position changes) to balance between the two terms above. Then the layout regularization is formulated as energy minimization as below:

$$L^* = \arg \min (C_L + \omega \cdot C_S), \quad (9)$$

where

$$\begin{aligned} C_L &= \sum_{i=1}^n \left(x_i^* + \frac{w_i^*}{2} - x_i - \frac{w_i}{2}\right)^2 + \left(y_i^* + \frac{h_i^*}{2} - y_i - \frac{h_i}{2}\right)^2 \\ C_S &= \sum_{i=1}^n (w_i^* - w_i)^2 + (h_i^* - h_i)^2 \end{aligned}$$

In addition to the aforementioned constraints selected in Section 4, we add additional constraints to Equation 9 to ensure the validity of the optimized layout. In our formulation, we include lower bound constraints and upper bound constraints for the variables, and sequential constraints for the elements' relative positions.

- **Lower and upper bound constraints.** These constraints restrict the changes of elements in reasonable ranges. Let (w_b, h_b) denote the size of the bounding box of the layout, we add additional positional constraints $0 \leq x_i^* \leq w_b$ and $0 \leq y_i^* \leq h_b$.

Further, to prevent the elements from being changed too much in their sizes, we also add upper bound constraints on their sizes. Let's take the width bound as an example, it is defined proportionally to the widths of all elements that have the same label ℓ . In our implementation, the maximal allowed width change for an element e_i is defined as $\max(0.5 \cdot \Delta w_\ell, 0.15 \cdot w_i)$, where Δw_ℓ is the maximal difference in width for elements that have the same label, and w_i is the width of e_i . The size constraints on element height are defined similarly.

- **Sequential constraints.** These constraints specify the relative positions of pairs of elements. With these

constraints, we expect that the elements' original layout will not be greatly altered by the regularization. Our experiments show that this type of constraints is crucial to layout regularization. Given 2 X -ordered (ascending order) elements e_i and e_j , the constraints are $x_i^* + w_i^* - x_j^* \leq 0$ if $x_i + w_i - x_j \leq 0$. The same goes for the vertical direction.

By solving the quadratic programming problem defined in Equation 9, we obtain the regularized layout. In our implementation, we add the constraints sequentially in order to avoid potential conflicts. If there is any conflicts detected during the optimization, we just remove the current constraint. However, the sequence of constraints will affect the results. To incorporate our preferences for different constraints, we sort all constraints according to their energy function $stdvar(g_i)$ (see Eq. 4), and then add them to the constraint set according to this order.

6 RESULTS AND DISCUSSION

Test database. Our experiments are conducted on a database of 32 digitized layouts from various applications. Our data set contains examples covering facades, slide designs, web designs, indoor scenes, and other graphical layouts. In Figures 5, 6, and 7 we show a set of different layouts regularized using our method. In the supplemental materials, we provide more results showing detected relations and regularized layouts. From these applications, we can see that our method enforces the regularity constraints, while preserving the high-level relations, such as symmetries and the repetitive patterns.

Evaluation metrics. In order to evaluate the effectiveness of our framework, we designed an interactive program to specify the ground truth relationships for each layout. We use the marked relations to compute precision (P), recall (R), and F-measure(F) defined as follows:

$$\begin{aligned}
 P &= \frac{\sum_{i \in G_g} \sum_{j \in G_d} num(g_i \cap g_j)}{\sum_{j \in G_d} num(g_j)}, \\
 R &= \frac{\sum_{i \in G_g} \sum_{j \in G_d} num(g_i \cap g_j)}{\sum_{i \in G_g} num(g_i)}, \\
 F &= \frac{2 \cdot P \cdot R}{P + R},
 \end{aligned}
 \tag{10}$$

where G_g is the set of constraint groups in the ground truth, G_d is the set of constraint groups in the detected result, and $num(\cdot)$ is the number of constraints in a constraint group. The term $g_i \cap g_j$ denotes the intersection of two constraint groups. It is empty if g_i and g_j are of different types of constraints. For alignment and same size, an n -element constraint group will contribute $n - 1$ constraint pairs, while an n -pair spacing group will contribute $n - 1$ constraint pairs (see Section. 4.1). Thus, we define the number of constraints of a constraint group as the number of constraint pairs it yields. For example, consider we have the top alignment of elements $G = \{e_1, e_2, e_3, e_4, e_5\}$ as ground truth, but the algorithm only detects elements $D = \{e_1, e_2, e_3, e_5\}$ as top

TABLE 1 Comparisons with [5] and [6] on alignment and same-spacing constraints. Our method is evaluated with and without labels. We show the average precision, recall, and F-measure for all layouts in the test dataset.

Method	Alignment			Same-spacing		
	P	R	F	P	R	F
Pav85 [5]	0.927	0.726	0.804	0.782	0.366	0.453
Xu2014 [6]	0.920	0.832	0.868	0.732	0.498	0.540
Ours (no label)	0.911	0.959	0.936	0.750	0.706	0.710
Ours	0.911	0.959	0.936	0.916	0.613	0.696

aligned. Then we have $num(D) = 4 - 1$, $num(G) = 5 - 1$, and $num(G \cap D) = 4 - 1$.

Comparison. We conducted comparisons with the methods of Xu et al. [6] and Pavlidis et al. [5]. Pavlidis et al. [5] propose to use a clustering method to detect the constraints. Xu et al. [6] employ the RANSAC method to get alignment constraints, and a clustering method for same spacing detection. We first conduct a test of alignment constraints. Fig. 8 shows the precision, recall, and F-measure for every layout in our test database. As we can see, our algorithm has similar precision to previous work, but higher recall for most layouts. This leads to the highest F-measure results on 93.8% of layouts in the database. The comparison is also summarized in Tab. 1 left. In the next test, we compare the same-spacing constraints. In Tab. 1 right, we show the comparison of the average values for precision, recall and F-measure. From this comparison we see that the same-spacing constraint is more difficult to detect than the alignment constraint. Additionally, it was also very difficult to define a ground truth for this constraint. From the above comparison, we can see that the precision of the same spacing detection benefits from the label information. However our method still works better than others even without the label information. In Fig. 9, we also show an illustrative example of a case where our method is more successful than Xu et al. [6]. We can see that Xu et al. can not handle layouts where elements overlap with each other, thus it cannot align the elements properly. In addition, we compare the performance of these three methods by measuring the average computation time for the examples in our dataset. The method in [5] could detect the constraints in 0.001s because of the simplicity of the method. The method of Xu et al. [6] needs 0.898s, while ours needs about 0.914s.

Running time. We have implemented the proposed method in C++. All the experiments are performed on a PC with two 2.70GHz Intel Xeon E5-2680 processors. We found that the running time highly depends on the number of elements and the number of relations in the input layout. On average, the constraint selection step takes 0.70 seconds, and the regularization step takes 3.59 seconds. The maximum times were 3.71 seconds and 15.78 seconds, respectively.

Robustness & scalability. We evaluated the robustness and scalability of our algorithm on synthesized examples. We first generate a regular grid of elements of two different sizes with 8 columns and 5 rows. We then perturb the corners of the elements with an increasing amount of Gaussian noise (measured relative to the element sizes). The performance of our method is demonstrated in Tab. 2. We can see that

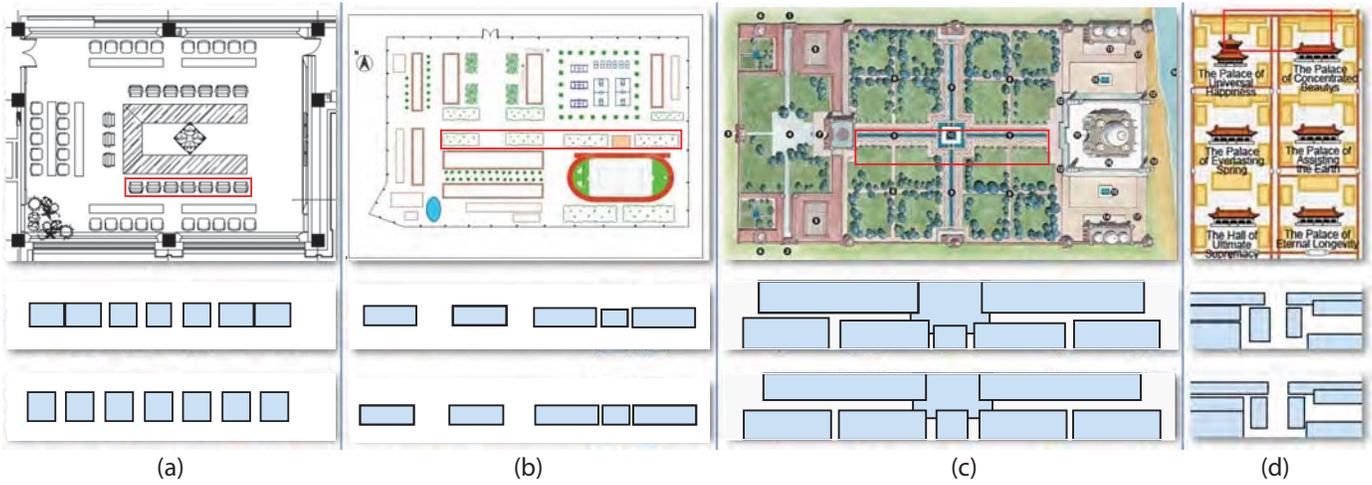


Fig. 5 Four different layouts are regularized using our method. Each column (from top to bottom) shows the input floor plan, zoomin of the marked region in the initial layout, and our regularized layout.



Fig. 6 Layouts regularization for a set of urban facade images. The top row shows the input facade images. The middle and the bottom rows show the zoomin views of the highlighted regions and the regularized results with abstract boxes.

our method works well if the noise is less than 10% of the element size. To evaluate the scalability, we use Gaussian noise with variance 0.02 and measure the running time for grids with a different number of elements. In Tab. 3 we show the results of this test. We can see that the accuracy decreases with larger grids. The reason is mainly that some of the same spacing constraints are not detected due to outliers.

Parameters. In our method, there exists multiple parameters. One parameter is the threshold t_a that is used to generate candidate groups. In order to verify the influence of this parameter on the results, we evaluate our method with different values of the threshold t_a on the alignment constraints (see Fig. 10). Our method can generate high quality results after a value of 0.2 times the average element

TABLE 2 Performance of our algorithm on a data set with increasing amount of Gaussian noise relative to the element size. #C is the number of detected constraints.

Level of noise	#C	P	R	F
0.00	321	1.000	1.000	1.000
0.02	321	1.000	1.000	1.000
0.04	319	1.000	0.993	0.996
0.06	297	1.000	0.915	0.956
0.08	290	1.000	0.894	0.944
0.10	263	1.000	0.795	0.886

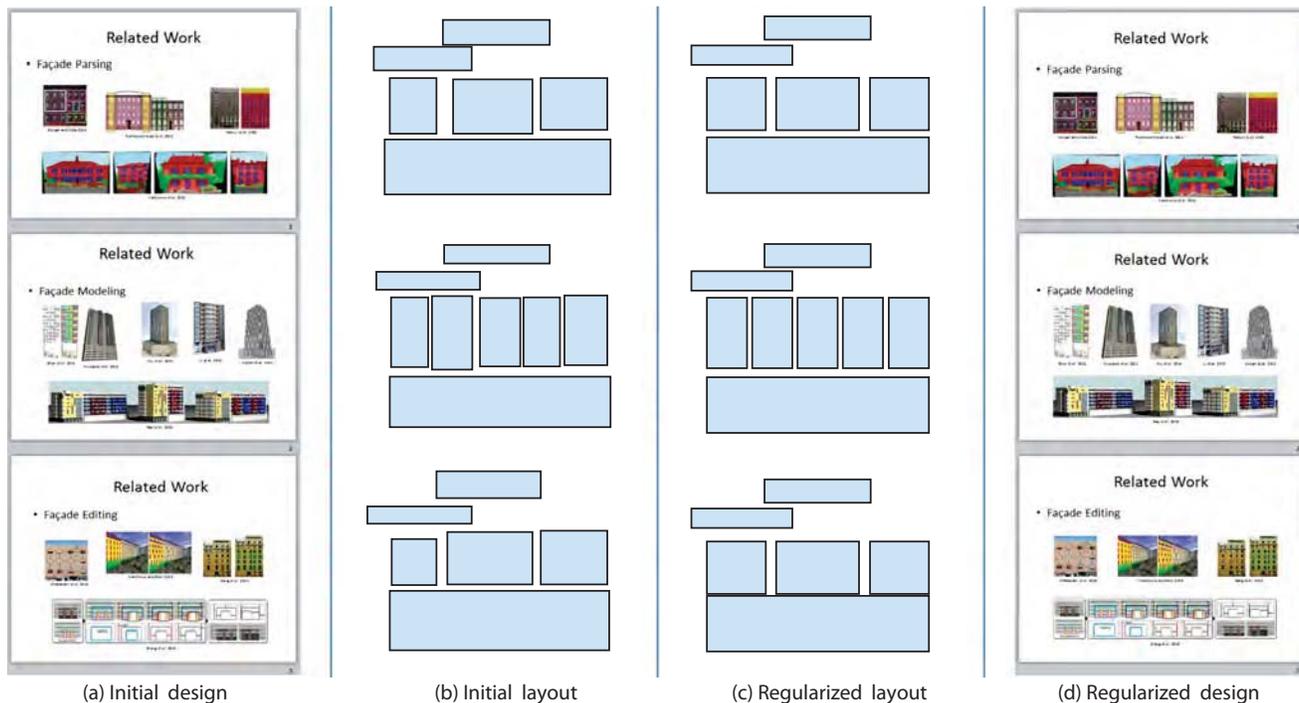


Fig. 7 Slide design beautified using our approach. From left to right: the initial design, bounding boxes of the elements in the design as input layout, optimized layout, and the final design.

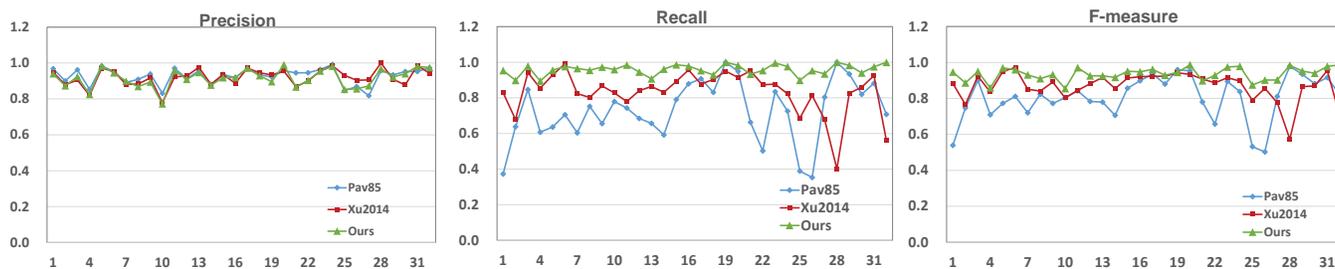


Fig. 8 The comparison of precision (left), recall (middle), and F-measure (right) of our method with Pav85 [5] and Xu2014 [6] on the alignment constraints.

TABLE 3 Performance of our algorithm on a data set with an increasing of number of rows and columns. Note that all the grid elements are perturbed by 2% Gaussian noise (relative to the element sizes).

Grid size	#C	P	R	F	Time(s)
5 × 8	321	1	1	1	2.245
10 × 8	678	0.987	0.983	0.985	6.428
5 × 16	676	0.975	0.986	0.981	6.996
10 × 16	1420	0.964	0.971	0.967	25.789
20 × 16	2940	0.947	0.964	0.955	121.822

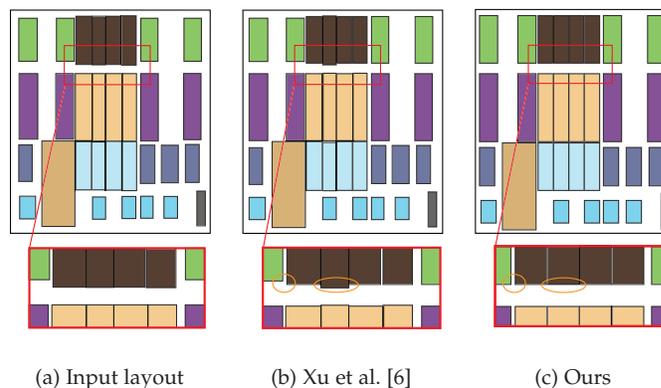


Fig. 9 A comparison of Xu et al. [6](b) and our method (c). The yellow circles indicate the differences.

512 the sparsity term. Here, we evaluate the performance with
 513 respect to the sparsity term w_a as shown in Fig. 11. The
 514 sparsity term plays an important role for selecting a trade
 515 off between precision and recall.

516 **Applications.** Our method is designed for general 2D
 517 layouts. One application is the regularization of digitized
 518 layouts, e.g., facade layouts shown in Fig. 6. Another ap-520 slide design (see Fig. 7), poster design, and other graphical

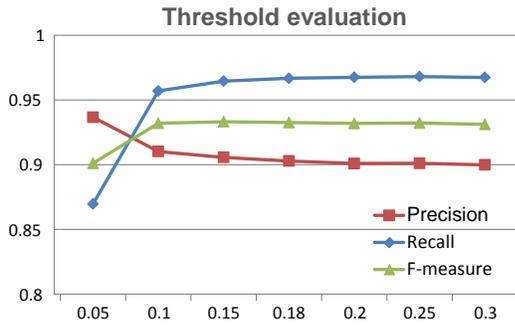


Fig. 10 The robustness of our method with respect to the threshold t_a . We show the change in average precision, recall, and F-measure for the alignment threshold uniformly sampled in the range $[0.05, 0.3]$.

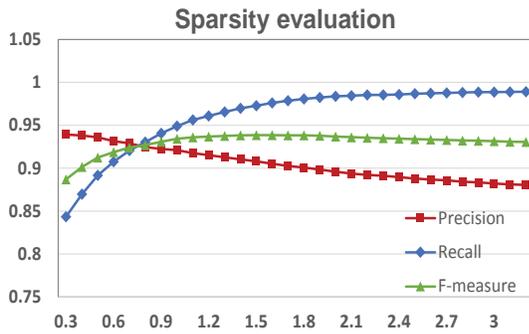


Fig. 11 The robustness of our method with respect to the sparsity term w_a .

521 designs (see Fig. 5).

522 **Extensions.** Our current implementation is developed for
 523 axis-aligned layouts, but we can extend our framework to
 524 consider more types of constraints and elements enclosed in
 525 oriented bounding boxes. In Fig. 12, the elements are dis-
 526 tributed on circles. For this example, we introduce two new
 527 types of constraints that consider spacing and alignment in
 528 this radial layouts. Our algorithm can be directly used for
 529 these constraints using polar coordinate system.

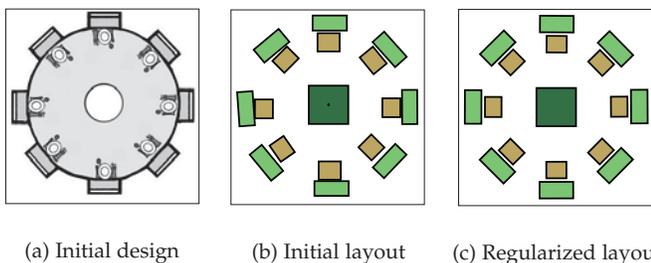


Fig. 12 An extension of our algorithm. In this example, elements (i.e., chairs or the tableware) are expected to be placed along concentric circles with same included angles. The black dot indicates the center of circles. (c) shows the result of our algorithm applied to this case by using a simple coordinate system conversion (from the Cartesian coordinate system to the polar coordinate system).

530 Another type of useful constraint is the same arc-length

531 constraint. The same arc length constraint enforces a con-
 532 stant arc length along a curve between two adjacent points
 533 that are sampled on this curve. In Fig. 13(a), we show a set of
 534 markers (the yellow squares) that are placed along the road
 535 centerline (in the yellow color). We can see that some adja-
 536 cent markers exhibit the same arc-length constraint. Directly
 537 fulfilling this constraint is difficult, considering that we do
 538 not know the curve function. We construct a map from a
 539 parameter vector to the points by a B-spline interpolation
 540 with chord length parameterization. Thus every parameter
 541 corresponds to a point, and the interval between two param-
 542 eters is equivalent to the chord length of two adjacent points.
 543 Then, we achieve the same arc-length by accomplishing
 544 the same spacing constraint on the parametric vectors. In
 545 Fig. 13(c), we show the result of this regularization. Another
 546 example is demonstrated in Fig. 6 of the supplemental
 547 materials.

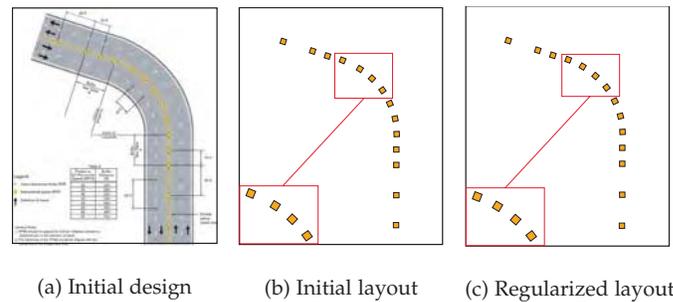


Fig. 13 The same arc-length distance constraint on points (the yellow squares). Our method successfully detects two kinds of arc length in this example and regularizes the curve points. Our framework can be applied to such input by constructing a parameterization of the points.

Our method does not fully explore the hierarchical struc-
 turing of constraints. However, we can still show such an
 example, where a given hierarchy defines the grouping
 information of elements (see Fig. 14). The regularization is
 achieved by applying our method from bottom to top.

553 **Limitations and future work.** Though our algorithm works
 554 well for most cases, we noticed that in some cases the result
 555 could be further improved with the availability of semantic
 556 information. For example, if there is an ornament on top of
 557 a window we can assume that there is a high probability
 558 that these two shapes are center aligned (see Fig. 15). Not
 559 using domain specific semantic priors is one limitation
 560 of our algorithm. Another limitation is that the possible
 561 constraints need to be known in advance. There is a large
 562 number of complex patterns, e.g., a set of elements being
 563 aligned along a spiral with regularly decreasing spacing,
 564 and it is unclear how our framework would perform if we
 565 would extend it using a large number of different complex
 566 constraint types. We consider this a very interesting avenue
 567 of future work. Further, we also plan to involve the user in
 568 the layout optimization stage to provide more control over
 569 the regularization process.

570 7 CONCLUSIONS

571 In this paper, we have presented an optimization-based ap-
 proach for regularizing general layouts. Our method takes

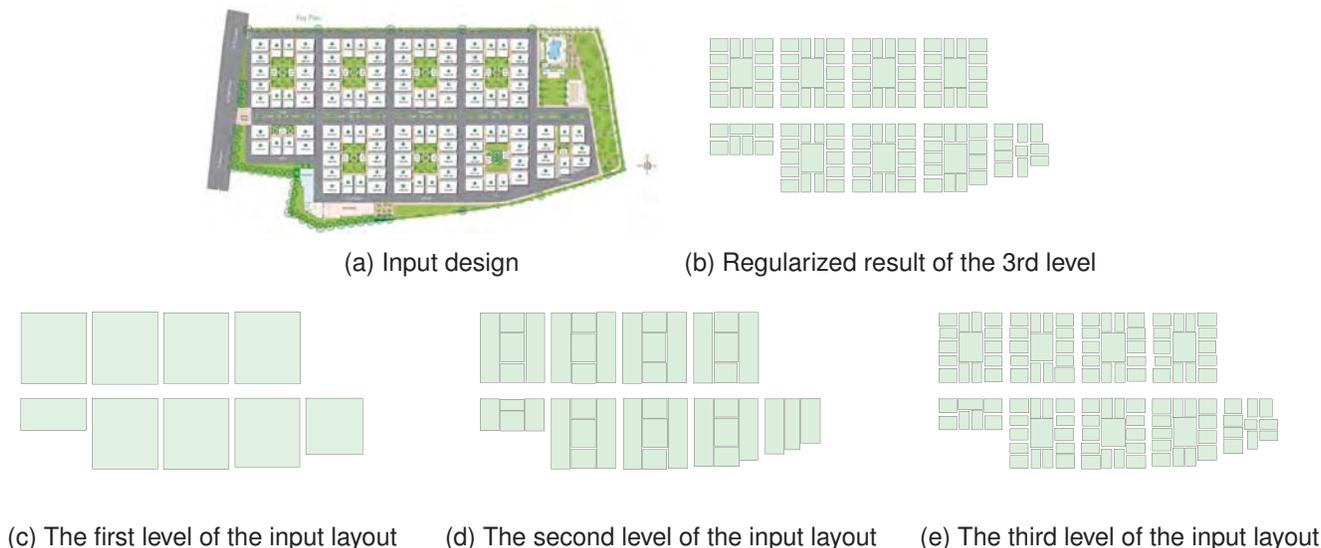


Fig. 14 The regularization of a hierarchical layout. The second row shows the hierarchy from top to down, which is marked by the user. We only use the marked hierarchy to define the group information of lower level layouts.

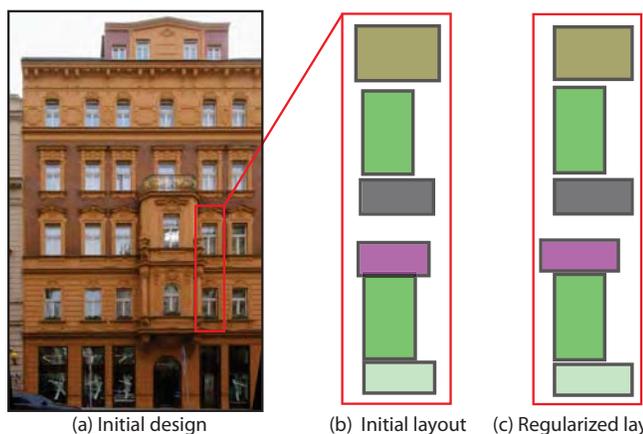


Fig. 15 A failure case of our algorithm. In this example, the user marks a wrong left edge of the ornaments below the windows in the highlighted region due to occlusions caused by perspective projection. Semantic prior information (e.g., an ornament and window are more likely to be center aligned) is necessary to correct this error.

as input a general layout represented as a set of labeled rectangles, and detects regularity constraints based on a linear integer programming formulation. The layout is regularized by minimizing the deformation of the initial layout while respecting the detected constraints. We have evaluated our method on various input layouts. Experimental results show that our method enforces the regularities in the layout, and is superior to alternative approaches in the literature. We have also shown the usefulness of our method for various applications.

ACKNOWLEDGMENTS

We would like to thank the reviewers for their helpful comments, and the authors of [6] for making their software public available and their help for the comparison. This

work was supported by the KAUST Visual Computing Center, the National Natural Science Foundation of China (61372168, 61331018, 61271431, and 61272327), and the U.S. National Science Foundation.

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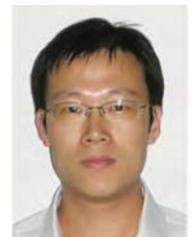
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