Radiomic Analysis of Imaging Heterogeneity in Tumours and the Surrounding Parenchyma Based on Unsupervised Decomposition of DCE-MRI for Predicting Molecular Subtypes of Breast Cancer

Ming Fan^{1#}, PhD, Peng Zhang^{1#}, BS, Yue Wang², PhD, Weijun Peng³, PhD, Shiwei Wang⁴, Xin Gao⁵, Maosheng Xu^{4*}, PhD, Lihua Li^{1*}, PhD

[#]Equal contributions

¹Institute of Biomedical Engineering and Instrumentation, Hangzhou Dianzi University, Hangzhou, China

²Department of Electrical and Computer Engineering, Virginia Polytechnic Institute and State University, Arlington, VA 22203, United States of America

³Department of Radiology, Fudan University Shanghai Cancer Center, Shanghai, China

⁴Department of Radiology, First Affiliated Hospital of Zhejiang Chinese Medical University, Hangzhou, Zhejiang, China

⁵King Abdullah University of Science and Technology (KAUST), Computational Bioscience Research Center (CBRC), Computer, Electrical and Mathematical Sciences and Engineering Division (CEMSE), Thuwal, 23955-6900, Saudi Arabia.

***Corresponding Author Info**

Maosheng Xu,

Phone: +86-571-87077785

Fax: +86-571-87077785

Email: 1243454330@qq.com

Lihua Li,

Phone: +86-571-86878587

Fax: +86-571-87713528

Email: lilh@hdu.edu.cn

Radiomic Analysis of Imaging Heterogeneity in Tumours and the Surrounding Parenchyma Based on Unsupervised Decomposition of DCE-MRI for Predicting Molecular Subtypes of Breast Cancer

Abstract

Objectives: This study aimed to predict the molecular subtypes of breast cancer via intratumoural and peritumoural radiomic analysis with subregion identification based on the decomposition of contrast-enhanced magnetic resonance imaging (DCE-MRI).

Methods: The study included 211 women with histopathologically confirmed breast cancer. We utilized a completely unsupervised convex analysis of mixtures (CAM) method by unmixing dynamic imaging series from heterogeneous tissues. Each tumour and the surrounding parenchyma were thus decomposed into multiple subregions, representing different vascular characterizations, from which radiomic features were extracted. A random forest model was trained and tested using a leave-one-out cross-validation (LOOCV) method to predict breast cancer subtypes. The predictive models from tumoural and peritumoural subregions were fused for classification.

Results: Tumour and peritumour DCE-MR images were decomposed into three compartments, representing plasma input, fast-flow kinetics and slow-flow kinetics. The tumour subregion related to fast-flow kinetics showed the best performance among the subregions for differentiating between patients with four molecular subtypes (area under the receiver operating characteristic curve (AUC)=0.832), exhibiting an AUC value significantly ($p<0.0001$) higher than that obtained with the entire tumour (AUC=0.719). When the tumour- and parenchyma-based predictive models were fused, the performance, measured as the AUC, increased to 0.897; this value was significantly higher than those obtained with other tumour partition methods.

Conclusions: Radiomic analysis of intratumoural and peritumoural heterogeneity based on the decomposition of image time-series signals has the potential to more accurately identify tumour kinetic features and serve as a valuable clinical marker to enhance the prediction of breast cancer subtypes.

Key points:

Decomposition of image time-series signals has the potential to more accurately identify tumour kinetic features.

Fusion of intratumoural- and peritumoural-based predictive models improves the prediction of breast cancer subtypes.

Key words:

Breast Neoplasms; Magnetic Resonance Imaging; Diagnostic Imaging

Abbreviations:

CAM Convex analysis of mixtures

NAC Neoadjuvant chemotherapy

PVE Partial-volume effect

KPC Kinetic pattern clustering

GLCM Grey level co-occurrence matrix

TTP Time-to-peak

PER Peak enhancement rate

WIS Wash-in-slope

WOS Wash-out-slope

Introduction

Tumour heterogeneity is common in breast cancer and confers a poor prognosis, results in a worse response to therapy, and promotes metastasis [1], impeding accurate characterization of the tumour. Dynamic contrast-enhanced magnetic resonance imaging (DCE-MRI) is sensitive to physiological changes (e.g., blood flow) in the underlying tissue and is well-suited to evaluate the extent of tumour angiogenesis and tumour heterogeneity by analysing patterns of enhancement [2; 3], which may reflect underlying genetic heterogeneity. Radiomic analyses of DCE-MRI have identified image biomarkers, such as a feature reflecting the heterogeneity of grey level distribution, to discriminate between breast cancers with different histopathological subtypes [4-8] and treatment responses [9]. Recent studies have evaluated intratumour imaging heterogeneity by partitioning the tumour into separate areas with varied dynamic enhancement patterns for better classification of tumour subtypes or prediction of responses to neoadjuvant chemotherapy (NAC) in breast cancer [10-13]. Emerging studies also suggest that image heterogeneity in the breast parenchyma that surrounds the tumour contributes to the discrimination of tumour subtypes or pathological stage [13-15].

These partitioning-based studies attempted to divide the tumour into non-overlapping regions according to voxel kinetic features. Due to the limited imaging resolution in DCE-MRI, however, the observed voxel, composed of multiple distinct dynamic patterns in a breast tumour, may be a reflection of the pixel-wise spatially mixed partial-volume effect (PVE) [16]. That is, a certain voxel may belong to a variety of kinetic features. As a consequence, some tumour regions are likely to contain activity representing a mixture of biological characteristics, which may lead to incorrect estimation of the dynamic enhancement pattern. Previous studies have proposed identifying the tumour tissue exhibiting a unique kinetic pattern using an unsupervised method for deconvoluting a dynamic imaging series [17; 18] or gene expression data [19; 20]. These image decomposition methods are advantageous because they more accurately evaluate vascular heterogeneity and identify changes in tumours [17; 21]. Despite the improvements associated with image decomposition, whether radiomic analysis of vascular structures is better than partitioning-based methods for characterizing and predicting breast cancer subtypes remains unclear. In addition to examining the tumour itself, verification is needed to determine whether imaging heterogeneity in the surrounding parenchyma can be used as a predictor of breast cancer subtypes based on the observation that the microenvironment around the tumour is spatially heterogeneous [22].

In this context, this study aimed to perform radiomic analyses of various vascular structures in breast tumours and surrounding parenchymal subregions using a decomposition method to identify dynamic characteristics with high accuracy and thus refine the prediction of breast cancer molecular subtypes.

Methods

Subjects

A total of 605 biopsy samples indicating invasive breast cancer were initially collected in our dataset between January 2013 and July 2014. Of these patients, 71 had incomplete MR sequence data and 278 had no available immunohistochemical data and were thus excluded from the dataset. Patients (n=20) who underwent surgical excision, radiation therapy or NAC before MRI examination were excluded. Twenty-six patients were excluded because they had no obvious tumour lesion. Thus, the final dataset included 211 women with a mean age of 52.4 years and an age range of 29-84 years.

MR imaging parameters

All breast MR examinations were performed with a 3.0-T system (Siemens Medical Systems) fitted with a dedicated eight-channel breast array coil with the patient placed in the prone position. DCE-MRI included one precontrast image acquisition and five postcontrast bilateral sagittal image acquisitions performed with a fat-suppressed T1-weighted three-dimensional sequence. The following parameters were used: 4.51 ms repetition time [TR], 1.61 ms echo time [TE], 448×448 matrix, 10° flip angle, 340×340 mm field of view, and 0.759×0.759 mm in-plane resolution. A bolus of 0.2 mmol/kg gadobutrol was intravenously injected by using an MR imaging-compatible power injector at a rate of 2 mL/second. The time between contrast material injection and the start of the first postcontrast acquisition was 60 seconds. Five contrast-enhanced images were then obtained with a temporal resolution of 60 seconds.

Image preprocessing

The location of the centre of the suspicious breast tumour was first annotated in each case retrospectively via consensus between two radiologists (*BLINDED*) with more than 10 years of experience. Image segmentation was performed on the third postcontrast series for all cases using a spatial fuzzy C-means (FCM) algorithm [23]. The breast MR images acquired from sequential MR imaging scans were registered as previously reported [23]. Fibroglandular tissue was segmented using an FCM clustering procedure on the MR image, excluding the skin and fatty tissue from the breast [6]. Images were segmented into the tumoural and peritumoural parenchymal regions. Similar to previous studies [24], the peritumoural shell of the surrounding tumour margin was approximately 20 mm with 26 pixels, and the in-plane resolution was 0.795 mm (0.795×26=19.73 mm).

Convex analysis of mixtures (CAM)-based shell decomposition of tumours and the surrounding parenchyma

The measured temporal signals of dynamic enhancement for each voxel i , i.e., $x(i)$, can be expressed as a nonnegative linear combination of the tissue-specific compartmental time-series curves $a_j(t)$, weighted by the relative tissue type proportions $K_j(i)$ at that pixel, which is defined in the following equation:

$$x(i)_{measured} = \{\sum_{j=1}^J K_j(i) a_j \mid K_j(i) \geq 0, \sum_{j=1}^J K_j(i) = 1, i = 1, \dots, N\},$$

where a_j is the vector notation of $a_j(t)$ over time and J is the number of functional tissue compartments, reflecting distinct kinetic patterns (detailed description in the Supplementary material).

By applying this method, the pixel time-series curves are decomposed into different tissue-specific compartments, for which high, moderate and low enhancement rates represent plasma input, fast-flow kinetics and slow-flow kinetics, respectively [17]. An image pixel i was determined as the J^{th} compartment if the value of the relative tissue type proportions $K_j(i)$ was nontrivial (i.e., larger than $1e-3$).

Tumour partitioning methods for comparison with CAM

In addition to the image decomposition method described above, we included other tumour partitioning-based methods that divided the breast tumour into subregions at all slices by clustering pixels according to the kinetic pattern clustering (*KPC*), time-to-peak (*TTP*), peak enhancement rate (*PER*) [10] wash-in-slope (*WIS*) and wash-out-slope (*WOS*) values [25]. Detailed descriptions of these methods are shown in the Supplementary material.

Feature extraction

To evaluate tumour heterogeneity based on signal distribution, imaging features, including ten statistical measurements consisting of the mean, minimum, maximum, median, variance, interquartile range (IQR), range, skewness, kurtosis and entropy of pixel values, were evaluated. A total of 19 volumetric texture features were calculated from the grey level co-occurrence matrix (GLCM), including contrast, correlation, energy, homogeneity, entropy, sum of squares variance, sum average, sum variance, sum entropy, difference variance, difference entropy, information correlation 1, information correlation 2, autocorrelation, dissimilarity, cluster shade, cluster prominence, maximum probability and inverse difference. Finally, four morphological features—surface area, volume, ratio between the surface area and volume, and compactness—were evaluated. We also evaluated the tumour longest diameter and three-dimensional parenchymal density [26] features for comparison with the predictive model. From the MRI sequential scans, imaging features were extracted from the precontrast series and from the difference between the intermediate (i.e., third) or last (fifth) postcontrast sagittal fat-suppressed T1-weighted MR image sequences and the precontrast series.

Pathological evaluation

The expression statuses of oestrogen receptor (ER), progesterone receptor (PR), human epidermal growth factor receptor type 2 (HER2) and Ki-67 were determined by using streptavidin-peroxidase (SP) immunohistochemistry (IHC) analysis. The ER and PR statuses were assessed by the nuclear staining intensity and the proportion of positively stained nuclei [20]. Breast cancer subtypes were determined as follows: 1) luminal A, ER/PR-positive, and HER2-negative; 2) luminal B, ER/PR-positive, and HER2-positive; 3) HER2, ER- and PR-negative, and HER2-positive; and 4) basal-like, ER-, PR-, and HER2-negative. Additionally, luminal subtypes with high Ki-67 expression were determined to be luminal B.

Statistical analysis

Differences in categorical variables (menopausal status, family history and tumour type) between molecular subtype characteristics were assessed using the χ^2 test or Fisher's exact test if the expected frequency in any cell of the table was less than five. Statistical

differences in tumour volume between the histopathology groups were evaluated by analysis of variance (ANOVA). The Kruskal-Wallis test was performed to evaluate group differences in the imaging features among the four molecular subtypes. The Bonferroni method was used to adjust for multiple statistical testing.

We employed the random forest method for multiclass classification, which yields more stable predictions than single estimator methods by bootstrapping training data and averaging the resulting tree-based predictions [27]. A nested leave-one-out cross-validation (LOOCV) method was used to evaluate model performance. The outer loop estimated a prediction score for the testing, while the inner loop was used to optimize parameters of the random forest model for optimal performance using gridsearch in combination with ten-fold cross-validation on the training data. The importance of the image features was evaluated by averaging the importance index obtained by the mean decrease in the Gini score of the random forest over all of the LOOCV loops. The receiver operating characteristic (ROC) curve was analysed, and the area under the curve (AUC) was assessed.

We assumed that the predictions based on various tumour or peritumour subregions were complementary and that combining them may efficiently increase the prediction accuracy. More specifically, the weight for each predictive score was determined by the accuracy of the classifier in the ten-fold cross-validation for each LOOCV circle.

MATLAB software (2015a MathWorks Inc) was used for all data analyses. $p < 0.05$ was considered indicative of a statistically significant difference.

Results

Patient characteristics

The histological types of invasive breast cancers were categorized as follows: invasive ductal carcinoma ($n=170$, 81.0%), invasive lobular carcinoma ($n=6$, 2.9%), invasive papillary carcinoma ($n=2$, 1.0%), mucinous carcinoma ($n=4$, 1.9%), medullary carcinoma ($n=1$, 0.5%), and apocrine carcinoma ($n=1$, 0.5%). Statistical tests showed no significant differences regarding histological types ($p=0.5151$), age ($p=0.1191$), maximum diameter ($p=0.1312$), menopausal status ($p=0.1234$) or three-dimensional MRI parenchymal density ($p=0.2330$) among the four breast cancer subtypes (Table 1).

Intratumoural heterogeneity identified by CAM

Based on the CAM analysis, breast tumours and surrounding parenchymal tissues were decomposed into three regions representing the following distinct spatial patterns of dynamic enhancement in vascular compartments: input plasma, fast-flow kinetics and slow-flow kinetics (Figure 1a-c). Among all dynamic curves, kinetics related to plasma input showed a pattern of rapid wash-in and fast wash-out (Figure 1d). The dynamic curves for the overlapped regions showed distinct kinetic patterns for these areas (Figure 1e). Similarly, the dynamic kinetics of the parenchyma are shown in Figure 2. Additionally, an example of CAM applied to an image of a luminal B tumour and its parenchymal regions are shown in Supplementary Figures S1 and S2, respectively.

Statistical analysis of imaging features

The results of the Kruskal-Wallis test for multiple comparisons of DCE-MRI features

among the four molecular subtypes are shown in Supplementary Table S1. Figure 3 illustrates the distribution of the dissimilarity imaging feature for the third postcontrast imaging series (Bonferroni corrected p -value <0.0001) in the whole tumour and the subregion representing a fast enhancement rate. The texture feature of the inverse difference showed significant differences among the four subtypes in the whole tumour (corrected $p=0.0011$) and the tumour subregion related to fast-flow kinetics (corrected $p<0.0001$). It is interesting to note that these texture features in the tumour subregions showed an overall increased level of heterogeneity and more significant differences with lower p -values than those in the whole tumour. The distributions of the statistical features of skewness and kurtosis are shown in Supplementary Figure S3. The luminal A subtype showed the highest values for these features, while HER2 exhibited the lowest values. In the tumour subregion, the same features showed greater differences among the four subtypes, with a more highly significant p -value. Tumours of the luminal B type showed negative values for skewness, while luminal A tumours showed low values. The ranked importance of features in leave-one-out cycles are represented in Supplementary Table S2.

Prediction of tumoural and peritumoural parenchymal subregions based on CAM

We also evaluated predictive model performance using features from the tumoural and peritumoural parenchymal subregions. The predictive model was evaluated to explore its association with the tumour IHC subtype, taking into account imaging features; the ROC is shown in Figure 4. Table 2 shows the performances of these variables in multivariate models, in which the tumour subregion related to fast-flow kinetics had the strongest predictive power, with an AUC of 0.832 and a 95% confidence interval (CI) from 0.794 to 0.870. Moreover, all models established with the three subregions were significantly better ($p<0.05$) than that based on the entire tumour (AUC=0.719) in terms of demonstrating an association with tumour IHC subtypes. We also evaluated the predictive model using the additional features of tumour maximum size and breast density separately, and the results are shown in Supplementary Table S3 and S4, respectively. However, the models with the additional tumour maximum size and breast density features exhibited performances (in terms of AUC values) nearly identical to those of the original models ($p>0.05$).

A predictive model of the parenchymal region was also established, with an AUC of 0.666, which was lower than that of the entire tumour. Using features from the parenchymal subregions, the performance values (in terms of AUC) were significantly increased to 0.782, 0.768, and 0.785 for the regions related to plasma input, fast-flow kinetics and slow-flow kinetics, respectively (Table 2).

Multimodel fusion analysis to discriminate among breast cancer subtypes

We also fused the predictive models from the tumoural and peritumoural parenchymal subregions to discriminate the four molecular subtypes (Table 3). Fusion of the predictions from the tumour subregions representing plasma input, fast-flow kinetics and slow-flow kinetics showed an AUC of 0.853, which was better than that of the parenchymal regions, which had an AUC of 0.802. When the predictive models of the tumour subregions and parenchymal regions were fused, we obtained an AUC of 0.897,

which was significantly higher than those obtained for all other methods (Table 3).

In addition, we segmented tumours into subregions based on five tumour partitioning methods: KPC, TTP, PEK, WIS and WOS; the kinetics of the nonoverlapped subregions are shown in Figure 5. The predictive models for these methods were established and fused, and their AUCs are shown in Table 3. These methods exhibited significantly better performances in terms of AUC values than the method using the whole tumour (Table 4). No significant differences in AUC values were observed among these methods. However, KPC, TTP, TEK, WIS and WOS showed significantly lower performances than the predictive fusion model using features from tumour subregions identified by CAM, with p -values of 0.0167, 0.0093, 0.0005, <0.0001 and <0.0001, respectively.

Discussion

We have presented a heterogeneity analysis employing a CAM-based decomposition method for the tumour and surrounding parenchyma to predict breast cancer subtypes. Based on this method, intratumoural radiomic analysis had significantly better predictive power than the entire tumour and other tumour segmentation methods. When predictive models from the tumour and parenchyma were fused, the fusion predictive model achieved the highest performance. Unlike conventional intratumoural analysis [10; 11; 25; 28], this study eliminated the PVE and identified tumour subregions based on tissue-specific kinetic characteristics, which was theoretically supported by a well-grounded mathematical framework [29]. Furthermore, this method was conducted without any type of external information, making it sufficiently sensitive to detect dynamic heterogeneity in time-series image data.

Previous studies have identified radiomic biomarkers associated with the histological characteristics of breast cancer, focusing on the extent of the tumour itself [6; 7; 28; 30-32]. Based on intratumoural radiomic analysis, studies have reported that contrast enhancement patterns in intratumoural regions correlate with clinical and histological characteristics [10; 11; 25; 33]. Our study was conducted based on the observation that tumour heterogeneity and subregions with differing biologies are more beneficial than approaches that use biomarkers obtained from an average function of the entire tumour [34]. The results also showed improved performance of the fusion model (in terms of AUC) compared with that based on the entire tumour, implying that features within tumour subregions, rather than the tumour itself, provide the majority of cancer-related characteristics.

In addition to the intratumoural analysis, we conducted an analysis of mixtures in the parenchymal environment immediately surrounding the tumour. DCE-MRI features in the bulk parenchyma have been shown to associate with breast cancer subtypes or prognostic factors [9; 24; 28; 35]. We observed that the parenchymal densities on MRI were not significantly different among breast cancer subtypes, and the performances of the predictive models with or without this variable were not significantly different in terms of AUC values. Although we observed a relatively low level of prediction accuracy using features from the parenchymal region, the predictive models derived from decomposed subregions were significantly improved compared to those derived

from the entire peritumoural parenchyma. This region may provide unique, orthogonal radiomic signatures that enable enhanced prediction of breast cancer subtypes. The results also demonstrated that a radiomic approach involving the fusion of intratumoural and peritumoural characteristics efficiently increased the prediction accuracy, indicating that predictions across the tumour and the microenvironment are complementary.

The strengths of our study include the uniform protocol for the acquisition of DCE-MR imaging across patients. Unlike other studies that performed intratumoural analysis based on clustering analysis [11; 12], we separated pixels with spatially mixed PVEs by conducting a convex analysis of each pixel with a time-series dynamic enhancement to achieve a better functional representation of the tumour and the surrounding parenchyma to predict breast cancer subtypes. In our experiments, the performance of the CAM-based method (in terms of AUC value) was significantly better than those of other clustering methods, i.e., KPC, TTP, PEK, WIS, and WOS.

In this study, texture and statistical features were analysed, and the feature of dissimilarity in the third enhancement in the tumour subregion related to fast kinetics showed the best individual performance and was ranked as the most important feature in a predictive model. Specifically, the overall highest values of this feature were observed in luminal A tumours, whereas values were the lowest in HER2 tumours. This feature quantifies image heterogeneity, reflecting differences in GLCM elements. A high dissimilarity reflects a high level of overall difference between image pixels.

Despite some significant findings, the work presented herein has limitations. First, this image decomposition method requires a relatively high temporal resolution, and applying this method to DCE-MR images is difficult with limited time-series data (i.e., less than three postcontrast series). Second, it would be of interest to perform intratumoural analysis based on other imaging modalities, such as DW-MRI [36] and T2-weighted imaging [37], to validate and extend this work. Third, the tumour sizes in this dataset were larger than 1 cm, and more studies with smaller tumour sizes should be performed. Fourth, it would also be worthwhile to validate the CAM-based tumour decomposition method by using an additional dataset with a different scanning protocol to test the robustness of the model.

In conclusion, intratumoural and peritumoural MR image decomposition identified breast tumour and parenchymal subregions in which DCE-MRI features were used as predictors specifically to classify molecular subtypes of breast cancer. In addition to breast tumours, this analysis framework could be applied to images of other types of cancer. These findings potentially have clinical benefits because they could help enable a clinical platform for the prediction of breast cancer subtypes that would allow identification of patients for more specific/individualized therapies without formal biopsy analysis. Additional work is needed before these methods can be utilized to facilitate the noninvasive assessment of breast cancer histopathological characteristics in clinical practice.

References

1. Koren, S. & Bentires-Alj, M. (2015) Breast Tumor Heterogeneity: Source of Fitness, Hurdle for Therapy. *Mol Cell* 60: 537-546.
2. Kuhl, C.K. & Schild, H.H. (2000) Dynamic image interpretation of MRI of the breast. *J Magn Reson Imaging* 12: 965-974.
3. Karahaliou, A., Vassiou, K., Arikidis, N.S., Skiadopoulos, S., Kanavou, T. & Costaridou, L. (2010) Assessing heterogeneity of lesion enhancement kinetics in dynamic contrast-enhanced MRI for breast cancer diagnosis. *Br J Radiol* 83: 296-309.
4. Wan, T., Bloch, B.N., Plecha, D., Thompson, C.L., Gilmore, H., Jaffe, C., et al (2016) A Radiogenomics Approach for Identifying High Risk Estrogen Receptor-positive Breast Cancers on DCE-MRI: Preliminary Results in Predicting OncotypeDX Risk Scores. *Sci Rep* 6: 21394.
5. Chang, R.F., Chen, H.H., Chang, Y.C., Huang, C.S., Chen, J.H. & Lo, C.M. (2016) Quantification of breast tumor heterogeneity for ER status, HER2 status, and TN molecular subtype evaluation on DCE-MRI. *Magn Reson Imaging* 34: 809-819.
6. *BLINDED*
7. Sutton, E.J., Dashevsky, B.Z., Oh, J.H., Veeraraghavan, H., Apte, A.P., Thakur, S.B., et al (2016) Breast cancer molecular subtype classifier that incorporates MRI features. *J Magn Reson Imaging*.
8. Wu, J., Cui, Y., Sun, X., Cao, G., Li, B., Ikeda, D.M., et al (2017) Unsupervised Clustering of Quantitative Image Phenotypes Reveals Breast Cancer Subtypes with Distinct Prognoses and Molecular Pathways. *Clin Cancer Res* 23: 3334-3342.
9. Fan, M., Wu, G., Cheng, H., Zhang, J., Shao, G. & Li, L. (2017) Radiomic analysis of DCE-MRI for prediction of response to neoadjuvant chemotherapy in breast cancer patients. *Eur J Radiol* 94: 140-147.
10. *BLINDED*
11. Chaudhury, B., Zhou, M., Goldgof, D.B., Hall, L.O., Gatenby, R.A., Gillies, R.J., et al (2015) Heterogeneity in intratumoral regions with rapid gadolinium washout correlates with estrogen receptor status and nodal metastasis. *J Magn Reson Imaging* 42: 1421-1430.
12. Wu, J., Gong, G., Cui, Y. & Li, R. (2016) Intratumor partitioning and texture analysis of dynamic contrast-enhanced (DCE)-MRI identifies relevant tumor subregions to predict pathological response of breast cancer to neoadjuvant chemotherapy. *J Magn Reson Imaging* 44: 1107-1115.
13. Braman, N.M., Etesami, M., Prasanna, P., Dubchuk, C., Gilmore, H., Tiwari, P., et al (2017) Intratumoral and peritumoral radiomics for the pretreatment prediction of pathological complete response to neoadjuvant chemotherapy based on breast DCE-MRI. *Breast Cancer Res* 19: 57.
14. Fan, M., He, T., Zhang, P., Zhang, J. & Li, L. (2017) Heterogeneity of Diffusion-Weighted Imaging in Tumours and the Surrounding Stroma for Prediction of Ki-67 Proliferation Status in Breast Cancer. *Sci Rep* 7: 2875.
15. Burnside, E.S., Drukker, K., Li, H., Bonaccio, E., Zuley, M., Ganott, M., et al (2016) Using computer-extracted image phenotypes from tumors on breast magnetic resonance imaging to predict breast cancer pathologic stage. *Cancer* 122: 748-757.
16. Chen, L., Choyke, P.L., Chan, T.H., Chi, C.Y., Wang, G. & Wang, Y. (2011) Tissue-specific compartmental analysis for dynamic contrast-enhanced MR imaging of complex tumors. *IEEE*

- Trans Med Imaging 30: 2044-2058.
17. Chen, L., Choyke, P.L., Wang, N., Clarke, R., Bhujwalla, Z.M., Hillman, E.M., et al (2014) Unsupervised deconvolution of dynamic imaging reveals intratumor vascular heterogeneity and repopulation dynamics. PLoS One 9: e112143.
 18. Chen, L., Chan, T.H., Choyke, P.L., Hillman, E.M., Chi, C.Y., Bhujwalla, Z.M., et al (2011) CAM-CM: a signal deconvolution tool for in vivo dynamic contrast-enhanced imaging of complex tissues. Bioinformatics 27: 2607-2609.
 19. Wang, N., Gong, T., Clarke, R., Chen, L., Shih le, M., Zhang, Z., et al (2015) UNDO: a Bioconductor R package for unsupervised deconvolution of mixed gene expressions in tumor samples. Bioinformatics 31: 137-139.
 20. Hammond, M.E., Hayes, D.F., Wolff, A.C., Mangu, P.B. & Temin, S. (2010) American society of clinical oncology/college of american pathologists guideline recommendations for immunohistochemical testing of estrogen and progesterone receptors in breast cancer. J Oncol Pract 6: 195-197.
 21. Ambikapathi, A., Chan, T.H., Lin, C.H., Yang, F.S., Chi, C.Y. & Wang, Y. (2016) Convex-Optimization-Based Compartmental Pharmacokinetic Analysis for Prostate Tumor Characterization Using DCE-MRI. IEEE Trans Biomed Eng 63: 707-720.
 22. Yili, Z., Xiaoyan, H., Hongwen, D., Yun, Z., Xin, C., Peng, W., et al (2009) The value of diffusion-weighted imaging in assessing the ADC changes of tissues adjacent to breast carcinoma. BMC Cancer 9: 18.
 23. Yang, Q., Li, L., Zhang, J., Shao, G., Zhang, C. & Zheng, B. (2014) Computer-aided diagnosis of breast DCE-MRI images using bilateral asymmetry of contrast enhancement between two breasts. J Digit Imaging 27: 152-160.
 24. Wu, J., Li, B., Sun, X., Cao, G., Rubin, D.L., Napel, S., et al (2017) Heterogeneous Enhancement Patterns of Tumor-adjacent Parenchyma at MR Imaging Are Associated with Dysregulated Signaling Pathways and Poor Survival in Breast Cancer. Radiology 285: 401-413.
 25. Ashraf, A., Gaonkar, B., Mies, C., DeMichele, A., Rosen, M., Davatzikos, C., et al (2015) Breast DCE-MRI Kinetic Heterogeneity Tumor Markers: Preliminary Associations With Neoadjuvant Chemotherapy Response. Transl Oncol 8: 154-162.
 26. Nie, K., Chen, J.H., Chan, S., Chau, M.K., Yu, H.J., Bahri, S., et al (2008) Development of a quantitative method for analysis of breast density based on three-dimensional breast MRI. Med Phys 35: 5253-5262.
 27. Breiman, L. (2001) Random Forests. Machine Learning 45: 5-32.
 28. Wu, S., Berg, W.A., Zuley, M.L., Kurland, B.F., Jankowitz, R.C., Nishikawa, R., et al (2016) Breast MRI contrast enhancement kinetics of normal parenchyma correlate with presence of breast cancer. Breast Cancer Res 18: 76.
 29. Wang, N., Hoffman, E.P., Chen, L., Zhang, Z., Liu, C., Yu, G., et al (2016) Mathematical modelling of transcriptional heterogeneity identifies novel markers and subpopulations in complex tissues. Sci Rep 6: 18909.
 30. Mazurowski, M.A., Zhang, J., Grimm, L.J., Yoon, S.C. & Silber, J.I. (2014) Radiogenomic analysis of breast cancer: luminal B molecular subtype is associated with enhancement dynamics at MR imaging. Radiology 273: 365-372.
 31. Grimm, L.J., Zhang, J. & Mazurowski, M.A. (2015) Computational approach to radiogenomics of breast cancer: Luminal A and luminal B molecular subtypes are associated with imaging

- features on routine breast MRI extracted using computer vision algorithms. *J Magn Reson Imaging* 42: 902-907.
32. Wu, J., Sun, X.L., Wang, J., Cui, Y., Kato, F., Shirato, H., et al (2017) Identifying Relations Between Imaging Phenotypes and Molecular Subtypes of Breast Cancer: Model Discovery and External Validation. *Journal of Magnetic Resonance Imaging* 46: 1017-1027.
 33. Yamaguchi, K., Abe, H., Newstead, G.M., Egashira, R., Nakazono, T., Imaizumi, T., et al (2015) Intratumoral heterogeneity of the distribution of kinetic parameters in breast cancer: comparison based on the molecular subtypes of invasive breast cancer. *Breast Cancer* 22: 496-502.
 34. O'Connor, J.P., Rose, C.J., Waterton, J.C., Carano, R.A., Parker, G.J. & Jackson, A. (2015) Imaging intratumor heterogeneity: role in therapy response, resistance, and clinical outcome. *Clin Cancer Res* 21: 249-257.
 35. Kim, J.Y., Kim, S.H., Kim, Y.J., Kang, B.J., An, Y.Y., Lee, A.W., et al (2015) Enhancement parameters on dynamic contrast enhanced breast MRI: do they correlate with prognostic factors and subtypes of breast cancers? *Magn Reson Imaging* 33: 72-80.
 36. Amornsiripanitch, N., Nguyen, V.T., Rahbar, H., Hippe, D.S., Gadi, V.K., Rendi, M.H., et al (2017) Diffusion-weighted MRI characteristics associated with prognostic pathological factors and recurrence risk in invasive ER+/HER2- breast cancers. *J Magn Reson Imaging*.
 37. Henderson, S., Purdie, C., Michie, C., Evans, A., Lerski, R., Johnston, M., et al (2017) Interim heterogeneity changes measured using entropy texture features on T2-weighted MRI at 3.0 T are associated with pathological response to neoadjuvant chemotherapy in primary breast cancer. *Eur Radiol* 27: 4602-4611.

Figure legends

Figure 1. Example of CAM applied to an image of a luminal A tumour in a 42-year-old woman. a) The tumour is decomposed into three regions, in which the blue, red and green colours represent the input plasma, fast-flow kinetics and slow-flow kinetics, respectively. b) Image pixels are grouped into clusters using an affinity propagation clustering method. The clusters represented by the vertices are identified by CAM. c) Images of the three associated regions represent input plasma, fast-flow kinetics and slow-flow kinetics, respectively. d) Dynamic enhancement curves for the tumour and three tumour subregions representing tissue-specific compartments. e) Dynamic enhancement curves for the overlapped tumour subregions, i.e., input and fast, input and slow, fast and slow, and the overlapping of all three regions.

Figure 2. Example of CAM applied to a parenchyma with a 2-cm width surrounding a luminal A subtype tumour in a 42-year-old woman. a) The parenchyma is decomposed into three regions, in which the blue, red and green colours represent the input plasma, fast-flow kinetics and slow-flow kinetics, respectively. B) Image pixels are grouped into clusters using an affinity propagation clustering method. The clusters represented by the vertices are identified by CAM. C) Images of the three associated regions represent input plasma, fast-flow kinetics and slow-flow kinetics, respectively. d) Dynamic enhancement curves for the parenchyma and three decomposed subregions representing tissue-specific compartments. e) Dynamic enhancement curves for the overlapped subregions, i.e., input and fast, input and slow, fast and slow, and the overlapping of all the three regions.

Figure 3. Boxplot of representative imaging features. a) Dissimilarity in the third enhancement in the entire tumour. b) Dissimilarity in the third enhancement in the tumour subregion associated with fast-flow kinetics. c) Inverse difference in the third enhancement sequence in the entire tumour. d) Inverse difference in the third enhancement sequence in the tumour subregion related to plasma input.

Figure 4. ROC plots of the multivariate model involving the fusion of all three tumour subregions for a) luminal A, b) luminal B, c) HER2 and d) basal-like tumours.

Figure 5. Illustration of intratumour analysis results based on CAM and five other methods for one luminal B case. Tumour subregions decomposed by CAM and the corresponding kinetic curves are shown in a); the blue, red and green colours represent plasma input, fast-flow kinetics and slow-flow kinetics, respectively. Tumours and the kinetics of the subregions partitioned by KPC, TTP, PEK, WIS and WOS are shown in b, c, d, e and f, respectively.

Table legends

Table 1. Tumour characteristics

Table 2. Performance of the predictive model using features obtained from the tumour and surrounding parenchyma

Table 3. Fusion of the predictive models from CAM-based analysis and partition-based methods

Table 4. Comparison of AUCs between CAM analyses and other partition-based methods

Supplementary methods

Convex analysis of mixtures (CAM)-based shell decomposition of tumours and the surrounding parenchyma

This method first applies clustering of voxels into an optimal number of representative and robust clusters, i.e., $\{x_m\}$, using affinity propagation clustering and expectation–maximization mixture model fitting [1]. To identify the vertices of a convex set $\mathcal{H}\{x_{measured}\}$, CAM was performed to automatically identify the pixel clusters spatially located at the corners of the clustered pixel time-series scatter simplex via a minimum error margin convex hull for data fitting:

$$\delta_{m,\{1,\dots,J\}\in C_J^M} = \min \|x_m - \sum_{j=1}^J a_j x_j\|_2, a_j \geq 0, \sum_{j=1}^J a_j = 1.$$

The most probable J vertices were estimated by optimizing the sum of the margin between the convex hull and the remaining “exterior” cluster centers to reach the minimum:

$$\hat{J} = \operatorname{argmin}_{\{1,\dots,J\}\in C_J^M} \sum_{m=1}^M \delta_{m,\{1,\dots,J\}\in C_J^M}.$$

Tumour partitioning methods for comparison with CAM

The KPC method was utilized to fully take advantage of features derived from kinetic curves by categorizing each pixel in the breast tumor and the surrounding parenchyma using K-means clustering based on the signals of all postcontrast series [2].

The PER was defined as the relative difference in each pixel value among image series, which is shown as follows:

$$\text{PER}(i) = \max \left\{ \frac{I_T(i) - I_0(i)}{I_0(i)} \right\}, T = \{1, 2, 3, 4, 5\},$$

where $I_T(i)$ represents the value of the i th-matched pixel in the T th image scan. Each breast tumor was divided into three regions by FCM clustering, representing the highest, moderate and lowest levels of the overall enhancement rate.

The TTP for each voxel within the tumor depicts the time at which peak enhancement was achieved, which was defined with the following equation:

$$\text{TTP}(i) = \operatorname{argmax}_T \left\{ \frac{I_T(i) - I_0(i)}{I_0(i)} \right\}, T = \{1, 2, 3, 4, 5\}.$$

Following the same procedures described in a previous study [2], pixel sets from the third, fourth and fifth series of postcontrast MR images were used to obtain peak enhancement values and were defined as early, moderate and late TTP, respectively.

The WIS reflects the rise in the uptake rate of the contrast agent when peak enhancement is achieved, which is shown by the following equation:

$$\text{WIS}(i) = \frac{I_{\text{TTP}(i)}(i) - I_0(i)}{S(\text{TTP}(i)) - S(0)},$$

where $S(0)$ is the time (seconds) at the precontrast series and $S(\text{TTP}(i))$ is the time at TTP. Each breast tumor was divided into three subregions by clustering the pixels

according to the value of the WIS .

The WOS reflects the drop in the contrast agent after peak enhancement is achieved, which is shown by the following equation:

$$WOS(i) = \frac{I_{TTP(i)}(i) - I_5(i)}{S(5) - S(TTP(i))},$$

where $S(5)$ is the time at the last time series. Each breast tumor was divided into three subregions by clustering the pixels according to the value of the WOS.

Supplementary Figures

Supplementary Figure S1. Example of CAM applied to an image of a luminal B tumour in a 56-year-old woman. a) Tumour image is decomposed into three regions, in which the blue, red and green colours represent the input plasma, fast-flow kinetics and slow-flow kinetics, respectively. b) Image pixels are grouped into clusters using an affinity propagation clustering method. The clusters represented by the vertices are identified by CAM. c) Images of the three associated regions represent input plasma, fast-flow kinetics and slow-flow kinetics, respectively. d) Dynamic enhancement curves for the tumour and three tumour subregions representing tissue-specific compartments. e) Dynamic enhancement curves for the overlapped tumour subregions, i.e., input and fast, input and slow, fast and slow, and the overlapping of all three regions.

Supplementary Figure S2. Example of CAM applied to a parenchyma with a 2-cm width surrounding a luminal B subtype tumour. a) The parenchyma is decomposed into three regions, in which the blue, red and green colours represent the input plasma, fast-flow kinetics and slow-flow kinetics, respectively. b) Image pixels are grouped into clusters using an affinity propagation clustering method. The clusters represented by the vertices are identified by CAM. c) Images of the three associated regions represent input plasma, fast-flow kinetics and slow-flow kinetics, respectively. d) Dynamic enhancement curves for the parenchyma and three decomposed subregions representing tissue-specific compartments. e) Dynamic enhancement curves for the overlapped subregions, i.e., input and fast, input and slow, fast and slow, and the overlapping of all the three regions.

Supplementary Figure S3. Boxplot of representative imaging features. a) Kurtosis in the third enhancement in the entire tumour. b) Kurtosis in the third enhancement in the tumour subregion associated with fast-flow kinetics. c) Skewness in the third enhancement sequence in the entire tumour. d) Skewness in the third enhancement sequence in the tumour subregion related to fast-flow kinetics.

Supplement Tables

Supplementary Table S1. Kruskal-wallis test for DCE-MRI features

Whole tumor	P value	Input	P value	Fast	P value	Slow	P value
Dissimilarity ^b	<0.0001	Dissimilarity ^b	<0.0001	Inverse difference ^b	<0.0001	Dissimilarity ^b	<0.0001
Homogeneity ^b	<0.0001	Inverse difference ^b	<0.0001	Compactness ^a	<0.0001	Inverse difference ^b	<0.0001
Surface area ^a	<0.0001	Homogeneity ^b	<0.0001	Homogeneity ^b	<0.0001	Homogeneity ^b	<0.0001
Contrast ^b	<0.0001	Compactness ^a	<0.0001	Surface area/Volume ^a	<0.0001	Compactness ^a	<0.0001
Homogeneity ^c	0.0001	Contrast ^b	<0.0001	Volume ^a	<0.0001	Volume ^a	<0.0001
Inverse difference ^c	0.0008	Difference entropy ^b	<0.0001	Dissimilarity ^b	<0.0001	Contrast ^b	<0.0001
Sum entropy ^b	0.0012	Volume ^a	<0.0001	Contrast ^b	<0.0001	Difference entropy ^b	<0.0001
Inverse difference ^b	0.0011	Dissimilarity ^a	<0.0001	Difference entropy ^b	<0.0001	Surface area/Volume ^a	<0.0001
Sum variance ^c	0.0103	Surface area ^a	<0.0001	Surface area ^a	<0.0001	Surface area ^a	<0.0001
Cluster prominence ^c	0.0104	Homogeneity ^a	<0.0001	Inverse difference ^c	<0.0001	Inverse difference ^a	<0.0001
Sum entropy ^c	0.0218	Difference variance ^a	<0.0001	Difference entropy ^a	0.0003	Dissimilarity ^c	<0.0001
Correlation ^a	0.0229	Energy ^b	<0.0001	Sum variance ^a	0.0010	Sum variance ^a	0.0001
Information correlation 1 ^a	0.0320	Sum variance ^a	<0.0001	Entropy ^a	0.0010	Difference entropy ^c	0.0002
Maximum probability ^b	0.0328	Entropy ^b	<0.0001	Sum entropy ^a	0.0014	Cluster prominence ^a	0.0008
Min ^a	0.0433	Difference variance ^c	0.0001	Maximum probability ^a	0.0016	Sum entropy ^a	0.0011
Sum variance ^b	0.0438	Cluster prominence ^a	0.0008	Cluster prominence ^a	0.0046	Difference variance ^c	0.0024
-	-	Maximum probability ^a	0.0012	Correlation ^a	0.0056	Entropy ^b	0.0035
-	-	Sum entropy ^a	0.0022	Kurtosis ^a	0.0093	Energy ^b	0.0075
-	-	Energy ^c	0.0038	Cluster prominence ^c	0.0110	Correlation ^b	0.0111
-	-	Sum variance ^c	0.0098	Energy ^b	0.0150	Kurtosis ^a	0.0150
-	-	Entropy ^c	0.0102	Correlation ^b	0.0164	Correlation ^a	0.0164
-	-	Sum variance ^b	0.0106	Energy ^c	0.0216	Cluster prominence ^b	0.0176
-	-	Sum entropy ^b	0.0111	Entropy ^b	0.0246	Sum variance ^c	0.0246

-	-	Sum entropy ^c	0.0213	Entropy ^c	0.0285	Sum variance ^b	0.0310
-	-	Correlation ^a	0.0287	Skewness ^b	0.0311	Cluster prominence ^c	0.0350
-	-	Kurtosis ^a	0.0326	Information correlation 2 ^c	0.0372	Skewness ^b	0.0464
-	-	Cluster prominence ^b	0.0330	Cluster prominence ^b	0.0405	-	-
-	-	Maximum probability ^b	0.0344	Sum entropy ^c	0.0497	-	-

^aFeature extracted in preconstrast series

^bFeature extracted in the third postcontrast series

^cFeature extracted in the fifth postcontrast series

Features with p-values (corrected by Bonferroni method) are shown.

Supplementary Table S2. List of 20 top ranked features in leave-one-out cycles

Input	Fast	Slow
Dissimilarity ^b	Homogeneity ^b	Inverse difference ^a
Difference variance ^b	Skewness ^b	Kurtosis ^a
Surface area/ Volume ^a	Surface area/ Volume ^a	Surface area/ Volume ^a
Surface area ^a	Surface area ^a	Surface area ^a
Inverse difference ^a	Inverse difference ^a	Sum of squares variance ^b
Skewness ^b	Sum variance ^a	Skewness ^b
Difference variance ^a	Kurtosis ^a	Cluster prominence ^b
Inverse difference ^c	Sum entropy ^a	Skewness ^c
Cluster shade ^c	Correlation ^a	Difference variance ^b
Cluster prominence ^a	Difference variance ^b	Sum entropy ^a
Skewness ^c	Cluster shade ^b	Homogeneity ^c
Sum entropy ^a	Sum entropy ^c	Information correlation 1 ^a
Cluster prominence ^b	Difference variance ^a	Volume ^a
Sum entropy ^b	Information correlation 1 ^a	Cluster prominence ^c
Correlation ^a	Correlation ^b	Difference variance ^c
Cluster prominence ^c	Cluster prominence ^c	Sum variance ^a
Maximum probability ^a	Compactness ^c	Standard deviation ^c
Kurtosis ^a	Cluster shade ^c	Range ^c
Min ^c	Cluster shade ^a	Kurtosis ^b
Correlation ^c	Sum of squares variance ^b	Interquantile range ^a

^aFeature extracted in preconstrast series

^bFeature extracted in the third postcontrast series

^cFeature extracted in the fifth postcontrast series

Supplementary Table S3. Performance of the predictive model with tumour maximum size as additional feature

Region	Luminal A	Luminal B	Basal-like	HER2	Mean
Entire tumour	0.768 (0.700, 0.836)	0.701 (0.630, 0.773)	0.669 (0.566, 0.772)	0.731 (0.644, 0.818)	0.718 (0.653, 0.783)
<i>p</i> -value	0.595	0.647	0.408	0.629	0.762
Subregion					
Input	0.881	0.786	0.829	0.769	0.815
95% CI	(0.820, 0.941)	(0.726, 0.846)	(0.760, 0.897)	(0.683, 0.854)	(0.773, 0.857)
<i>p</i> -value	0.339	0.418	0.510	0.679	0.646
Fast	0.881	0.799	0.804	0.844	0.829
95% CI	(0.830, 0.933)	(0.740, 0.859)	(0.730, 0.877)	(0.779, 0.910)	(0.777, 0.882)
<i>p</i> -value	0.704	0.428	0.341	0.721	0.591
Slow	0.866	0.818	0.814	0.810	0.828
95% CI	(0.805, 0.927)	(0.767, 0.870)	(0.743, 0.885)	(0.725, 0.895)	(0.795, 0.862)
<i>p</i> -value	0.427	0.593	0.319	0.911	0.682

p-values for comparisons between predictive models with and without tumour maximum size as additional variable

Supplementary Table S4. Performance of the predictive model with parenchymal density as additional feature

Region	Luminal A	Luminal B	Basal-like	HER2	Mean
Entire tumour	0.747	0.725	0.659	0.719	0.717
95% CI	(0.684, 0.809)	(0.647, 0.802)	(0.551, 0.767)	(0.630, 0.808)	(0.706, 0.728)
p-value	0.285	0.177	0.429	0.347	0.761
Subregion					
Input	0.862	0.761	0.849	0.766	0.804
95% CI	(0.805, 0.919)	(0.709, 0.812)	(0.779, 0.920)	(0.680, 0.851)	(0.730, 0.878)
p-value	0.583	0.107	0.448	0.593	0.316
Fast	0.885	0.776	0.810	0.840	0.821
95% CI	(0.836, 0.934)	(0.723, 0.829)	(0.740, 0.880)	(0.773, 0.907)	(0.785, 0.857)
p-value	0.599	0.125	0.719	0.822	0.416
Slow	0.851	0.808	0.826	0.820	0.824
95% CI	(0.794, 0.908)	(0.748, 0.868)	(0.762, 0.890)	(0.738, 0.901)	(0.777, 0.872)
p-value	0.708	0.645	0.619	0.433	0.712

p-values for comparison between predictive models with and without parenchymal density as additional variable

References

- [1]. Frey BJ, Dueck D. Clustering by passing messages between data points. *Science*. 2007; 315(5814): 972-6.
- [2]. Fan M, Cheng H, Zhang P, Gao X, Zhang J, Shao G, et al. DCE-MRI texture analysis with tumor subregion partitioning for predicting Ki-67 status of estrogen receptor-positive breast cancers. *J Magn Reson Imaging*. 2017.