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Electron dynamics in films made of transition metal nanograins embedded in SiO₂: Infrared reflectivity and nanoplasma infrared resonance

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We report on near normal infrared reflectivity spectra of ~ 550 nm thick films made of cosputtered transition metal nanograins and SiO₂ in a wide range of metal fractions. Co_{0.85}(SiO₂)_{0.15}, with conductivity well above the percolation threshold has a frequency and temperature behavior according to what it is found in conducting metal oxides. The electron scattering rate displays a unique relaxation time characteristic of single type of carriers experiencing strong electron-phonon interactions. Using small polaron fits we identify those phonons as glass vibrational modes. Ni_{0.61}(SiO₂)_{0.39}, with a metal fraction closer to the percolation threshold, undergoes a metal-nonmetal transition at ~ 77 K. Here, as it is suggested by the scattering rate nearly quadratic dependence, we broadly identify two relaxation times (two carrier contributions) associated to a Drude mode and a midinfrared overdamped band, respectively. Disorder induced, the midinfrared contribution drives the phase transition by thermal electron localization. Co_{0.51}(SiO₂)_{0.49} has the reflectivity of an insulator with a distinctive band at ~ 1450 cm⁻¹ originating in electron promotion, localization, and defect induced polaron formation. Angle dependent oblique reflectivity of globally insulating Co_{0.38}(SiO₂)_{0.62}, Fe_{0.34}(SiO₂)_{0.66}, and Ni_{0.28}(SiO₂)_{0.72}, reveals a remarkable resonance at that band threshold. We understand this as due to the excitation by normal to the film electric fields of defect localized electrons in the metallic nanoparticles. At higher oblique angles, this localized nanoplasma couples to SiO₂ longitudinal optical Berreman phonons resulting in band peak softening reminiscent to the phonon behavior undergoing strong electron-phonon interactions. Singular to a globally insulating phase, we believe that this resonance might be a useful tool for tracking metal-insulator phase transitions in inhomogeneous materials. © 2009 American Institute of Physics. [DOI: 10.1063/1.3126485]

I. INTRODUCTION

In the recent past there have been many attempts to describe the conduction mechanisms in films made of metallic grains in an insulating matrix films. Besides being mainly theoretical,¹ most experiments were carried out analyzing transport and magnetic measurements.² They have been mostly addressed to mechanisms behind transport and carrier scattering involving the Giant Hall effect^{3,4} which depends on a combination of nanoparticle diameter, interparticle distance, and size distribution.⁵ There have also been a plethora of theoretical work addressing the electronic transport in this kind of systems.⁶

Here we attempt to improve the understanding of spatially inhomogeneous systems with inherent complexity⁷ by expanding our knowledge on the electron dynamics in well characterized films made of transition metal nanograins cosputtered with SiO₂. Phonons are expected to be electron

dressed as in devices running from single molecular transistors to electron-phonon quantum dot interactions.⁸

We have carried out temperature dependent far infrared (FIR) measurements with techniques that allow a quantitative and reliable evaluation of samples with different metal transition volume fractions. We attribute significance to our study because it also reveals a behavior close what it is generally found in optical measurements for bulk conducting transition metal oxides where quenched disorder provides ground for rather complex behaviors.⁹

Examples of earlier spectroscopic work may be traced to absorption measurements by Devaty and Sievers¹⁰ on the study of ~ 100 Å Ag particles embedded in an insulating gelatin matrix. The optical properties of several volume fractions of Ag small particles in KCl were also studied by Cummings *et al.*;¹¹ Kim and Tanner¹² reported on the IR response of aluminum small particles and closer to our reflectivity work, Noh *et al.*¹³ studied percolation through optical properties of Ni-MgO composites. Having as common ground

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sample characterization by transmission electron microscopy (TEM) those measurements only achieve qualitative agreement when analyzed with the Maxwell–Garnet dielectric theory¹⁴ or effective medium approaches.^{15–17} Room temperature transmission measurements of cosputtered Ag–SiO₂ and Au–SiO₂ granular films with a wide metal fraction were studied by Cohen *et al.*¹⁸ It was concluded that metal particles as small as 20 Å have optical constants that do not differ significantly from those of the bulk metals. More recently, absorption and photoluminescence properties of sol-gel granular transition metals in SiO₂ matrices were reported by Yeshchenko *et al.*^{19,20}

Spatial homogeneity is at the basis of the understanding on the intrinsic behavior of transition metal oxides and, in particular, the metal to insulator transitions found in highly correlated oxides. Ranging from high T_c superconductors to manganites they show a plethora of properties related to several competing states due to subtle phase separations. These materials reveal intrinsic inhomogeneities found in manganites as nanoscale granularity.^{21,22} This might also be concomitant to cuprates where phase competition might be tied to oxygen vacancies distributed at random in the lattice inhomogeneous patterns reflecting disorder and distortion. Then, our results also aim to add a critical experimental view of the nature of metal-insulator transition in oxides as our results are from known samples made of components providing completely disordered environment. i.e., to contrast the way that it is currently understood the clean limit, against the relevance of incorporating inhomogeneities, i.e., quenched disorder, by which two states, insulating and metallic, coexist nearly degenerated.⁹ It is to also note that glassy behavior is claimed near a metal-insulator transition.^{11,22}

As a step toward that aim we show that our films, with plain glass network disorder as the main characteristic in the microscale, have a rather straight macroscale response to tools regularly used in the field of IR spectroscopy. In other words, what we analyze is the film response of nanoscale metallic objects in a macroscopic insulating matrix at the FIR-midinfrared (MIR) (wavelength: $\sim 2\text{--}1000\ \mu\text{m}$; wave-numbers $\sim 11\,000\text{--}20\ \text{cm}^{-1}$). We obtain spectra that are analogous to those regularly found in oxides in which we verify, as for transport measurements that in a suitable percolating network polarons are formed.

We selected for our study films with three different transition metal fractions whose response is assimilated to a metal oxide, to an intermediate case with lower conductivity, and to an insulator respectively. In the first case the temperature dependent specular reflectivity of Co_{0.85}(SiO₂)_{0.15} is found to have similar features as encountered in the current literature for conducting oxides. They have a Drude component, phonons mostly carrier screened at FIR frequencies, and a long tail that extends toward near infrared (NIR) associated with hopping electron conductivity, and the presence of strong electron-phonon interactions. Ni_{0.61}(SiO₂)_{0.39} represents the intermediate case that it is interesting because at about these metal transition concentrations, the percolating network is reduced. Being near the percolation threshold, they have giant enhancements in the two contributions to the Hall resistivity.^{3,4} The temperature dependent near normal

reflectivity shows that Ni_{0.61}(SiO₂)_{0.39} is a system in which the relative reduction in the number of carriers allows less screened phonon bands on the top of a continuum. In this example the spectra main features correspond to a weaker Drude Lorentzian, centered at zero frequency, and to a wide MIR overdamped oscillator. This is understood as a profile of convoluted states traced to transitions of localized charges that can be photoexcited to glass defects such as dangling bonds, these playing the role of unintended doping.

The third case is dedicated to samples in which most of the conducting critical paths are truncated and where nanoparticles are better defined. They now have IR spectra with well defined vibrational bands and an extra band $\sim 1450\ \text{cm}^{-1}$. Most remarkable, it is a distinctive resonant sharp peak found for the *P*-polarized angle dependent specular reflectivity. Found at the threshold edge of the band at $\sim 1450\ \text{cm}^{-1}$ associated with electron promotion to higher energies, it is interpreted as due to near surface defect localized electrons that shaking against the positive background create the electric dipole detected in the IR. These last measurements unequivocally individualize that edge, also found in all semiconducting oxides, as having an electronic origin.

We reason that all these measurements may also be thought as a helpful first experimental approach describing films made of real metal nanoparticles in an insulating environment yielding grounds for plasmon circuit design.²³

It is important to note that the overall properties discussed in the present manuscript apply to all our films regardless on the metal transition used in making the films. Our samples are superparamagnetic down to 4 K.

II. SAMPLE PREPARATION AND CHARACTERIZATION

TM_{*x*}(SiO₂)_{1-*x*} ($0 < x < 1$; TM=Fe, Co, Ni) $\sim 550\ \text{nm}$ thick films have been made by magnetron cosputtering. Films were deposited on glass and kapton substrates kept at room temperature. The chamber pressure before sputtering was kept at 10^{-7} torr. During the deposition, while the substrate was rotated to assure composition uniformity, the chamber was kept at 5 mTorr in an Ar atmosphere.

The metal volume fractions were controlled by changing relative sputtering rates and subsequently verified by energy dispersive x-ray spectroscopy (Philips EDAX XL30) which yielded $\sim 7\%$ uncertainty for the film metal fraction.

We have also characterized these samples by TEM and with small angle x-ray (SAXS) and wide angle x-ray (WAXS) scattering techniques.^{5,24} While two dimensional projection TEM images, shown in Figs. 1 and 2 for Co_{*x*}(SiO₂)_{1-*x*} and Ni_{*x*}(SiO₂)_{1-*x*}, respectively,²⁵ identify these systems as made of metallic nanoparticles, a three dimensional SAXS, probing a larger number of particles, suggests features typical of polydisperse systems. We conclude that the sputtering process generates a variety of amorphous larger structures, nanoparticles, and isolated atoms, regardless the metal transition volume fraction, with about 29% truly nanoparticles with a volume distribution histogram centered at $\sim 2.3\ \text{nm}$.²⁴

FIG. 1. Examples of TEM images for $\text{Co}_x(\text{SiO}_2)_{1-x}$, (a) $x=0.28$, (b) $x=0.45$, (c) $x=0.62$, and (d) $x=0.77$. Inset: x-ray diffraction pattern for $\text{Co}_{0.77}(\text{SiO}_2)_{0.23}$ (after Ref. 25).

III. EXPERIMENTAL AND SPECTRAL ANALYSIS

Temperature dependent NIR, MIR, and FIR reflectivity spectra between 30 and 11 000 cm^{-1} were measured in a Fourier transform IR (FT-IR) Bruker 113v and a FT-IR Bruker 66 interferometer with 2 cm^{-1} (FIR and MIR) and 6 cm^{-1} (NIR) resolution. Previously to each measurement, as prepared films were gently treated by passing on them a lens paper embedded in absolute alcohol. A gold mirror was used as 100% reference.

Our samples were mounted on a cold finger of an Oxford DN 1754 cryostat for measurements between 77 and 500 K.

FIG. 2. Examples of TEM images for $\text{Ni}_x(\text{SiO}_2)_{1-x}$, (a) $x=0.30$, (b) $x=0.40$, (c) $x=0.50$, and (d) $x=0.61$. Inset: x-ray diffraction pattern for $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$ (after Ref. 25).

For lower temperatures we also used a He-closed cycle refrigeration system (Displex) coupled to the Bruker 66 reflectivity attachment.

Polarized room temperature angle dependent reflectivity measurements between 20° and 70° have been done using a Spectra Tech Series 500 specular reflectance accessory inserted in the IR beam path. The radiation was polarized with a polarizer made of a gold wire grid on a KRS-5 substrate.

We estimated phonon frequencies using a standard multioscillator dielectric simulation fit of reflectivity spectra.²⁶ The dielectric function, $\epsilon(\omega)$, is given by

$$\epsilon(\omega) = \epsilon_1(\omega) + i\epsilon_2(\omega) = \epsilon_\infty \prod_j \frac{(\omega_{j\text{LO}}^2 - \omega^2 + i\gamma_{j\text{LO}}\omega)}{(\omega_{j\text{TO}}^2 - \omega^2 + i\gamma_{j\text{TO}}\omega)}. \quad (1)$$

We then optimized the calculated reflectivity against the experimental points and thus estimated the high frequency dielectric function, ϵ_∞ , the transverse and longitudinal optical (LO) phonon frequencies, $\omega_{j\text{TO}}$ and $\omega_{j\text{LO}}$, and their transverse and longitudinal damping constants, $\gamma_{j\text{TO}}$ and $\gamma_{j\text{LO}}$, respectively. We also calculated the S_j strength of the j th oscillator as

$$S_j = \omega_{j\text{TO}}^{-2} \frac{\left(\prod_k \omega_{k\text{LO}}^2 - \omega_{j\text{TO}}^2 \right)}{\left(\prod_{k \neq j} \omega_{k\text{TO}}^2 - \omega_{j\text{TO}}^2 \right)}. \quad (2)$$

In addition, when the spectra required it, we added the plasma contribution (Drude term) to the dielectric simulation function as

$$- \frac{[\omega_p^2 + (\gamma_p - \gamma_0)\omega]}{[\omega(\omega - i\gamma_0)]}, \quad (3)$$

where ω_p is the plasma frequency, γ_p is its damping, and γ_0 is understood as a phenomenological damping introduced to reflect lattice drag effects. When these two dampings are set equal, one retrieves the classical Drude formula.²⁷

From these analyses the real and imaginary parts of the dielectric function are extracted and used in the calculation of relaxation times as described below. They also allow to calculate the real part of the optical conductivity given by $\sigma_1(\omega) = (\omega/4\pi)\epsilon_2$, being ϵ_2 the imaginary part of the measured dielectric function.

The classical Drude model, describing free carriers contribution centered at zero frequency, may be extended to systems where strong electron-phonon interactions are conspicuous^{28,29} by making the damping term complex³⁰

This is the so-called extended Drude model³¹ useful in describing the coupling any bosonic field to a Fermi liquid. From this, the frequency dependent electronic scattering rate due to many-body interactions at a temperature T , $[1/\tau(\omega, T)]$, may be written as³⁰

$$\frac{1}{\tau(\omega, T)} = \frac{\omega_p^2}{4\pi} \text{Re} \left(\frac{1}{\sigma(\omega)} \right) = \left(\frac{\omega_p^2}{\omega} \right) \left(\frac{\epsilon_2}{(\epsilon_1^2 + \epsilon_2^2 + 1 - 2\epsilon_1)} \right). \quad (4)$$

Using this formalism, our findings for the three kind of as-deposited films will be presented. The first one as example of

FIG. 3. (Color online) Temperature dependent near normal reflectivity of $\text{Co}_{0.85}(\text{SiO}_2)_{0.15}$. Full line: experimental; superposing dot: fit. Inset: same sample metallic behavior. Note that here we plot resistance instead of resistivity because, although with almost the same slope, we found changes when probing the resistivity at different sites in a same film.

those with metal transition volume fractions well above the percolation threshold; a second set of samples with metallic fractions close to metal-insulating transition (where giant enhancements in the ordinary and extraordinary Hall effect are found); and a third group of samples with metallic concentrations characteristic of insulating films.

A. $\text{Co}_{0.85}(\text{SiO}_2)_{0.15}$: A film with metal fraction well above the metal-insulator transition

Figure 3 shows the temperature dependent near normal specular reflectivity of $\text{Co}_{0.85}(\text{SiO}_2)_{0.15}$ having similar features, as found in the current literature for conducting oxides, i.e., as consequence of the transition metal hybridization in the insulating matrix it behaves as a “dirty” metal. That is, from 30 to 11 000 cm^{-1} and from 30 to 495 K, the spectra have a Drude component, phonons mostly carrier screened at FIR frequencies, and a long tail that extends toward NIR. This last associated with hopping electron conductivity and the presence of strong electron-phonon interactions. The temperature dependence of these spectra is representative of any other film in which the transition metal volume fraction implies metallic electron conductivity. On cooling, the spectral weigh is shifted as the phonon-electron scattering diminishes allowing an increment in the Drude component.

It should also be noted that in order to obtain an excellent tail fit at MIR frequencies it is necessary to introduce highly overdamped oscillator above 1 eV. It may be interpreted as due to photoexcited discrete electronic transitions to midgap empty, glass related, defect levels. This coexists with the overwhelming contribution of freer electron hopping that screens this feature. This point will become clear discussing $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$ in Sec. III B.

Figure 4 shows the experimental scattering rate calculated using in Eq. (4). These results, linear above phonon frequencies, and with strong temperature dependence, are

FIG. 4. (Color online) Temperature dependent scattering rate for $\text{Co}_{0.85}(\text{SiO}_2)_{0.15}$.

typical of a single kind of carrier (i.e., one relaxation time) under the presence of a strong electron-phonon interactions.

Then, drawn by the remarkable similarity of our spectra with the known for bulk conducting oxides,³² and in an effort to identify the main optical phonon groups involved in the electron-phonon interactions, we have analyzed the real part optical conductivity, $\sigma_1(\omega) = (\omega/4\pi)\epsilon_2$ (ϵ_2 is the imaginary part of the dielectric function), within a small polaron context. For this purpose, we use the theoretical formulation for small polarons due to nondiagonal phonon transitions, as proposed by Reik³³ and Reik and Heese.³⁴ In this model, optical properties are due to carriers in one small band and interband transitions are excluded. Starting with a Holstein's Hamiltonian,³⁵ the frequency dependent conductivity is calculated using Kubo's formula.³⁶ Then, the real part of the optical conductivity for finite temperature, $\sigma_1(\omega, \beta)$ is given by

$$\sigma_1(\omega, \beta) = \sigma_{\text{DC}} \frac{\sinh\left(\frac{\hbar\omega}{2}\beta\right) \exp[-\omega^2 \psi^2 r(\omega)]}{\frac{\hbar\omega}{2} \beta [1 + (\omega\psi\Delta)^2]^{1/4}}, \quad (5)$$

$$r(\omega) = \left(\frac{2}{\omega\psi\Delta}\right) \ln\{\omega\psi\Delta + [1 + (\omega\psi\Delta)^2]^{1/2}\} - \left[\frac{2}{(\omega\psi\Delta)^2}\right] \{[1 + (\omega\psi\Delta)^2]^{1/2} - 1\}, \quad (6)$$

with

$$\Delta = 2\varpi_j\Psi, \quad (7)$$

and

$$\Psi^2 = \frac{\left[\sinh\left(\frac{1}{2}\hbar\varpi_j\beta\right)\right]}{2\varpi_j^2\eta}. \quad (8)$$

Here, the conductivity, $\sigma_1(\omega, \beta)$, $\beta = 1/kT$, is mainly three parameter dependent; $\sigma_{\text{dc}} = \sigma(0, \beta)$, the electrical dc conductivity; the frequency ϖ_j that corresponds to the average between the transverse and the LO mode of the j th reststrahlen band; and η , a parameter characterizing the strength

of the electron-phonon interaction, i.e., the average number of phonons that contribute to the polarization around a localized polaron. It is important to stress that from all these parameters, η , is the only actually free in the optical conductivity computation for each phonon frequency ω_j . This is because phonon frequencies are fixed by the reflectivity measurements and the dc-zero frequency-conductivity is known from independent transport measurements.³⁷ $\eta \sim 3$ implies a low to mild electron-phonon interaction while a value around 14 would be corresponding to the very strong end.³⁸

We assume that a frequency dependent conductivity results from the addition of Gaussian-like [Eq. (6)] individual contributions, each, calculated at a phonon frequency ω_j and a temperature T . The fits, applied to every experimental conductivity, are shown in Fig. 5. They are in very good agreement with the experimental data and their temperature dependence. The resistivities were constrained to positive values.

Starting from the lowest measured temperature, at 30 K (Fig. 5), a good reproduction requires to only allow as variables the first-order main vibrational frequencies of glass SiO₂. In spite of omitting an explicit correlation between the different contributions the fitted frequencies are in agreement with the experimental ones, and, as it is intuitively expected, at 30 K the electron-phonon parameters η_j ($j=1,2,3,4,5$), shown in Table I, are in a regime for stronger localization. It is worth mentioning that these values for the η 's, and the individualization of only fundamental lattice frequencies for the low temperature conductivities (stronger localization), are findings shared with earlier results in complex oxides.³⁹ They suggest a low temperature property for the IR optical conductivities that may apply to all alike oxides in a low temperature regime.

In contrast, when the temperature is raised to 300 K (Fig. 5), the highest frequency vibration mode at 980 cm⁻¹, and its overtone 1890 cm⁻¹, are singular to the fit at MIR frequencies.⁴⁰ That fundamental vibration band, ~ 980 cm⁻¹ in SiO₂, is assigned to the transverse optical of the asymmetric stretching modes (As1,As2) of the Si–O–Si.^{41,42} It has the total polarization enhanced by ion motion linked to that vibration.⁴³

The detected overtone implies stronger dipole moments generated by polaronic coupling between the charge and the vibrating lattice.³² Sum phonon processes of different orders are now expected to also contribute to the optical absorption blurring higher assignments due to a number of multiphonon individual combinations.³⁷ We note that Co_{0.85}(SiO₂)_{0.15} having, at 300 K, η 's from 5 to 7 (Table I), suggests phonon interactions in the mid to higher strength regime.

B. Ni_{0.61}(SiO₂)_{0.39}: A film near the percolation threshold

Ni_{0.61}(SiO₂)_{0.39} represents an intermediate case that it is of interest because at about these metal transition concentrations, near the percolation threshold, there are giant enhancements in the two contributions to the Hall resistivity. The ordinary that appears as consequence of the Lorentz force, and the extraordinary one, related to the spin-orbit coupling.

FIG. 5. (Color online) Temperature dependent optical conductivity of Co_{0.85}(SiO₂)_{0.15}. Full line: experimental; superposing dots: fit. The fit assumes that each conductivity is the sum of Gaussian-like [Eq. (6)] contributions (drawn in full lines) each calculated at a phonon frequency ω_j and at a temperature T (see text and Table I).

We have particularly chosen Ni_{0.61}(SiO₂)_{0.39} because this film also experiences a clear metal to nonmetal transition at ~ 77 K (inset, Fig. 6).

The temperature dependent near normal reflectivity of Ni_{0.61}(SiO₂)_{0.39} (Fig. 6) shows a system in which the reduction in the number of carriers allows less screened phonon

FIG. 6. (Color online) Temperature dependent near normal reflectivity of $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$. Full line: experimental, superposing dot: fit. Inset: same sample resistivity (dots indicate the temperatures at which the spectra were taken).

bands below 1000 cm^{-1} . These appear on the top of a continuum extending into the MIR. At 30 K, in the insulating regime, we did not consider the reflectivity in the higher frequency range (dotted line in Fig. 6) because the film and substrate interface seem to be inducing an interference pattern as the number of carriers is not enough to screen out the substrate.

From them, two main features are distinct in the spectra. One corresponds to a weaker Drude Lorentzian, centered at zero frequency, and another to a wide overdamped oscillator at MIR frequencies. This last is a common feature in oxides that it is usually interpreted in terms of d - d transitions, doped semiconductor, charge density wave ordering, or polarons.³² Plotted in Fig. 7, it is apparent that the MIR dipole weakens approaching the metal to insulator transition at $\sim 77 \text{ K}$ suggesting a complex carrier behavior in thermally driven processes. Their scattering rates, using Eq. (4), yield a clear departure from the linear behavior found in Sec. III A. Here, as it is shown in Fig. 8(b), it is close to having a quadratic frequency dependence.

Significantly, Nagel and Schnatterly^{44,45} showed that a two carrier response may be described by a dielectric function as given by

$$\epsilon(\omega) = 1 - \frac{4\pi N_a e^2}{m_a^*(\omega^2 + i\omega/\tau_a)} - \frac{4\pi N_b e^2}{m_b^*(\omega^2 + i\omega/\tau_b)}. \quad (9)$$

This yields an effective relaxation time

TABLE I. Parameters of the small polaron theory fit for the optical conductivity of $\text{Co}_{0.85}(\text{SiO}_2)_{0.15}$. Note that vibrational frequencies are in agreement with the film IR experimental bands (in brackets) and that the conductivity IR tail at higher than 30 K is dominated by the overtone of the vibrational band at $\sim 980 \text{ cm}^{-1}$. The fit resistivities, ρ_{dc} , are also included.

T (K)	ρ_{dc} ($\Omega \text{ cm}$)	η_1	ω_{ph1} (cm^{-1})	η_2	ω_{ph2} (cm^{-1})	η_3	ω_{ph3} (cm^{-1})	η_4	ω_{ph4} (cm^{-1})	η_5	ω_{ph5} (cm^{-1})
30	0.000 260	4.65	275.0(280)	5.7	357.1(361.3)	8.02	481.3(400)	10.81	670.7(575)	14.4	940.0(980)
77	0.000 488	2.0	281.0(280)	3.8	385.0 (381)	5.46	599.0(575)	7.4	943.0(980)	10.5	1469.0
300	0.002 416	5.2	283.0	4.9	380.0	5.51	560.0	5.72	1070.0	7.12	1950.0
495	0.002 569	9.4	280.0	5.9	340.0	5.7	590.0	5.65	1080	6.47	2040.0

FIG. 7. (Color online) Temperature dependent Drude and MIR oscillator for $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$. Inset: same sample resistivity.

$$\left(\frac{1}{\tau}\right)_{\text{eff}} = \frac{1}{\tau_a} \left[1 + \frac{B}{A} \left(\frac{\omega^2 + \tau_a^{-2}}{\omega^2 + \tau_b^{-2}} \right) \right]^{-1} + \frac{1}{\tau_b} \left[1 + \frac{A}{B} \left(\frac{\omega^2 + \tau_b^{-2}}{\omega^2 + \tau_a^{-2}} \right) \right]^{-1}. \quad (10)$$

Then, following Refs. 44 and 45, with $A=4\pi e^2 N_a/m_a^*$, and $B=4\pi e^2 N_b/m_b^*$, and if $\omega\tau_b \ll 1$ or if $\omega\tau_a > 1$, $\omega\tau_b < 1$ and $(2B/A) \omega^2 \tau_b^2 \ll 1$, Eq. (10) reduces to

$$(1/\tau)_{\text{eff}} \sim (1/\tau)_a + (\omega_p/\omega_p)_a \tau_b \omega^2 = a + b \cdot \omega^2. \quad (11)$$

This, originally developed for noble metal disordered films⁴⁴ has the experimental form of $(1/\tau)_{\text{eff}}$ found for electron scattering rate of $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$ [Fig. 8(a)]. We may then broadly state that two contributions, yielding a quadratic effective relaxation time—departing from the linear behavior found for $\text{Co}_{0.85}(\text{SiO}_2)_{0.15}$ (Fig. 3)—may be identified as for a sample where two kind of carriers coexist in different environments. In our case, it is likely to be more complex because the glass environment in which electrons move. Electrons with different electron densities, effective masses, and relaxation times, may be identified as globally belonging to two carrier assemblies⁴³ in the unavoidable structural imperfections of our samples. The MIR oscillator band (Fig. 7) may then be thought as a profile of convoluted states. In a band picture, they would originate in transitions from valence band to midgap empty states, here likely associated to originally localized electrons in topological glass defects such as dangling bonds and voids. These last playing the role

FIG. 8. (Color online) Temperature dependent scattering rate for $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$. (a) Linear plot; (b) same data plotted to show the near quadratic behavior.

of unintended doping in an amorphous environment. We might, alternatively, have argued that localized self-trapped charges that may be IR photoexcited are the ones creating the MIR band. However, we feel that the ideas as presented in the preceding paragraph are better in pointing to glass defects playing a role in the overall mechanism for hopping conductivity in our disordered films.

It was anticipated above that the coexistence of localized and itinerant carriers, promoted by the strong interactions between charge carriers and the ions, yields the formation of polarons. The increment in the surface to bulk ratio in the nanoparticles and the fact that transition metal ions in the nanoparticle surface might be uncoordinated (metal nanoaggregates might obey a dense random packing ordering as in amorphous metals)^{46,47} favor an atom relaxation mechanism interacting strongly with the highly polarizable $2p$ oxygen orbital.

Thus, the underlined polaronic nature of charge carriers in $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$ is again supported by the fitting to the experimental conductivities using Eq. (6). The fit parameters are shown in Table II. The temperature dependent optical conductivities of $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$, Fig. 9, show results similar to those for $\text{Co}_{0.85}(\text{SiO}_2)_{0.15}$. The η 's (Table II) characterizing the strength of the electron-phonon interaction suggests stronger localization, and, as found for $\text{Co}_{0.85}(\text{SiO}_2)_{0.15}$, when we increase the temperature higher order phonons play non-negligible role at MIR frequencies.

We also note that the consequences of electron thermal localization may quantitatively be estimated using the sum rule that allows calculating the area ratio of the MIR optical conductivity at 495 and 77 K. Thus,

$$N_{\text{eff}}(\omega) = \frac{2mV_{\text{cell}}}{\pi e^2} \int_0^{11000} \sigma_1(\omega') d\omega', \quad (12)$$

where N_{eff} is an effective carrier number, V_{cell} is a “volume cell,” m and e are the mass and charge, respectively, yields a rough estimated of about 82% on the relative number of localized carriers when the film cools to 77 K.

C. $\text{TM}_x(\text{SiO}_2)_{1-x}$ $0.55 > x > 0.0$, TM=Co, Ni, Fe: Films with metal fractions below the metal-insulator transition

We will now comment on our results for the case in which the amount of transition metal in the films is such that most of the conducting critical paths are truncated. Thus, as it is shown in Fig. 10 for $\text{Co}_{0.51}(\text{SiO}_2)_{0.49}$, the film near normal specular reflectivity displays well defined vibrational bands and a sharp threshold at $\sim 1250 \text{ cm}^{-1}$ (we ignore features at frequencies higher than $\sim 2100 \text{ cm}^{-1}$ because at about that value SiO_2 has the transmission edge beyond which a wavy interference pattern distorts the spectrum). It also shows that all bands undergo a redshift relative to pure SiO_2 glass (dashed line in Fig. 10). This kind of frequency shifts have been already found in ion implanted and irradiated glass samples where the bond angle tend to be smaller.⁴⁸ When the average Si–O–Si bond angle is reduced the fundamental Si–O asymmetric stretching vibration at $\sim 1000 \text{ cm}^{-1}$ shifts down in frequency.⁴⁹ We understand that shift as due to topological errors result of introducing the transition metal ions in the glass network with a possible contribution of

TABLE II. Examples of parameters for the small polaron theory fits to the optical conductivity of $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$. Note that vibrational frequencies are in agreement with the film IR experimental bands (in brackets) and that the conductivity tail for temperatures higher than 77 K is dominated by the overtone of the highest vibrational band at $\sim 1000 \text{ cm}^{-1}$. The fit resistivities, ρ_{dc} , are also included. For 77 K we also added an extra contribution as a low frequency phonon band at 210 cm^{-1} due the resonance (see text) distorting the conductivity edge. This effect was not considered for 200 K.

T (K)	ρ_{dc} ($\Omega \text{ cm}$)	η_1	ω_{ph1} (cm^{-1})	η_2	ω_{ph2} (cm^{-1})	η_3	ω_{ph3} (cm^{-1})	η_4	ω_{ph4} (cm^{-1})	η_5	ω_{ph5} (cm^{-1})	η_6	ω_{ph6} (cm^{-1})
77	0.007 65	8.19	210.0	7.17	410.0(423)	9.18	483.0 (495)	10.5	591.0(584)	11.66	820-(832)	7.85	1100.0(1126)
200	0.007 70	6.9	430.0(423)	7.5	490.0(495)	7.2	571.0(584.0)	7.7	830.0(832)	8.7	1100.0(1126)	11.3	1984.0

FIG. 9. (Color online) Temperature dependent optical conductivity of $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$. Full line: experimental; superposing dots: fit. The fit assumes that each conductivity is the sum of Gaussian-like [Eq. (6)] contributions (drawn in full lines), each calculated at a phonon frequency ω_j and at a temperature T (see text and Table II).

strong electron-phonon interactions and localization. We also note an unlike behavior for the reflectivity minimum in the carrier-LO mode interaction at 1210 cm^{-1} .

It is known that on cooling the reflectivity minimum, at approximately the highest LO frequency, undergoes a red-shift when there are strong electron-phonon interactions.⁵⁰ Moreover, the band centered at $\sim 1450 \text{ cm}^{-1}$, assigned to the electron promotion to higher energy available levels, is regularly found to increase in intensity. (e.g., see for $\text{Sr}_2\text{FeMo}_{0.2}\text{W}_{0.8}\text{O}_6$ in Ref. 51 (inset, Fig. 7)). Contrasting, the band minimum for $\text{Co}_{0.51}(\text{SiO}_2)_{0.49}$ at 1210 cm^{-1} (Fig. 10) although reproduces the behavior expected for strong electron-phonon interactions does also suggests that no much else is taking place in a wide range of temperatures. For this reason, to search and enhance any longitudinal contribution that might be hiding in the spectra, we also performed angle dependent reflectivity at room temperature.

FIG. 10. (Color online) Temperature dependent reflectivity of $\text{Co}_{0.51}(\text{SiO}_2)_{0.49}$. Dashed line is the SiO_2 glass reflectivity at room temperature. Inset: same sample resistivity (dots indicate the temperatures at which the spectra were taken).

Oblique reflectivity has been regularly use for detecting LO modes, lattice vibrations perpendicular to a film surface, in transmission mode. Berreman⁵² first pointed out that having radiation polarized parallel and perpendicular to the plane defined by the incident radiation and the normal to the film surface would allow to directly measure LO modes. Since transverse magnetic (TM) P -polarized radiation has a wave vector with components parallel and perpendicular to the film surface extra bands not seen in transverse electric S -polarization will appear.

In normal incidence, longitudinal modes are found at the minima (zero) of the dielectric function or a maximum of $\text{Im}\{-1/\epsilon\}$. In oblique reflectivity, the energy loss for incident radiation TM polarized reduces to

$$P \approx \frac{\epsilon_0 \omega}{2} \text{Im}\{\epsilon\} |E_N|^2 = \frac{\mu_0 \omega}{2} \sin^2 \alpha \text{Im}\left\{\frac{-1}{\epsilon}\right\} |H|^2, \quad (13)$$

where E_N is the electric normal field, H is the magnetic field parallel to the interfaces, and α is the angle of incidence.

FIG. 11. (Color online) Oblique IR reflectivity of SiO_2 at different incident angles.

FIG. 12. (Color online) Angle dependent oblique P -polarized IR reflectivity of $\text{Co}_{0.38}(\text{SiO}_2)_{0.62}$, $\text{Fe}_{0.34}(\text{SiO}_2)_{0.66}$, and $\text{Ni}_{0.28}(\text{SiO}_2)_{0.72}$ at 300 K. Circles enhance the onset of the remarkable nanoplasma resonance at the band threshold. For better viewing the spectra have been vertically displaced.

Thus, at the longitudinal modes the spectra will have a distinctive enhancement due to the maximum of $\text{Im}\{-1/\epsilon\}$ in contrast to transverse optical modes intensities.⁵³

Using this principle on glasses Almeida⁵⁴ showed that glass- SiO_2 sustains clear TO-LO splits for the main vibrational bands. Reproduced by us in Fig. 11, the profiles show that by increasing the angle of incidence the overall band weight shifts to higher frequencies peaking as expected at longitudinal modes. Main bands are rather broad because for each glass vibrational splitting, there might be several like modes contributing to the one band profile. We will call them Berreman phonons to differentiate those structures from an unexpected feature that becomes active in the reflectivity of our films at about the same frequencies.

Figure 12 shows the P -polarized angle dependent specular reflectivity of a number of insulating films. We note that as the angle increases in addition to much ill defined Berreman longitudinal phonons a sharp peak appears at the very edge of the 1450 cm^{-1} band. As it is seen for $\text{Co}_{0.38}(\text{SiO}_2)_{0.62}$, $\text{Fe}_{0.34}(\text{SiO}_2)_{0.66}$, and $\text{Ni}_{0.28}(\text{SiO}_2)_{0.72}$, this peak becomes stronger with increasing angle and at $\sim 70^\circ$ is the dominant feature.

To our knowledge, there is only one report that discusses a comparable phenomenon. Ahn *et al.*⁵⁵ working on Fe_3O_4 films deposited on a MgO substrate found a resonant band emerging on the top of the film reflectivity but related to the MgO LO phonons. We believe that the appearance of this resonance in our films has the same physical origin. Nominally, replacing the conducting Fe_3O_4 films by a metal nano-

particle and insulator MgO by the SiO_2 glass matrix we may understand our physical picture using the boundary conditions as proposed in Ref. 54.

The normal (E_N) and tangential (E_T) components at the boundary for the incident to the film electric field are then given by⁵³

$$E_N = -\sin \alpha \sqrt{\mu_0/\epsilon_0} H \begin{cases} 1/\epsilon, & \text{on the metal side,} \\ 1/\epsilon_{\text{matrix}}, & \text{on the glass side,} \end{cases} \quad (14)$$

$$E_T = \sqrt{\epsilon_{\text{matrix}} - \sin^2 \alpha} \times \sqrt{\mu_0/\epsilon_0} \times H \times 1/\epsilon_{\text{matrix}}, \quad \text{on both sides.} \quad (15)$$

We see that the tangential component E_T has a null condition at $\epsilon(\omega) \sim \sin^2 \alpha$. When this is satisfied, the field incident has only the normal component that in turn excites electrons in the nanoparticle. Thus, once the appropriate angle is reached, a collective electron oscillation is induced as a localized plasma with origin in the metallic nanostructure. The resonant plasma band, as it is shown in Fig. 12, appears at or slightly lower energy of the edge denoting the electron promotion by energetic enough photons. We then reason that the origin of the collective electron oscillation may be traced to electrons that are not able to overcome the metal-dielectric interface of the transition metal nanoparticles embedded in SiO_2 . Being localized, the collective cloud pairs with the positive ion background to yield a strong IR active electric dipole. The coupled oscillation-wave propagating photon-

FIG. 13. (Color online) 50° and 70° S -(dots) and P -(full line) polarized oblique reflectivity for $\text{Fe}_{0.34}(\text{SiO}_2)_{0.66}$ near the IR nanoplasma resonant frequency at 300 K.

FIG. 14. (Color online) Nanoplasma resonant peak frequency vs angle of incidence for $\text{Co}_{0.38}(\text{SiO}_2)_{0.62}$, $\text{Fe}_{0.34}(\text{SiO}_2)_{0.66}$, and $\text{Ni}_{0.28}(\text{SiO}_2)_{0.72}$. Dashed line is a guide for the eye.

electron cloud is known as plasma polariton.⁵⁶ On the other hand, the role of the nanoparticle irregular surface remains to be established since at metal-dielectric interfaces electron oscillations are confined to the surface and localization leads to giant enhancement of the local and electrical fields. In surface enhanced Raman scattering this principle, i.e., plasma localization in rough surfaces, is used to resolve molecule vibrational modes with highest resolution.⁵⁷

The longitudinal vibrations of $\text{Fe}_{0.34}(\text{SiO}_2)_{0.66}$ (Fig. 13), shown in Fig. 11 for SiO_2 , have stronger bands and shift in frequency as expected for the LO mode following Eq. (13) in every reststrahlen band. As the reflectivity angle is increased to 70° [Fig. 13(b)] the longitudinal mode merges with the resonant band inducing broadening and softening of the overall band profile. The pure longitudinal character of the resonant electronic cloud may also be visualized in Fig. 13 where the *S*-(TE) and *P*-(TM) polarized spectra are plotted. Figure 13(a) shows for 50° incidence the dissimilar profiles of the vibrational band, assigned to TO-LO antisymmetric stretching, against that of the resonance. This last has a corresponding *S*-polarized sharp antiresonance confirming its purely longitudinal character even for intermediate angles of incidence. When we plot (Fig. 14) peak positions against the incident angle we find two regimes. At low angles, the almost linear behavior is associated with the resonant condition leading the IR response while a strong departure from it is found at higher angles. It is as if the glass LO modes, interacting with the nanoplasma, experience a frequency shift reminiscent to phonons in oxides in an environment with strong electron-phonon interactions.^{49,50}

IV. CONCLUSIONS

Summarizing, we have shown the IR response for transition metal nanograins embedded in SiO_2 for three specific metal fractions. Well above the percolation threshold the films, regardless the transition metal, have the behavior known for conducting oxides with the characteristic hopping conductivity as transport mechanism. At intermediate concentrations the main feature in the IR spectra, in addition to

FIG. 15. (Color online) Angle dependent oblique *P*-polarized IR reflectivity of $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$ at 300 K. The circle points to the detection of the nanoplasma resonance in an electron screened environment. For better viewing the spectra have been vertically displaced relative to the one at 50° .

a Drude term, is a MIR band that in the case of $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$ follows a thermally driven metal-nonmetal phase transition. The polaron fit to the optical conductivity here shows a localization and stronger electron-phonon interaction.

A remarkable nanoplasma resonance is found in globally insulating films strongly interacting with Berreman phonons. Common to all our films the key for its unambiguous detection is the reduced number of free carriers. As in Fig. 15 for $\text{Ni}_{0.61}(\text{SiO}_2)_{0.39}$, if the films have enough hopping electrons the resonant peak will be only detected at the highest oblique configurations and even then, it would easily be confused by a regular phonon feature.

It is important to emphasize that hopping conductivity-polaron formation—midgap band assimilated to an overdamped oscillator—and the resonant condition are features always present for all metal fractions with different degree of occurrence. It depends on the fractional amount of transitional metal nanoparticles, and thus, on the number of carriers. The evolution of transport properties relies on the behavior of insulating and metallic aggregates reminiscent of highly correlated systems where there is coexistence of competing states in an inhomogeneous environment with nanometric scaling.^{58–61}

We may then conclude that the nanoplasma resonant band addressed in the above sections may turn to be a useful

tool to optically monitor with great detail a metal to insulator transition. While the resonance will be screened in a sample with enough hopping electrons it will be a sharp feature in globally insulating environments.

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